

```
22
                                                                        `case` and `ctrl` in the input SummarizedExperiment object.")
                     23
                     24
                     25
                                           #separate cases and controls
                     26
                                                idx <- which(colData(dat se)$group == "case")
                     27
                     28
                                                 case dat se <- SummarizedExperiment(assays=list(counts=assays(dat se)$counts[, idx]),</pre>
                     29
                                                                                                                                       colData=colData(dat se)[idx, -1])
                                                 ctrl_dat_se <- SummarizedExperiment(assays=list(counts=assays(dat_se)$counts[, -idx]),</pre>
                     30
                     31
                                                                                                                                       colData=colData(dat se)[-idx, -1])
                     32
                                                                                                                                                                                                                           Subject_ID
                     33
                     34
                                           #K = number of cell types
                                            K <- ncol(colData(case_dat_se))-1</pre>
                     35
                     36
                     37
                                            #N1 = number of samples for group 1
                     38
                                           N1 <- ncol(assays(case_dat_se)$counts)
                                           #N1 = number of samples for group 2
                     39
                                           N2 <- ncol(assays(ctrl dat se)$counts)
                     40
                                                                                                                                                            Nz: # of ctvl
                                           #NS = total number of Samples for group 1&2
                     41
                                           NS \leftarrow N1 + N2
                     42
                                                                                                                                                                                                                                                                                            (NI+NS)xK
                                                                                                                                                                                          X-sub1: proportion (0.1)
X-sub2: 73 Am N
                                            #NU = total number of Unique subjects for group 1&2
                     43
                                            caseUN <- length(unique(colData(case dat se)[, 1]))</pre>
                     44
                                                                                                                                                                                                                                         // ] ろ M Ni ちする X-Sub 1 本日 B WifNs MK
                                            ctrlUN <- length(unique(colData(ctrl_dat_se)[, 1]))</pre>
                     45
                     46
                                           NU <- caseUN + ctrlUN
                     47
                      48
                     49
                                           X_sub1 <- as.matrix(rbind(colData(case_dat_se)[, -1], colData(ctrl_dat_se)[, -1]))</pre>
                     50
                                           X sub2 <- rbind(matrix(1, nrow=N1, ncol=K), matrix(0, nrow=N2, ncol=K))*X_sub1 >> \frac{1}{2} \frac{1}
                     51
                                      \# X_{sub2} = X_{sub2}[,1:para]
                     52
                                                                                                                                                                                                                                               \mathcal{L}
                     53
                                           X \ 0 \leftarrow cbind(X \ sub1, X \ sub2)
                                                                                                                                                                                                                                                                         \theta_{121} \theta_{122} ... \theta_{12K} z_1\theta_{121} z_1\theta_{122} ... z_1\theta_{12K}
                     54
                                           X_list <- lapply(1, function(x){return(X_0)})</pre>
                                                                                                                            S4 [250 x 12] (Matrix::dgCMa S4 object of class dgCMatrix
                                           X <- bdiag(X_list)</pre>
                                                                                                                                                                                                                                                           X =
                     55
                                                                                                                             integer [2250]
                                                                                                                                                             012345...
                                                                                                                                                                                                                                                                         \theta_{J11} \theta_{J12} ... \theta_{J1K} z_J\theta_{J11} z_J\theta_{J12} ... z_J\theta_{J1K}
                     56
                                                                                                                                                             0 250 500 750 1000 1250 ...
                                                                                                                                                                                                                                                                         \theta_{I21} \theta_{I22} ... \theta_{I2K} z_I\theta_{I21} z_I\theta_{I22} ... z_I\theta_{I2K}
                                                                                                                             integer [2]
                                                                                                                                                             250 12
                                                                                                Dimnames
                                                                                                                            list [2]
                                                                                                                                                             List of length 2
                                                                                                                                                                                                                                                                        \theta_{IT_{1}1} \theta_{IT_{1}2} ... \theta_{IT_{1}K} z_{I}\theta_{IT_{1}1} z_{I}\theta_{IT_{1}2} ... z_{I}\theta_{IT_{1}K}
                                                                                                                             double [2250]
                                                                                                                                                             0.0223 0.0150 0.0131 0.0469 0.0469 0.0718 ...
