Zixiao Wu 515491-Individual Assignment 3

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R Markdown

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4.7 Exercises Problem 10

```
library(ISLR)
library(MASS)
library(class)
head(Weekly)
```

```
##
                   Lag2
                                  Lag4
                                         Lag5
                                                 Volume
                                                        Today Direction
     Year
            Lag1
                          Lag3
           0.816
## 1 1990
                  1.572 -3.936 -0.229 -3.484 0.1549760 -0.270
                                                                     Down
## 2 1990 -0.270
                  0.816
                        1.572 -3.936 -0.229 0.1485740 -2.576
                                                                     Down
## 3 1990 -2.576 -0.270
                         0.816
                                1.572 -3.936 0.1598375
                                                                       Uр
## 4 1990
           3.514 -2.576 -0.270 0.816
                                      1.572 0.1616300
                                                                       Uр
                  3.514 -2.576 -0.270 0.816 0.1537280
                                                                       Uр
           1.178  0.712  3.514  -2.576  -0.270  0.1544440  -1.372
                                                                     Down
```

attach(Weekly)

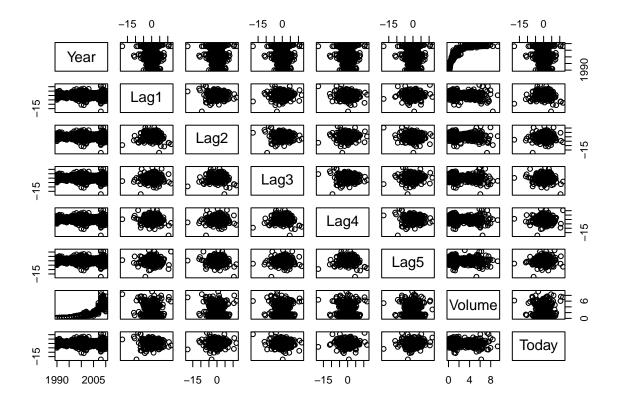
#(a)

summary(Weekly)

```
##
         Year
                         Lag1
                                              Lag2
                                                                   Lag3
##
    Min.
            :1990
                            :-18.1950
                                        Min.
                                                :-18.1950
                                                             Min.
                                                                     :-18.1950
##
    1st Qu.:1995
                    1st Qu.: -1.1540
                                         1st Qu.: -1.1540
                                                             1st Qu.: -1.1580
##
    Median:2000
                    Median :
                               0.2410
                                        Median:
                                                   0.2410
                                                             Median:
                                                                        0.2410
##
    Mean
            :2000
                               0.1506
                                         Mean
                                                   0.1511
                                                             Mean
                                                                       0.1472
##
    3rd Qu.:2005
                    3rd Qu.:
                               1.4050
                                         3rd Qu.:
                                                   1.4090
                                                             3rd Qu.:
                                                                       1.4090
            :2010
##
    Max.
                    Max.
                            : 12.0260
                                         Max.
                                                : 12.0260
                                                             Max.
                                                                     : 12.0260
##
         Lag4
                              Lag5
                                                 Volume
                                                                     Today
##
    Min.
            :-18.1950
                        Min.
                                :-18.1950
                                             Min.
                                                     :0.08747
                                                                Min.
                                                                        :-18.1950
    1st Qu.: -1.1580
                        1st Qu.: -1.1660
                                             1st Qu.:0.33202
                                                                1st Qu.: -1.1540
    Median :
               0.2380
                        Median:
                                   0.2340
                                             Median :1.00268
                                                                Median :
                                                                           0.2410
##
    Mean
              0.1458
                        Mean
                                  0.1399
                                             Mean
                                                     :1.57462
                                                                Mean
                                                                           0.1499
    3rd Qu.:
               1.4090
                        3rd Qu.:
                                  1.4050
                                             3rd Qu.:2.05373
                                                                3rd Qu.: 1.4050
##
           : 12.0260
                                : 12.0260
                                                     :9.32821
                                                                        : 12.0260
    Max.
                        Max.
                                             Max.
                                                                Max.
```

```
## Direction
## Down:484
## Up :605
##
##
##
##
```

pairs(Weekly[,1:8])



