# Ziyang GAO

Curriculum Vitae

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## Research Interests

Arithmetic geometry, (mixed) Shimura varieties, Diophantine geometry, families of abelian varieties, rational/integral points, transcendence problems.

#### Academic Positions

2024– **Professor**.

UCLA, CA, USA

2021–2024 **Professor**, W3 (highest level in the German system).

Leibniz University Hannover, Germany

2015–2021 **chargé de recherche**, (tenured junior researcher).

CNRS, Institut Mathématiques de Jussieu-Paris Rive Gauche, Paris, France

2016–2018 **Instructor**.

Princeton University, NJ, USA

2015–2016 **Member**.

Institute for Advanced Study (IAS), NJ, USA

#### Education

2012–2015 PhD of Math, Université Paris-Sud, France and Leiden University, Netherlands.

Supervisors: Emmanuel Ullmo and Bas Edixhoven

Dissertation: The mixed Ax–Lindemann theorem and its applications to the Zilber–Pink conjecture.

2011–2012 M2 (Master 2) of Math, Université Paris-Sud, France.

2010–2011 M1 (Master 1) of Math, University of Milan, Italy.

2006–2010 Bachelor of Science, Math, Peking University, China.

# Awards and Fundings

Spring 2026 Von Neumann Fellowship, IAS.

2025 Compositio Prize for the period 2020–2022.

- Awarded every 3 years to a paper published in the journal Compositio Mathematica. For my paper "Generic rank of Betti map and unlikely intersections".
- 2024 Frontiers Science Award.
- 2023 ICCM Best Paper Award (International Consortium of Chinese Mathematicians).
- 2022 David Goss Prize.
  Awarded every two years to mathematicians under 35 for outstanding contributions to number theory.
- 2020 ICCM Best Paper Award (International Consortium of Chinese Mathematicians).
- 09/2020- ERC Starting Grant "UnIntUniBd", approx. 1,5 million €. Early termination 09/2024
- 08/2025 after move to the US.
- 02/2020- research funding ANR T-ERC(7) "UniBdPt", approx. 120k €. Early termination in
- 07/2022 08/2020 after awarded ERC.
  - 2015 Stieltjes Prize.

Dutch mathematical thesis prize.

# **Publications and Preprints**

- 23 Hodge cycles and quadratic relations between holomorphic periods on CM abelian varieties (with E. Ullmo), *Preprint*, 2024.
- 22 **Heights and periods of algebraic cycles in families** (with S. Zhang), *Preprint*, 2024.
- 21 Bigness of the tautological line bundle and degeneracy loci in families of abelian varieties, *Compte-rendu*, 2024.
- 20 **Bi-**Q-structure on Hermitian symmetric spaces and quadratic relations between **CM periods** (with E. Ullmo and A. Yafaev), *Preprint*, 2024.
- 19 The Relative Manin–Mumford Conjecture (with P. Habegger), Preprint, 2023.
- Degeneracy loci in the universal family of abelian varieties (with P. Habegger), Journal of Number Theory (JNT Prime), vol. 270 (Proceedings of the Second JNT Biennial Conference 2022), p. 96-121, 2025. doi.org/10.1016/j.jnt.2024.05.015, published online in May 2024
- 17 **The Uniform Mordell–Lang Conjecture** (with T. Ge and L. Kühne), *Preprint*, 2021.
- 16 Recent developments of the Uniform Mordell-Lang Conjecture, Survey, 2021.
- 15 The Ax–Schanuel conjecture for variations of mixed Hodge structures (with B. Klingler), *Math. Annalen*, vol. 388, p. 3847–3895, 2024. doi.org/10.1007/s00208-023-02614-w, published online in April 2023
- 14 A consequence of the relative Bogomolov conjecture (with V. Dimitrov and P. Habegger), *Journal of Number Theory (JNT Prime)*, vol. 230 (Proceedings of the First JNT Biennial Conference 2019), p. 146–160, 2022.
- 13 **Uniformity in Mordell–Lang for curves** (with V. Dimitrov and P. Habegger), *Annals of Mathematics*, vol. 194, p. 237–298, 2021.