https://github.com/haoharryfeng/ISLET/blob/main/R/dataprep.R
                                                                                                                            list [0]
                                                                                                                                                             List of length 0
```

N=NS (# of somple)

```
57
                                  #obtain a vector of unique subject IDs, for all, to use later
                                  sub id <- c(colData(case dat se)[, 1], colData(ctrl dat se)[, 1])</pre>
58
59
60
                                  propm <- as.matrix(rbind(colData(case dat se)[, -1], colData(ctrl dat se)[, -1]))</pre>
                             # propd = apply(propm, MARGIN = 2, makea, sub_id = sub_id, X = X, NU = NU, simplify = F)
propd <- apply(X=propm, MARGIN=2, FUN=makea,</pre>
61
                                                                                                                                                                                                                                             A = \begin{pmatrix} \mathbf{a}_{11} & 0 & 0 & 0 & \dots & \mathbf{a}_{1K} & 0 & 0 & 0 \\ 0 & \mathbf{a}_{21} & 0 & 0 & \dots & 0 & \mathbf{a}_{2K} & 0 & 0 \\ 0 & 0 & \ddots & 0 & \dots & 0 & 0 & \ddots & 0 \\ 0 & 0 & 0 & \mathbf{a}_{J1} & \dots & 0 & 0 & 0 & \mathbf{a}_{JK} \end{pmatrix}_{N \times Q}
\mathbf{a}_{jk} := (\theta_{j_1k}, \theta_{j_2k}, \dots, \theta_{iT:L})' \text{ is } \mathbf{a}_{j_2k} := (\theta_{j_1k}, \theta_{j_2k}, \dots, \theta_{iT:L})' \text{ is } \mathbf{a}_{j_2k} := (\theta_{j_1k}, \theta_{j_2k}, \dots, \theta_{iT:L})' \text{ is } \mathbf{a}_{j_2k} := (\theta_{j_1k}, \theta_{j_2k}, \dots, \theta_{iT:L})' \text{ is } \mathbf{a}_{j_2k} := (\theta_{j_1k}, \theta_{j_2k}, \dots, \theta_{iT:L})' \text{ is } \mathbf{a}_{j_2k} := (\theta_{j_1k}, \theta_{j_2k}, \dots, \theta_{iT:L})' \text{ is } \mathbf{a}_{j_2k} := (\theta_{j_1k}, \theta_{j_2k}, \dots, \theta_{iT:L})' \text{ is } \mathbf{a}_{j_2k} := (\theta_{j_1k}, \theta_{j_2k}, \dots, \theta_{iT:L})' \text{ is } \mathbf{a}_{j_2k} := (\theta_{j_1k}, \theta_{j_2k}, \dots, \theta_{iT:L})' \text{ is } \mathbf{a}_{j_2k} := (\theta_{j_1k}, \theta_{j_2k}, \dots, \theta_{iT:L})' \text{ is } \mathbf{a}_{j_2k} := (\theta_{j_1k}, \theta_{j_2k}, \dots, \theta_{iT:L})' \text{ is } \mathbf{a}_{j_2k} := (\theta_{j_1k}, \theta_{j_2k}, \dots, \theta_{iT:L})' \text{ is } \mathbf{a}_{j_2k} := (\theta_{j_1k}, \theta_{j_2k}, \dots, \theta_{iT:L})' \text{ is } \mathbf{a}_{j_2k} := (\theta_{j_1k}, \theta_{j_2k}, \dots, \theta_{iT:L})' \text{ is } \mathbf{a}_{j_2k} := (\theta_{j_1k}, \theta_{j_2k}, \dots, \theta_{iT:L})' \text{ is } \mathbf{a}_{j_2k} := (\theta_{j_1k}, \theta_{j_2k}, \dots, \theta_{iT:L})' \text{ is } \mathbf{a}_{j_2k} := (\theta_{j_1k}, \theta_{j_2k}, \dots, \theta_{iT:L})' \text{ is } \mathbf{a}_{j_2k} := (\theta_{j_1k}, \theta_{j_2k}, \dots, \theta_{iT:L})' \text{ is } \mathbf{a}_{j_2k} := (\theta_{j_1k}, \theta_{j_2k}, \dots, \theta_{iT:L})' \text{ is } \mathbf{a}_{j_2k} := (\theta_{j_1k}, \theta_{j_2k}, \dots, \theta_{j_2k}, \dots, \theta_{j_2k})' \text{ is } \mathbf{a}_{j_2k} := (\theta_{j_1k}, \theta_{j_2k}, \dots, \theta_{j_2k}, \dots, \theta_{j_2k})' \text{ is } \mathbf{a}_{j_2k} := (\theta_{j_1k}, \theta_{j_2k}, \dots, \theta_{j_2k}, \dots, \theta_{j_2k})' \text{ is } \mathbf{a}_{j_2k} := (\theta_{j_1k}, \theta_{j_2k}, \dots, \theta_{j_2k}, \dots, \theta_{j_2k})' \text{ is } \mathbf{a}_{j_2k} := (\theta_{j_1k}, \theta_{j_2k}, \dots, \theta_{j_2k}, \dots, \theta_{j_2k})' \text{ is } \mathbf{a}_{j_2k} := (\theta_{j_1k}, \theta_{j_2k}, \dots, \theta_{j_2k}, \dots, \theta_{j_2k})' \text{ is } \mathbf{a}_{j_2k} := (\theta_{j_1k}, \theta_{j_2k}, \dots, \theta_{j_2k})' \text{ is } \mathbf{a}_{j_2k} := (\theta_{j_1k}, \theta_{j_2k}, \dots, \theta_{j_2k})' \text{ is } \mathbf{a}_{j_2k} := (\theta_{j_1k}, \theta_{j_2k}, \dots, \theta_{j_2k})' \text{ is } \mathbf{a}_{j_2k} := (\theta_{j_1k}, \theta_{j_2k}, \dots, \theta_{j_2k})' \text{ is } \mathbf{a}_{j_2k} := (\theta_{j_1k}, \theta_{j_2k}, \dots, \theta_{j_2k})' \text{ is } \mathbf{a}_{j_2k} := (\theta_{j