cor(Weekly[,1:8])

```
##
                Year
                             Lag1
                                         Lag2
                                                    Lag3
          1.00000000 -0.032289274 -0.03339001 -0.03000649 -0.031127923
## Year
         -0.03228927 1.000000000 -0.07485305 0.05863568 -0.071273876
## Lag1
         -0.03339001 -0.074853051 1.00000000 -0.07572091 0.058381535
## Lag2
         -0.03000649 \quad 0.058635682 \ -0.07572091 \quad 1.00000000 \ -0.075395865
## Lag3
         -0.03112792 -0.071273876  0.05838153 -0.07539587  1.0000000000
## Lag4
         -0.03051910 -0.008183096 -0.07249948 0.06065717 -0.075675027
## Lag5
## Volume 0.84194162 -0.064951313 -0.08551314 -0.06928771 -0.061074617
         -0.03245989 -0.075031842 0.05916672 -0.07124364 -0.007825873
## Today
##
                 Lag5
                           Volume
                                         Today
         ## Year
## Lag1
         -0.008183096 -0.06495131 -0.075031842
         -0.072499482 -0.08551314 0.059166717
## Lag2
```

```
## Lag3
          0.060657175 -0.06928771 -0.071243639
## Lag4
        -0.075675027 -0.06107462 -0.007825873
          1.000000000 -0.05851741 0.011012698
## Volume -0.058517414 1.00000000 -0.033077783
## Today 0.011012698 -0.03307778 1.000000000
From the numerical and graphical summaries above, we can know that there may be a positive relationship
\#(b)
log = glm(Direction ~ Lag1+Lag2+Lag3+Lag4+Lag5+Volume, data=Weekly, family=binomial)
summary(log)
##
## Call:
## glm(formula = Direction ~ Lag1 + Lag2 + Lag3 + Lag4 + Lag5 +
      Volume, family = binomial, data = Weekly)
##
## Deviance Residuals:
##
      Min
                1Q Median
                                  3Q
                                          Max
## -1.6949 -1.2565 0.9913 1.0849
                                      1.4579
##
## Coefficients:
              Estimate Std. Error z value Pr(>|z|)
## (Intercept) 0.26686 0.08593 3.106 0.0019 **
              -0.04127
                          0.02641 -1.563 0.1181
## Lag1
                          0.02686
                                   2.175 0.0296 *
## Lag2
              0.05844
## Lag3
              -0.01606
                          0.02666 -0.602 0.5469
## Lag4
              -0.02779
                          0.02646 -1.050 0.2937
              -0.01447
                          0.02638 -0.549 0.5833
## Lag5
## Volume
              -0.02274
                          0.03690 -0.616 0.5377
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
      Null deviance: 1496.2 on 1088 degrees of freedom
## Residual deviance: 1486.4 on 1082 degrees of freedom
## AIC: 1500.4
## Number of Fisher Scoring iterations: 4
We can see that Lag2 is significant in 99% confidencial level.
\#(c)
log_prob = predict(log, type="response")
log_pred = rep("down", 1089)
log pred[log prob > 0.5] = "up"
table(log_pred, Direction)
```

```
Direction
## log_pred Down Up
       down
             54 48
##
             430 557
       up
#mean(log_pred==Direction)
(54+557)/(54+557+48+430)
## [1] 0.5610652
557/(430+557)
## [1] 0.5643364
48/(54+48)
## [1] 0.4705882
From the confusion matrix we can know that the correct rate is 56.1%. When predicting a up market, the
#(d)
train = (Year < 2009)
Test = Weekly[!train ,]
Test_Direction= Direction[!train]
log2 = glm(Direction ~ Lag2, data=Weekly, family=binomial, subset=train)
log_prob2 = predict(log2,Test, type="response")
log_pred2 = rep("Down", nrow(Test))
log_pred2[log_prob2>0.5] = "Up"
table(log_pred2,Test_Direction)
##
            Test_Direction
## log_pred2 Down Up
##
        Down
               9 5
##
        Uр
               34 56
mean(log_pred2==Test_Direction)
## [1] 0.625
We can see the model has a correct rate of 62.5%.
\#(e)
lda = lda(Direction ~ Lag2, data=Weekly, subset=train)
lda_pred = predict(lda,Test)
table(lda_pred$class, Test_Direction)
```

```
##
         Test_Direction
##
          Down Up
##
             9 5
            34 56
##
     Uр
mean(lda_pred$class==Test_Direction)
## [1] 0.625
We can see the LDA model has the same corret rate as Logistic model.
\#(g)
set.seed(114514)
train.x = Lag2[train]
test.x = Lag2[!train]
train_direction = Direction[train]
dim(train.x) = c(985,1)
dim(test.x) = c(104,1)
knn_pred = knn(train.x, test.x, train_direction, k=1)
table(knn_pred, Test_Direction)
##
           Test_Direction
## knn_pred Down Up
##
       Down
              21 29
##
       Uр
              22 32
mean(knn_pred==Test_Direction)
## [1] 0.5096154
We can see that the correct rate is 50%, lower than the models above.
\#(h)
The logistic regression and the LDA. They are the methods with a higher correct rate, sensitivity and p
#(i)
#knn, k = 5
knn_pred2 = knn(train.x, test.x, train_direction, k=5)
table(knn_pred2, Test_Direction)
##
            Test_Direction
## knn_pred2 Down Up
##
        Down 15 22
               28 39
##
        Uр
```

```
mean(knn_pred2==Test_Direction)
## [1] 0.5192308
#knn, k = 10
knn_pred3 = knn(train.x, test.x, train_direction, k=10)
table(knn_pred3, Test_Direction)
##
            Test_Direction
## knn_pred3 Down Up
##
        Down
              19 19
##
        Uр
               24 42
mean(knn_pred3==Test_Direction)
## [1] 0.5865385
#logistic
log2 = glm(Direction ~ Lag2 + Volume, data=Weekly, family=binomial, subset=train)
log_prob2 = predict(log2, Test, type="response")
log_pred2 = rep("Down", 104)
log_pred2[log_prob2>0.5] = "Up"
table(log_pred2,Test_Direction)
##
            Test_Direction
## log_pred2 Down Up
##
        Down
               20 25
               23 36
##
        Uр
mean(log_pred2==Test_Direction)
## [1] 0.5384615
lda2 = lda(Direction ~ Lag2 + Volume, data=Weekly, subset=train)
lda_pred2 = predict(lda2,Test)
table(lda_pred2$class, Test_Direction)
##
         Test_Direction
##
          Down Up
            20 25
##
     Down
##
            23 36
    Uр
mean(lda_pred2$class==Test_Direction)
```

[1] 0.5384615

As the experiment above, the model which appears to provide the best results is knn(k = 10) model, with