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ISLET / R / islet.test.R



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```
1 #####
2 #####
3 #####
4 ##functions for LRT
5 #####
6 #####
7 #####
8 #(1) data prep for LRT
9 #function to change input format wrt to each cell type, to get ready for LRT
10 changeinput<-function(dc, iK){
11     K <- dc@K
12     X.tmp1 <- dc@X
13     X.tmp2 <- X.tmp1[, -(K+iK)]
14     dc@X <- X.tmp2
15     return(dc)
16 }
17
18 changeinput_slope<-function(dc, iK){
19     K <- dc@K
20     X.tmp1 <- dc@X
21     ## For slope test, the parameters being tested are: B_t[(3*K+1):(4*K)]
22     X.tmp2 <- X.tmp1[, -(3*K+iK)]
```

```
23     dc@X <- X.tmp2
24     return(dc)
25 }
26
27
28 #(2) LRT function in Unix and Windows
29 ###function to implement EM algorithm in ISLET algorithm
30
31
32 ###function to implement EM algorithm in ISLET algorithm
33 #function here for windows only, using lapply, no parallel computing
34 ✓ islet.lrt.block<-function(Y, datuse, ktest){
35     #exp_case = as.matrix(datuse@exp_case)
36     #exp_ctrl = as.matrix(datuse@exp_ctrl)
37     X <- datuse@X
38     A <- datuse@A
39     K <- datuse@K
40     NU <- datuse@NU
41     NS <- datuse@NS
42     # para <- datuse@para
43
44     #initialization of parameters parameter estimation storage
45     B_est <- NULL
46     Sig0_est <- NULL
47     SigU_est <- NULL
48     E_U_est <- NULL
49     llk <- NULL
50     ##
51     Y <- t(Y)
52     G <- ncol(Y)
53     # Y=log2(Y+1)
54
55     #####1. Initialization of parameters
56     #1.1 cell type profiles AND csDE B parameters
57     #B_0 = solve(X, Y)
58     B_0 <- Matrix::tcrossprod( Matrix::tcrossprod(solve( Matrix::crossprod(X)). X). t(Y))
```



```
59
60 #1.2 error terms
61 # sig <- mean((Y-X%*%B_0)^2)
62 sig <- colMeans((Y-X%*%B_0)^2)
63 #sig <- 20
64
65 #1.3 missing values
66 U_0 <- rep(0, NU*K)
67
68 B_t <- B_0
69 #sig_t = rep(sig, 7)
70 U_t <- U_0
71 #sig0_t <- rep(sig, G)
72 #sigK_t <- rep(sig, K)
73 sig0_t <- sig #rep(sig, G)
74 sigK_t <- matrix(rep(sig, each=K), nrow=K)
75
76 iem <- 1
77 diff1 <- 100
78 diff2 <- 100
79 pp <- 1
80 norm <- mean(colMeans(Y))
81
82 #Sig_U = diag(rep(sigK_t, each = NU))
83 Sig_p<-lapply(seq_len(G), function(x, A, sig0_t, sigK_t, NU, Y, X, B_t){
84   #invSig_U<-Matrix::bdiag(diag(rep(1/sigK_t, each=NU)))
85   invSig_U<-Matrix::bdiag(diag(rep(1/sigK_t[,x], each=NU)))
86   Sig<-solve( Matrix::crossprod(A)/sig0_t[x]+invSig_U)
87   hftmp1 <- Matrix::tcrossprod(Sig, A)
88   hftmp2 <- BiocGenerics::t(Y[, x] - Matrix::tcrossprod(X, BiocGenerics::t(B_t[, x])))
89   U<- Matrix::tcrossprod(hftmp1, hftmp2)/sig0_t[x]
90   return(list(Sig=Sig, U=U))
91 }, A, sig0_t, sigK_t, NU, Y, X, B_t)
92 E_Up<-do.call(cbind, lapply(Sig_p, function(x)x$U))
93
94
```