62
                                                                                          ind id=sub id, datX=X, aNU=NU, simplify=FALSE)
63
64
                                  A 0 <- do.call(cbind, propd)
65
                                 #A list=lapply(1,function(x){return(A 0)})
66
                                  A<-bdiag(A_0)
67
68
                                  CT<-colnames(propm)</pre>
69
                                                                                                                                                                                                                                   where \mathbf{a}_{jk} := (\theta_{j_1k}, \theta_{j_2k}, \cdots, \theta_{jT_jk})' is simply a reorganized vector of cell type proportions,
70
                                                                                                                                                                                                                                    to align with random effect u.
                                                                                                                                                                                                                                                                                                                                                                                                                                         n E Box1
71
                                  datuse <- inputSet(exp case=assays(case dat se)$counts.</pre>
72
                                                                                       exp ctrl=assays(ctrl dat se)$counts,
                                                                                                                                                                                                                                                                                              ###function to make the design matrix [A] for random effect
                                                                                                                                                                                                                                                                                                                                                                                                                                                         Q=50x6=300
                                                                                                                                                                                                                                                                                             #updated on 05/31/2022 to reflect the change in ID order
73
                                                                                       X=X.
                                                                                                                                                                                                                                                                                            #user should sort their data by subject ID
#makea <- function(onectprop, ind_id=bub_id, datX = X, aNU = NU){</pre>
74
                                                                                       A=A,
                                                                                                                                                                                                                                                                                             makea <- function(onectprop, ind_id, datX , aNU){</pre>
75
                                                                                       K=K.