- 12 Uniform bound for the number of rational points on a pencil of curves (with V. Dimitrov and P. Habegger), *IMRN*, vol. 2021, p. 1138-1159, 2021. doi.org/10.1093/imrn/rnz248, published online in December 2019
- 11 **Generic rank of Betti map and unlikely intersections**, *Compositio Mathematica*, vol. 156 (12), p. 2469-2509, 2020.
- 10 **The Geometric Bogomolov Conjecture** (with S. Cantat, P. Habegger and J. Xie), *Duke Mathematical Journal*, vol. 170, p. 247-277, 2021.
- 9 Mixed Ax-Schanuel for the universal abelian varieties and some applications, *Compositio Mathematica*, vol. 156 (11), p. 2263-2297, 2020.
- 8 Faltings Heights and L-functions (with R. von Känel and L. Mocz), in "Arithmetic and Geometry: Ten Years in Alpbach" edited by Gisbert Wüstholz and Clemens Fuchs, *Annals of Mathematics Studies*, vol. 202, Princeton U. Press.
- 7 Appendix to **The Betti map associated to a section of an abelian scheme** (Y. André, P. Corvaja and U. Zannier), *Inventiones mathematicae*, vol. 222, p. 161-202, 2020.
- 6 Heights in families of abelian varieties and the Geometric Bogomolov Conjecture (with P. Habegger), *Annals of Mathematics*, vol. 189, p. 527-604, 2019.
- 5 **Panorama on Ax type transcendence results**, *Proceedings of the 7th ICCM*, vol. II, p. 33-52, International Press of Boston, 2019.
- 4 Enlarged mixed Shimura varieties, bi-algebraic system and some Ax type transcendental results, Forum of Mathematics, Sigma, vol. 7, 2019, e16.
- 3 About the mixed André-Oort conjecture: reduction to a lower bound for the pure case, *Comptes rendus Mathématique*, vol. 354, p. 659-663, 2016.
- 2 A special point problem of André-Pink-Zannier in the universal family of abelian varieties, Annali della Scuola Normale Superiore di Pisa, Classe di Scienze, vol. XVII, p. 231-266, 2017.
- 1 Towards the André-Oort conjecture for mixed Shimura varieties: the Ax-Lindemann theorem and lower bounds for Galois orbits of special points, *Journal für die reine und angewandte Mathematik* (*Crelle*), vol. 732, p. 35-146, 2017.

## Teaching

- Fall 2025 **207A**: Introduction to Shimura varieties and compactifications, *UCLA*, CA (USA).
- Spring 2025 **207C: Introduction to Arakelov Geometry**, *UCLA*, CA (USA).
- W&S 2025 Participating Number Theory Seminar: Mordell Conjecture, after Faltings 1983, *UCLA*, CA (USA).
- Winter 2025 **110BH: Honors Algebra**, *UCLA*, CA (USA).
- Spring 2024 Elliptic Curves, Leibniz University Hannover, Hannover (Germany).
  - Fall 2023 Algebraic Number Theory 2, Leibniz University Hannover, Hannover (Germany).

- Spring 2023 **Block seminar: Irrationality and Transcendence**, *Leibniz University Hannover*, Hannover (Germany).
- Spring 2023 **Block seminar : Mordell Conjecture**, *Leibniz University Hannover*, Hannover (Germany).
  - Fall 2022 **Diophantine Geometry**, *Leibniz University Hannover*, Hannover (Germany).
- Spring 2022 Algebraic Groups, Leibniz University Hannover, Hannover (Germany).
  - Fall 2021 **Diophantine Geometry**, *Leibniz University Hannover*, Hannover (Germany).
  - Sep 2021 minicourse at ETH-UZh-Sbg Arithmetic and Geometry Research Group workshop, Alpbach (Austria).
- Spring 2018 MAT 202, Linear Algebra with applications, Princeton University, NJ (USA).
  - Fall 2017 MAT 214, Numbers, Equations and Proofs, Princeton University, NJ (USA).
- Spring 2017 MAT 202, Linear Algebra with applications, Princeton University, NJ (USA).
  - Fall 2016 MAT 214, Numbers, Equations and Proofs, Princeton University, NJ (USA).
- Spring 2015 Number theory 2: Local fields, Leiden University, Leiden (Netherlands).
  - Fall 2014 Introduction to Algebraic Topology, Leiden University, Leiden (Netherlands).