```

95 while(iem<15){
96   # cat("iteration=", iem, "\n")
97   iem <- iem + 1
98   #####2. E-step
99   #observed data COV(Y) = V
100
101   #V = A**Sig_U**t(A) + diag(rep(sig0_t, 5*600))
102
103   #2.1 E[U|Y]: missing data [U|Y] given observed data
104   #invV = solve(V)
105   # E_U = mu_p = t(Sig_U) **% t(A) **% invV **% (Y - X **% B_t)
106   # Sig_p = Sig_U - crossprod(Sig_U,t(A)) **% invV **% A **% Sig_U
107
108   # Estimate from last iteration
109
110   E_U <- E_Up
111   mu_p <- E_Up
112   E_U_frame <- as.data.frame(as.matrix(E_U))
113   #2.2 E[t(S)S|Y]
114   E_StS <- lapply(seq_len(G), function(x, A, Sig_p, mu_p, X, B_t, Y){
115     sum( Matrix::diag(Matrix::tcrossprod( Matrix::tcrossprod(A, Sig_p[[x]]$Sig), A))) +
116     sum(( Matrix::tcrossprod(A, BiocGenerics::t(mu_p[, x])) +
117       Matrix::tcrossprod(X, BiocGenerics::t(B_t[, x])) - Y[, x])^2)},
118     A, Sig_p, mu_p, X, B_t, Y)
119   E_StS <-unlist(E_StS)
120
121   #2.3 E[U_k^T U_k|Y]
122   mutra_split <- lapply(Sig_p, function(x){
123     sig_p<-split(diag(x$Sig), ceiling(seq_len(NU*K)/NU))
124     tra<-unlist(lapply(sig_p, sum))
125     return(tra)
126   })
127   mu_split <- split(E_U_frame, ceiling(seq_along(E_U_frame[, 1])/NU))
128
129   E_UkTuk <- do.call('cbind', mutra_split) + do.call('rbind', lapply(mu_split, colss))
130

```

每种cell-type
是个 σ_i^2

$u \sim N(0, \Sigma_u)$
相当于每个人有一个 $J \times K$ 的 vector
indicate individual variance
 $u \in (J \times K) \times 1$.

Given that $A \in N \times (J \times K)$

$\Sigma_u \in (0, +\infty)^{(J \times K) \times (J \times K)}$
 $\Rightarrow Au \in \mathbb{R}^{J \times K \times 1}$
每个人自己的

$\Rightarrow u = \begin{bmatrix} u_{11} \\ u_{21} \\ \vdots \\ u_{j1} \\ u_{12} \\ u_{22} \\ \vdots \\ u_{jk} \end{bmatrix}$
 $\Sigma_u = \begin{bmatrix} \sigma_1^2 & & & & & \\ & \sigma_1^2 & & & & \\ & & \ddots & & & \\ & & & \sigma_1^2 & & \\ & & & & \sigma_2^2 & \\ & & & & & \ddots \\ & & & & & & \sigma_2^2 & \\ & & & & & & & \ddots \\ & & & & & & & & \sigma_k^2 \end{bmatrix} (J \times K) \times (J \times K)$

param of interest:
 β, σ, u .

fixed effect

$$y|u \sim N(X\beta + Au, \sigma^2 I)$$

$$\hat{\beta} \leftarrow \text{regression algorithm}$$

$$\text{diff}_1 = \sum (|\beta^{(t+1)} - \beta^{(t)}| +$$

$$|\sigma^{(t+1)} - \sigma^{(t)}| +$$

$$\text{diff}_2 = \sum (|Eu^{(t+1)} - Eu^{(t)}|) / (JK \cdot \bar{y}^2)$$

random-effect. average of EU 的变化量.

given that JK, \bar{y} 已知, 只要 diff2 收敛,
 $< 1e-5$

```

####3. M-step
#3.1 B
B_tp <- Matrix::tcrossprod( Matrix::tcrossprod(solve( Matrix::crossprod(X)), X),
                           BiocGenerics::t(Y- Matrix::tcrossprod(A, BiocGenerics::t(E_U))) )

#make correction in case B[1:K]<0 or B_tp[(K+1):2K]<0
#important to bound the estimation to positive values

# B_tp[1:K,]=ifelse(B_tp[1:K,]<0,0,B_tp[1:K,])
# B_tp[-(1:K),]=ifelse(B_tp[1:K,]+B_tp[-(1:K),]<0,-B_tp[1:K,],B_tp[-(1:K),])

#3.2 sigma_0^2
sig0_tp <- E_StS/(NS)

#3.3 sigma_k^2
sigK_tp <- E_UkTUK/(NU)

####4. Stopping criteria
diff1 <- sum(abs(B_tp - B_t)) + abs(sig0_tp - sig0_t) + sum(abs(sigK_tp - sigK_t))

n1 <- sum(abs(B_tp - B_t))/length(B_tp)
n2 <- sum(abs(B_tp))/length(B_tp)
pp <- n1/n2
#   cat("B_sum_val=", n2, "\n")
#   cat("B_change_val=", n1, "\n")
#   cat("B_change_prop=", pp*100, "% \n")

####5. Update params
B_t<-B_tp
sig0_t <- sig0_tp
sigK_t <- sigK_tp

Sig_p<-lapply(seq_len(G), function(x, A, sig0_t, sigK_t, NU, Y, X, B_t){
  Sig_U<- Matrix::bdiag(diag(rep(sigK_t[, x], each=NU)))
  invSig_U<-Matrix::bdiag(diag(rep(1/sigK_t[, x], each=NU)))

```

