

VII: Buoyancy and Buoyant Force

1: Buoyancy

- The phenomenon that keeps a body swim or suspended is known as Buoyancy.
- The force a fluid exerts on a body immersed is known as Buoyant Force(F_B)

2: Buoyant Force

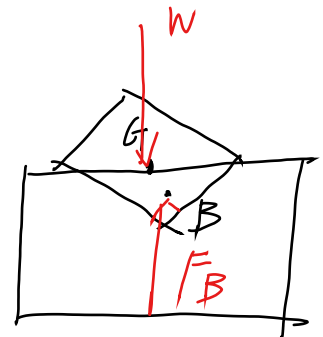
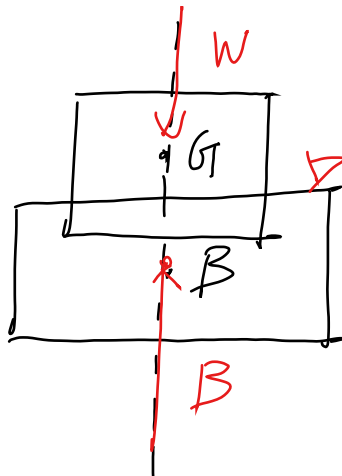
- According to the 2nd law of hydrostatic: Pressure in a fluid at rest is constant over any surface normal to the field of a body force.
- The resultant horizontal force has been canceled out, so the buoyant force acts in the vertical direction.
- The resultant force is the buoyant force acts vertically upward and is equal to the weight of the displaced fluid.
- Archimedes'law:

$$F_B = \rho V g$$

- This formula can be induced by calculating the resultant force of the both sides of a submerged project.

3: Floating body

- For a floating body, its weight is equal to the buoyant force.
- $W = m_{floatingbody} g$
- $F_B = m_{displacedliquid} g$
- $W = F_B$
- i.e. $m_{floatingbody} = m_{displacedfluid}$



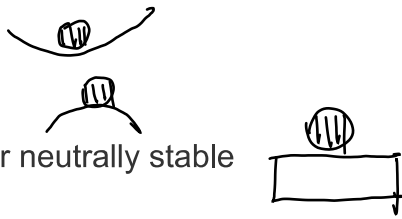
VIII: Stability

1: Stability

- The buoyant force acts through the centroid of the displaced fluid volume.
- The point B is called the centre of the buoyancy.

- For equilibrium body, there is no moments.
- If the F and W are not in the same line, there will be a rotational moment.
- According to the action of the moment, the types of the equilibrium can be distinguished into 3 parts:

- Stable
- Unstable
- Neutral or neutrally stable

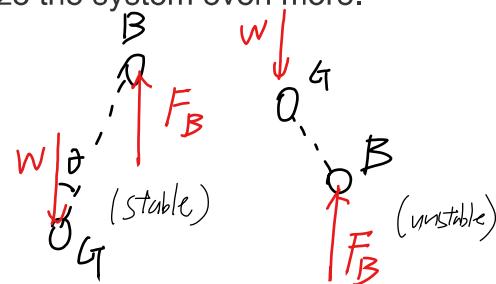


2: Submerged Bodies

- For wholly immersed body, the condition for stable equilibrium is that G is under the B.
- If the weight and buoyant force isn't in the same line, then they produce rotational momentum.
 - If G is below B, the momentum tends to restore stability.
 - If B is below G then the resultant momentum tends to destabilize the system even more.
 - If the G and B coincide then neutral stability is obtained.

3: Stability of the submerged bodies

- When B is above the G, the body is in the equilibrium of the stable.
 - The stable equilibrium case has a righting couple, namely $W \times BG \times \sin \theta$ (anticlockwise), which tries to restore the tilt (clockwise).
- When B is below G, the body is in unstable equilibrium.
 - The case of unstable equilibrium the couple (anticlockwise) tends to increase the angle of tilt (anticlockwise).
- If the B and G are coincident then body is in neutral equilibrium.



4: Floating Bodies

- It is not necessary that G is under the B.
- The body undergoes an angular displacement will change the immersed volume so that change the buoyancy (B).
- The new centre of B is B' and the new buoyant force is $F_{B'}$.
- We define the metacenter as the point where a vertical through the new centre of buoyancy intersects the continuation of the line BG.
- The distance between the metacenter (M) and centroid (G) is called the metacenter height.
- If the V is the volume of displaced liquid and \overline{MB} is the distance of MB, I is the second order moment of area of the water line:

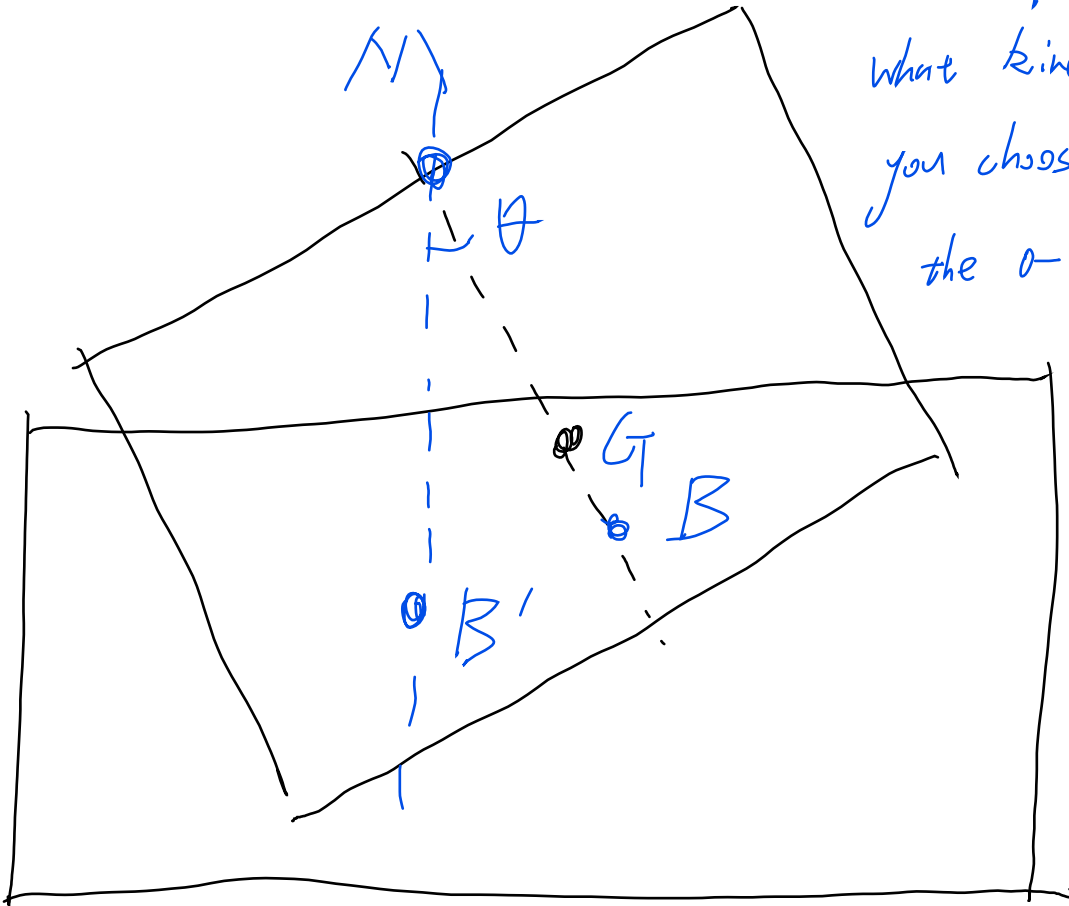
$$\overline{MB} = \frac{I}{V}$$

$$\overline{MG} = \overline{MB} \pm \overline{GB} = \frac{I}{V} \overline{GB}$$

- Minus if G is above B and Plus if G is below B.

~~X~~ ∴

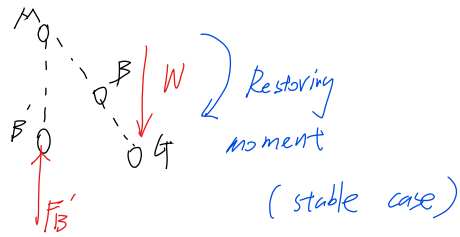
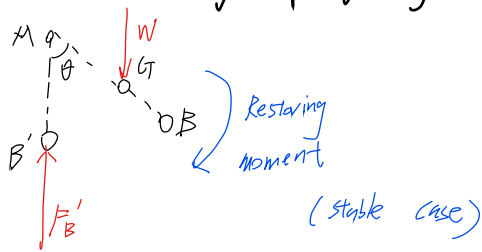
I depends on
what kind of axis
you choose, normally
the o-o, sometimes
x-x or y-y.



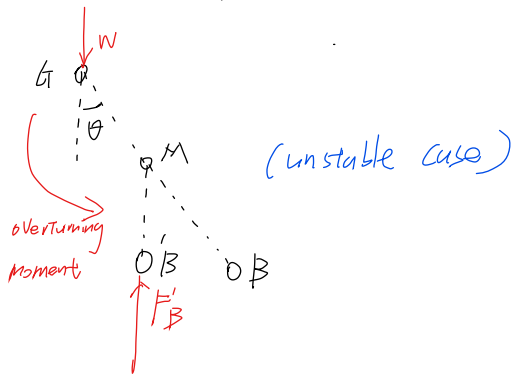
$$\overline{MG} = \frac{I}{V} + \overline{GB} \quad (G \text{ is below } B)$$

$$\overline{MG} = \frac{I}{V} - \overline{GB} \quad (G \text{ is above } B)$$

• The stability of floating bodies



- For stability of floating bodies, the metacentric height has to be positive (M has to be above the G)



- The restoring moment

$$= W \cdot \overline{MG} \cdot \sin \theta$$

if it is minus, it'll become the overturning moment