                                                                                                                                                                                                                                                                                                   lp <- split(onectprop, ind_id)</pre>
                                                                                                                                                                                                                                                                                                  a1 <- matrix(0, nrow=nrow(datX), ncol=aNU)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                       45=250
76
                                                                                                                                                                                                                                                                                             # ct sub=table(sub id)[as.character(unique(sub id))]
77
                                                                                                                                                                                                                                                                                                  lp=lp[names(ct sub)]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                    N(l) = 50
                                                                                                                                                                                                                                                                                                  chk <- unique(ind id) #chk should have the length of NU</pre>
78
                                                                                       case num=caseUN,
                                                                                                                                                                                                                                   List of length 50
                                                                                                                                                                                                                                                                                                  lp<-lp[as.character(chk)]</pre>
                                                                                                                                                                                                                                   0.0223 0.0150 0.0131 0.0469 0.0469
                                                                                                                                                                                                                                                                                                                                                                                                                                                                       T = t
                                                                                                                                                                                                                                   0.0718 0.0114 0.0615 0.0226 0.0405
                                                                                                                                                                                                                                                                                                  count <- rep(0, length(chk))</pre>
79
                                                                                       ctrl num=ctrlUN,
                                                                                                                                                                                                    double [5]
                                                                                                                                                                                                                                   0.0358.0.0897.0.0563.0.0853.0.0145
                                                                                                                                                                                                                                                                                                  for(i in seq_len(aNU)){
                                                                                                                                                                                                                                   0.0546.0.0783.0.0336.0.0524.0.0767
80
                                                                                       CT=CT,
                                                                                                                                                                                                                                   0.0287.0.0194.0.0188.0.0162.0.0137
                                                                                                                                                                                                                                                                                                      tmp <- sum(ind id == chk[i])</pre>
                                                                                                                                                                                                                                   0.0238.0.0582.0.1034.0.0357.0.0165
                                                                                                                                                                                                                                                                                                      count[i] <- tmp</pre>
                                                                                                                                                                                                                                   0.0816.0.0257.0.0811.0.0580.0.0219
81
                                                                                       SubjectID=sub id,
                                                                                                                                                                                                    double [5]
                                                                                                                                                                                                                                   0.04631.0.07325.0.00903.0.02621.0.01249
                                                                                                                                                                                                                                                                                                                                                                                              R=1 (3-4 cell tipe)
                                                                                                                                                                                                                                   0.0764.0.0735.0.0829.0.0587.0.0792
82
                                                                                       type='intercept'
                                                                                                                                                                                                                                   0.0112 0.0715 0.0677 0.0132 0.0262
                                                                                                                                                                                                                                                                                                  for(i in seq_len(aNU)){
83
                                                                                                                                                                                                                                                                                                                                                                                                   ^ V1 (人) ( V2
                                                                                                                                                                                                                                                                                                      s <- 1+sum(count[0:(i-1)])
                                                                                                                                                                                                                                                                                                                                                                                                  1 0.02230079 0.00000000 0.00000000 0.00000000
                                                                                                                                                                                                                                                                                                      e <- sum(count[seq_len(i)])</pre>
                                  message("Complete: data preparation for ISLET.")