## Long-term Visiting Scholar

- 07-09/2024 Morningside Center of Mathematics, Beijing, China.
- 01-04/2023 MSRI, Berkeley, CA, USA. For the special program "Diophantine Geometry".
  - Organizer of the Learning Seminar. Scientific program writer of the part "Uniform Mordell–Lang and adelic line bundles" and gave 2 lectures.
- 02-03/2022 IHES, Bures-sur-Yvette, France.
  - 08/2018 Morningside Center of Mathematics, Beijing, China.
- 2017-2018 Institute for Advanced Study (IAS), Princeton, NJ, USA.
  - 06/2017 Fields Institute, Toronto, Canada.

# Advising and mentoring

#### PhD thesis

- 2024- John Zhou, UCLA, CA, USA.
- 2024- Zhaobo (Tom) Han, UCLA, CA, USA.
- 2024 Ruida Di, Leibniz University Hannover, Germany.

#### PhD tutor

- 2020-2021 Camille Amoyal, Sorbonne Université, France.
- 2019-2021 **Zhouhang Mao**, Sorbonne Université, France.

#### Bachelor and master thesis

- 2023 **Justus Wiegand**, bachelor, Leibniz University Hannover, Germany.
- 2022 Maximilian Rabeler, master, Leibniz University Hannover, Germany.

- 2021 Ruida Di, master, Sorbonne Université, France.
- 2019 **Sou-Manh Chhin**, master, Université Paris-Diderot, France.
- 2018 **Zhenlin Ran**, master, Université Paris-Diderot, France.

#### **Postdocs**

- **Riccardo Pengo**, *Leibniz University Hannover*, Germany, 10/2023-09/2024. Tenure-track researcher at University of Messina (Italy).
- **Francesco Campagna**, *Leibniz University Hannover*, Germany, 10/2022-08/2023. Assistant Professor with tenure at Clermont-Ferrand (France).
- **Hang Fu**, *Leibniz University Hannover*, Germany, 10/2022-09/2024. Postdoc at Basel (Switzerland).
- **Gabriel Dill**, *Leibniz University Hannover*, Germany, 04/2022-09/2023, on leave 01-05/2023 for a postdoc at MSRI.

Assistant Professor at Neuchêtal (Switzerland).

- **Guy Fowler**, *Leibniz University Hannover*, Germany, 10/2021-09/2024. Postdoc at Manchester.
- Jinzhao Pan, Sorbonne Université and Leibniz University Hannover, France and Germany, 01/2021-09/2024.
   Postdoc at Shanghai Jiaotang University.

# Acdemic Experience

#### (Selected) Conferences Talks

- Nov 2025 Diophantine approximation and transcendence, CIRM, Luminy (France).
- Sep 2025 Frontier in Mathematical Sciences, Hong Kong.
- Jul 2025 section "Varieties over global fields" of SRI (Algebraic Geometry conference every 10 years), Colorado (USA).
- Jun 2025 Complex Geometry and Beyond (Ngaiming Mok's 70th birthday conference), Shanghai (China).
- Sep 2024 Southern California Number Theory Day, Irvine (CA, USA).
- Jul 2024 Conference on "Arithmetic Geometry" in Honour of Gerd Faltings' 70th Birthday, Bonn (Germany).
- Jul 2024 The 2nd International Congress of Basic Science, Beijing (China).
- Jul 2024 The Mordell conjecture 100 years later, Boston (MA, USA).
- Dec 2023 2023 Winter Meeting in Algebra and Geometry, Rome (Italy).
- Aug 2023 Recent Developments in Algebraic Geometry, Arithmetic and Dynamics (Part II), Singapore.
- Aug 2023 PKU Mathematics Forum (Peking University), Beijing (China).
- Apr 2023 Degeneracy of algebraic points, MSRI, Berkeley (CA, USA).
- Feb 2023 Introductory Workshop: Diophantine Geometry, MSRI, Berkeley (CA, USA).