```

166     invSig_U<-Matrix::bdiag(diag(rep(1/sig0_t[x], each=nrow(A))))
167     Sig<-solve( Matrix::crossprod(A)/sig0_t[x]+invSig_U)
168     U<- Matrix::tcrossprod(Matrix::tcrossprod(Sig, A),
169                             t(as.matrix(Y[, x] -
170                                 Matrix::tcrossprod(X, BiocGenerics::t(B_t[, x])))) )/sig0_t[x]
171     return(list(Sig_U=Sig_U, Sig=Sig, U=U))
172 }, A, sig0_t, sigK_t, NU, Y, X, B_t)
173 Sig_p_all<-NULL
174 # Sig_p_all=do.call(rbind, Sig_p)
175 # E_Up_all=Sig_p_all%*% t(A)%*% (Y - X %*% B_t)/sig0_t
176 # E_Up_diag=split(as.data.frame(as.matrix(E_Up_all)), rep(1:G, each=ncol(A)))
177 E_Up<-do.call(cbind, lapply(Sig_p, function(x)x$U))
178
179     diff2 <- sum(abs(E_Up - E_U))/(length(E_U)*mean(colMeans(Y))^2)
180 #     cat("Random effect diff2=", diff2, "\n")
181
182 }
183 # Estimate of fixed effect
184 B_est<-cbind(B_est, B_t)
185 # Estimate of random effect
186 E_U_est<-cbind(E_U_est, E_Up)
187 # Estimate of variance Sigma_U, Sigma_0
188 Sig0_est <- cbind(Sig0_est, sig0_t)
189 SigU_est <- cbind(SigU_est, sigK_t)
190
191 #calculate LLK
192 llk<-lapply(seq_len(G), function(x){
193     Sig<- Matrix::tcrossprod( Matrix::tcrossprod(A, Sig_p[[x]]$Sig_U), A)+
194         Matrix::bdiag(diag(sig0_t[x], nrow = nrow(A)))
195     l<- Matrix::determinant(Sig)$modulus+
196         Matrix::tcrossprod(Matrix::crossprod(Y[, x]- Matrix::tcrossprod(X, BiocGenerics::t(B_t[, x])),
197                                     solve(Sig)),
198                             BiocGenerics::t(Y[, x]- Matrix::tcrossprod(X,
199                                     BiocGenerics::t(B_t[, x])))) )
200     return(-as.numeric(l))
201 })
202

```



```

202      llk<-unlist(llk)
203
204      #compile return list
205
206      LLK <- llk
207      return(LLK)
208
209      #cat("Complete: LRT calculation for one cell type.")
210  }
211
212
213
214  ###Wrap function to run ISLET LRT, using parallel computing
215  #ipc is the index of parallel computing for
216
217  ✓ isletTest<-function(input, BPPARAM=bpparam() ){
218      G <- nrow(input@exp_case)
219      type<-input@type
220      Yall<-as.matrix(cbind(input@exp_case, input@exp_ctrl))
221      aval.nworkers<-BPPARAM$workers
222      block.size<-max(ceiling(G/aval.nworkers), 5)
223      Yall.list <- split(as.data.frame(Yall), ceiling(seq_len(G)/block.size))
224
225      # if(.Platform$OS.type == "unix") {
226      ## do some parallel computation under Unix
227      #     multicoreParam <- MulticoreParam(workers = ncores)
228      mf <- bplapply(X=Yall.list, islet.solve.block, datuse=input, BPPARAM=BPPARAM)
229      #use islet.lrt.unix
230
231  ✓ test.fun<-function(iTest){
232      cat("csDE testing on cell type",iTest, "\n")
233      if(type == 'intercept'){
234          inputnew <- changeinput(dc=input, iK=iTest)
235      }else{inputnew <- changeinput_slope(dc=input, iK=iTest)}
236
237      tmp1 <- bplapply(X=Yall.list, islet.lrt.block, datuse=inputnew,
238                      lrttest=iTest, BPPARAM=BPPARAM)

```



```
230         KESL=TEST, DFFPARAM=DFFPARAM)
239     tmp2 <- unlist(tmp1)
240     tmp3 <- unlist(lapply(mf, '[', 7))
241     ###obtain the p-values from each cell type
242     tmp4 <- LRT(tmp3, tmp2, df=1)
243     return(tmp4)
244 }
245 test.list<-lapply(seq_len(input@K), FUN=test.fun)
246 test.res<-do.call(cbind,test.list)
247 colnames(test.res) <- colnames(input@X[, seq_len(input@K)])
248 cat("csDE testing on", input@K,"cell types finished", "\n")
249 # }else {
250 ## This will be windows
251 ## Use serial param or do not use any parallel functions, just use 'lapply'
252 ## result should be of the same "type" from both the if and else statements.
253
254 # nworkers<-ncores
255 # cl <- makeCluster(nworkers)
256
257 ## Remove clusterExport(), clusterEvalQ() if use devtools::install() to build package
258 # clusterExport(cl,list('colss'))
259 # clusterEvalQ(cl,{
260 #     library(Matrix)
261 #     library(BiocGenerics)})
262
263 # mf <- parLapply(cl, X=Yall.list, islet.solve.block, datuse = input)
264
265
266 # test.list<-lapply(seq_len(input@K),FUN=test.fun)
267 # test.res<-do.call(cbind,test.list)
268 # colnames(test.res) <- colnames(input@X[, seq_len(input@K)])
269 # cat("csDE testing on", input@K,"cell types finished", "\n")
270 # stopCluster(cl)
271 # }
272 return(test.res)
273 }
```