84
                                                                                                                                                                                                                                                                                                                                                                                                  2 0.01501410 0.00000000 0.00000000 0.00000000
                                                                                                                                                                                                                                                                                                      a1[s:e, i] <- lp[[i]]
                                   return(datuse)
85
                                                                                                                                                                                                                                                                                                                                                                                                   3 0.01314183 0.00000000 0.00000000 0.00000000
                                                                                                                                                                                                                                                                                                                                                                                                   4 0.04691058 0.00000000 0.00000000 0.00000000
86
                                                                                                                                                                                                                                                                                                                                                                                                   5 0.04692466 0.00000000 0.00000000 0.00000000
                                                             y = X\beta + Au + \varepsilon
                                                                                                                                                                                                                                                                                                                                                                                                   6 0.00000000 0.07183477 0.00000000 0.00000000
                                                                                                                                                                                                                                                                                                                                                                                                   7 0.00000000 0.01136901 0.00000000 0.00000000
                                                  where \varepsilon \sim N(\mathbf{0}, \sigma_0^2 I) are the residuals. Here, X and A are the design matrices for the
                                                                                                                                                                                                                                                                                                                                                                                                   8 0.0000000 0.06145904 0.0000000 0.00000000
                                                  9 0.00000000 0.02264138 0.00000000 0.00000000
                                                                                                                                                                                                                                                                                                                                                                                                10 0.00000000 0.04052955 0.00000000 0.00000000
                                                 \cdots, \beta_K)' has two components: (m_1, m_2, \cdots, m_K) are the baseline average gene expres-
                                                  sion in the control group, and (\beta_1, \beta_2, \dots, \beta_K) are the difference between the case
                                                                                                                                                                                                                                                                                                                                                                                                12 0.00000000 0.00000000 0.08965811 0.00000000
                                                  group and the control group. The random effect \mathbf{u} = (u_{11}, u_{21}, \cdots, u_{I1}, u_{12}, u_{22}, u_{I1}, u_{I2}, u_{I3}, u_{I4}, u_
                                                 \dots, u_{12}, \dots, u_{1K}, u_{2K}, \dots, u_{1K})' captures the individual-level gene expression deviance
                                                                                                                                                                                                                                                                                                                                                                                                14 0.00000000 0.00000000 0.08530417 0.00000000
```

from the group-level mean, for each cell type. The design matrices X and A are in the

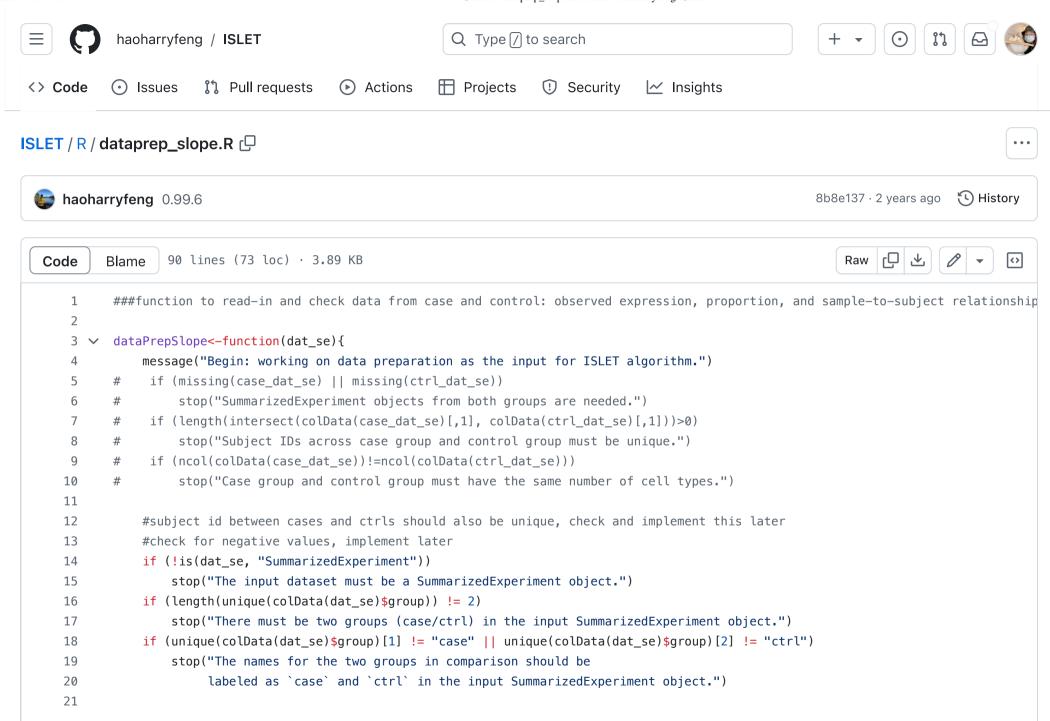
https://github.com/haoharryfeng/ISI

form:

3/3

15 0.00000000 0.00000000 0.01453683 0.00000000

16 0.00000000 0.00000000 0.00000000 0.05460231



```
22
                                           idx <- which(colData(dat se)$group == "case")
23
24
                                           case dat se <- SummarizedExperiment(assays=list(counts=assays(dat se)$counts[, idx]),</pre>
25
                                                                                                                                                                                    colData=colData(dat se)[idx, -1])
                                          ctrl dat se <- SummarizedExperiment(assays=list(counts=assays(dat se)$counts[, -idx]),</pre>
26
27
                                                                                                                                                                                    colData=colData(dat se)[-idx, -1])
28
29
30
31
32
                                          #K = number of cell types
33
                                           K <- ncol(colData(case dat se))-2</pre>
34
35
                                           #N1 = number of samples for group 1
36
                                          N1 <- ncol(assays(case dat se)$counts)
                                           #N1 = number of samples for group 2
37
                                          N2 <- ncol(assays(ctrl_dat_se)$counts)</pre>
38
                                           #NS = total number of Samples for group 1&2
39
                                          NS <- N1 + N2
40
                                           #NU = total number of Unique subjects for group 1&2
41
42
                                           caseUN <- length(unique(colData(case dat se)[, 1]))</pre>
43
                                           ctrlUN <- length(unique(colData(ctrl_dat_se)[, 1]))</pre>
                                          NU <- caseUN + ctrlUN
44
                                           case age<-colData(case dat se)[, 2] ## The first two columns are: subject ID and sample age.