- Sep 2022 Number Theory Days, Lausanne (Switzerland).
- Sep 2022 O-minimality and Diophantine Geometry (Jonathan Pila's 60th birthday), Oxford (UK).
- Aug 2022 Mordell 2022: 100 years of elliptic curves, Cambridge (UK).
- Jul 2022 Second JNT Biennial Conference, Cetraro (Italy).
- Jun 2022 Modern Breakthroughs in Diophantine Problems, Banff (Canada), participation online.
- May 2022 Simons Symposium on Periods and L-Values of Motive, Simons Foundation, Scotland.
- Apr 2022 Diophantische Approximationen (ID 2216), Oberwolfach (Germany).
- Mar 2022 Rational Points 2022, Franken-Akademie Schloss Schney (Germany).
- Dec 2021 3rd Kyoto-Hefei workshop on arithmetic geometry, Kyoto (Japan), participation online.
- Sep 2021 Arakelov Geometry (SFB 1085 Higher Invariants Interactions between Arithmetic Geometry and Global Analysis), Regensburg (Germany).
- Aug 2021 Arithmetic of Shimura varieties over global fields, Cetraro (Italy).
- June 2021 Recent Developments in Algebraic Geometry, Arithmetic and Dynamics (Part I), Singapore, participation online.
- Dec 2020 ICCM (International Consortium of Chinese Mathematicians), *plenary speaker*, Hefei (China), participation online.
- Feb 2020 DART (Differential Algebra and Related Topics) X, CUNY (NY, USA).
- Sep 2019 Topics in Rational and Integral Points, Basel (Switzerland).
- Jul 2019 First JNT Biennial Conference, Cetraro (Italy).
- Jul 2019 Journée Gretchen & Barry Mazur, IHÉS (France).
- Jan 2019 International Conference on Periods and L-functions (Gisbert Wüstholz's 70th birthday), Sanya (China).
- May 2018 Shimura varieties and hyperbolicity of moduli spaces, Montréal (Canada).
- May 2018 Diophantine Geometry, CIRM, Luminy (France).
  - Jul 2017 Specialization Problems in Diophantine Geometry (Umberto Zannier's 60th birthday), Cetraro (Italy).
- Feb 2017 Heights and Applications to Unlikely Intersections, Fields Institute (Canada).
- Nov 2016 Second Sino-French Conference in Arithmetic Geometry at TSIMF, Sanya (China).
- Aug 2016 7th International Congress of Chinese Mathematicians, Beijing (China).
- Jun 2016 Arithmetic and Geometry: Ten years in Alpbach, Alpbach (Austria).
- May 2016 Hauteurs de Faltings des variétés abéliennes CM, Gronoble (France).
- Apr 2016 Diophantische Approximationen (ID 1615), Oberwolfach (Germany).
- Jun 2015 Sino-French research institute on arithmetic geometry, Beijing (China).
- Jul 2014 Second ERC Research Period on Diophantine Geometry, Cetraro (Italy).
- Mar 2014 On Lang and Vojta's conjectures, CIRM, Luminy (France).

#### Colloquium and Seminar Talks

- 2025 Minnesota (colloquium), Stanford, Caltech.
- 2024 IAS-Princeton joint, Columbia-CUNY-NYU joint, UCLA, Northwestern, UW Seattle, VaNTAGe; Jussieu Paris; National University of Singapore, SUSTech (Shenzhen, China).
- 2023 UCLA (colloquium), UW-Madison (colloquium), Duke (Frontiers), Number Theory Web Seminar; Dutch Intercity Number Theory Seminar, Clermont-Ferrand (France); National University of Singapore (colloquium).
- 2022 Yale (colloquium), Boston University, UCLA.
- 2021 Brown, UCSB; Chalmers/Gothenburg joint, Göttingen–Hannover joint; SUSTech (Shenzhen, China).
- 2020 Harvard, Berkeley; Bordeaux, Groningen (Netherlands), HUJI-BGU (Isreal), London, Paris Algebraic Cycles, Warwick–Oxford–Reading–Kings joint; Morningside Center (Beijing, China).
- 2019 MIT, Columbia; Cambridge UK, Humboldt Universität zu Berlin, Dortmund (Germany), ENS Lyon, Jussieu Paris; Peking University (Beijing, China), SUSTech (Shenzhen, China).
- 2018 IAS-Princeton joint, Columbia-CUNY-NYU joint; University of Zurich, Humboldt Universität zu Berlin; University of Hong Kong.
- 2017 Berkeley, IAS-Princeton joint; Amsterdam, Leiden; Fudan University (Shanghai, China).
- 2016 Columbia-CUNY-NYU joint; Basel, Clermont-Ferrand (France), IHÉS.
- 2015 IAS member talk, Northwestern, Rutgers at Newark, University of Connecticut; Jussieu Paris, SNS Pisa; Morningside Center (Beijing, China).
- 2014 Jussieu Paris, Orsay, IHÉS.