45
                                          ctrl_age<-colData(ctrl_dat_se)[, 2]</pre>
46
47
                                                                                                                                                           与dataprep基本目目. 比处 B=(m, ..., M k, B, ..., Bk,
48
                                          X_sub1 <- as.matrix(rbind(colData(case_dat_se)[, -(seq_len(2))], colData(ctrl_dat_se)[, -(seq_len(2))]))</pre>
49
                                                                                                                                                                                                                                                                                                                                                                                X_sub2 <- rbind(matrix(1, nrow=N1, ncol=K), matrix(0, nrow=N2, ncol=K))*X_sub1</pre>
50
51
                                          X_age <- c(case_age, ctrl_age)</pre>
52
                                          X_sub3 <- X_sub1*X_age
53
                                          X sub4 <- rbind(matrix(1, nrow=N1, ncol=K), matrix(0, nrow=N2, ncol=K))*X sub1*X age
                                          ## This is difference in slope between two groups
54
                                                                                                                                                                                                                                                  X_0 = \left( \frac{\partial u}{\partial x} + \frac{\partial u}{\partial y} + \frac{\partial u
55
                                          X sub4 <- X sub4
                                          X_0 \leftarrow cbind(X_sub1, X_sub2, X_sub3, X_sub4)
56
```

```
BE P 4kx G1
           X list <- lapply(1, function(x){return(X 0)})</pre>
57
58
           X <- bdiag(X list)</pre>
59
           #obtain a vector of unique subject IDs, for all, to use later
60
           sub id <- c(colData(case dat se)[, 1], colData(ctrl dat se)[, 1])</pre>
61
62
           propm <- as.matrix(rbind(colData(case_dat_se)[, -(seq_len(2))], colData(ctrl_dat_se)[, -(seq_len(2))]))</pre>
63
           # propd = apply(propm, MARGIN = 2, makea, sub_id = sub_id, X = X, NU = NU, simplify = F)
64
           propd <- apply(X=propm, MARGIN=2, FUN=makea,</pre>
65
                          ind id=sub id, datX=X, aNU=NU, simplify=FALSE)
66
67
           A_0 <- do.call(cbind, propd)
68
           #A_list=lapply(1,function(x){return(A_0)})
69
           A<-bdiag(A 0)
70
71
           CT<-colnames(propm)</pre>
72
73
           datuse <- inputSet(exp_case=assays(case_dat_se)$counts,</pre>
74
75
                          exp_ctrl=assays(ctrl_dat_se)$counts,
76
                          X=X
77
                          A=A,
                         K=K,
78
79
                          NS=NS,
80
                          NU=NU,
81
                          case_num=caseUN,
82
                          ctrl_num=ctrlUN,
83
                          CT=CT,
                          SubjectID=sub_id,
84
                          type='slope'
85
86
           message("Complete: data preparation for ISLET.")
87
88
           return(datuse)
       }
89
```