### Services

#### Journal activities

- 2023- Expositiones Mathematicae, Associate editor.
- 2022-2023 Expositiones Mathematicae, Leading guest editor for the special volume in memory of Bas Edixhoven.
  - 2015- Referee for Annals of Mathematics, Publ. I'IHES, JAMS, Acta. Math., Inv. Math., Forum of Mathematics (Pi & Sigma), Duke Mathematical Journal, JEMS, Annales de I'ENS, Compositio Mathematica, Mathematische Annalen, Algebra & Number Theory, IMRN, etc.
  - 2020- Referee for grants, including ISF (Israel), ANR (French), ERC (European).

    Department services
- 2024–2025 Graduate admission committee at UCLA (CA, USA).

- Fall 2022 Hiring committee of W1 (junior professor) position at Leibniz University Hannover (Germany).
- Mar 2022-Jun Deputy management of the Institute of Algebra, Number Theory and Discrete Mathe-
  - 2024 matics at Leibniz University Hannover (Germany).

#### Broader impacts

- 2026 David Goss Prize committee.
- Jul 2026 Organizer of the "4th JNT biennial conference", Cetraro (Italy).
- Sep 2025 Organizer of "Arithmetic and Diophantine Geometry, via ergodic theory and o-minimality (in honor of Emmanuel Ullmo's 60th birthday)", IHES (France).
- Aug 2025 Organizer of "Arithmetic Dynamics and Diophantine Geometry", NUS (Singapore).
- Jul 2025 SRI (Algebraic Geometry conference every 10 years), organizer of the section "O-minimality and arithmetic aspects of Hodge theory", Colorado (USA).
- Oct 9 2024 Scientific American report on my work on Uniform Mordell-Lang.
  - 2024 David Goss Prize committee.
  - Aug 2024 Organizer of the "3rd JNT biennial conference", Cetraro (Italy).
- summer 2024 Mentor and adviser of undergraduate research project "Special subvarieties of mixed Shimura varieties and Ribet sections", Beijing (China).
  - Oct 2023 Scientific committee of the "2nd Algant Alumni Network Symposium", St Jacut de La Mer (France).
- Jun 23, 2023 Organizer of "Women in Math Lunch", Hannover (Germany).
- Apr 7, 2023 Panellist of "Academic job applications (general process, with a focus on tenure track jobs)", MSRI, Berkeley (CA, USA).
- Jul 13, 2022 Organizer of "Women in Math Lunch", Hannover (Germany).

## Organization of seminars

- 2021-2024 Organizer of the Arithmetic Geometry and Number Theory Seminar at Leibniz University Hannover (Germany).
- 2021-2022 Organizer of the working group "Adelic line bundles on quasi-projective varieties", joint between Leibniz University Hannover (Germany) and University of Basel (Switzerland).
- 2020-2021 Organizer of the working group "Rational points and uniformity" at Sorbonne Université, Paris (France).
- 2018–2021 Organizer of the Number Theory Seminar of IMJ-PRG (Paris 6 and 7 joint), Paris (France).
- 2016-2017 Organizer of the Princeton University-IAS joint Number Theory Seminar, NJ (USA).
- 2012-2014 Organizer of Séminaire MathJeunes, Paris (France).

## Languages

Madarin Chinese (Native), French (Fluent), English (Fluent), Cantonese (Good), Italian (Intermediate).