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$$16. (1). \cos A = \frac{b^2 + c^2 - a^2}{2bc} = \frac{\sqrt{5}}{2}$$

$$\frac{1}{2}c^2 = b^2 - a^2$$

$$c^2 = a^2 + b^2 - 2ab \cos C$$

$$\sin B - \sin^2 A = \pm \sin^2 C$$

$$\sin^2 A \cos^2 C + \pm \sin^2 A \cdot \pm \sin^2 C + \pm \sin^2 C \cdot \pm \sin^2 A + \sin^2 C \cos^2 A$$

$$-\sin^2 A = \pm \sin^2 C$$

$$\frac{1}{2} \cos^2 C + \frac{1}{2} \sin^2 C + \frac{1}{2} \cos^2 C - \frac{1}{2} = \pm \sin^2 C$$

$$\cos^2 C + \sin^2 C + \sin^2 C - 1 = \sin^2 C$$

$$\cos^2 C + 1 - 2\sin^2 C + \sin^2 C - 1 = \sin^2 C$$

$$\cos^2 C = 2\sin^2 C$$

$$\therefore \frac{\sin^2 C}{\cos^2 C} = \frac{1}{2} \quad \therefore \tan^2 C = \frac{1}{2} \quad \therefore \tan C = \frac{\sqrt{2}}{2}$$

$$12) \sin C = \frac{\sqrt{6}}{3} \quad \cos C = \frac{\sqrt{3}}{3}$$

$$\sin B = \sin(A+C) = \sin A \cos C + \cos A \sin C$$

$$= \frac{\sqrt{2}}{2} \cdot \frac{\sqrt{3}}{3} + \frac{\sqrt{3}}{2} \cdot \frac{\sqrt{6}}{3} = \frac{2\sqrt{6} + 3\sqrt{6}}{6}$$

$$S_{\triangle ABC} = \frac{1}{2} bc \sin A = 3$$

$$bc = 6\sqrt{2}$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$\therefore b = 2\sqrt{2}$$

AI Response:

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$\cos A = \frac{b^2 + c^2 - a^2}{2bc} = \frac{\sqrt{5}}{2}$

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℄ Š> \(\ \cos A \) ∈ ∝ \(\ \frac{\sqrt{5}}{2} \) \) , i ≠ ∝ \(\ \cos A \) ∈' | \([-1, 1]\) § ¨ ©ª « ¬ – Š>

2. **®⁻ ° ±²³ **^

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$\sin^2 A \cos^2 C + \frac{1}{2} \sin 2A \cdot \frac{1}{2} \sin 2C + \frac{1}{2} \sin 2C \cdot \frac{1}{2} \sin 2A + \sin^2 C \cos^2 A$

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3. **ÃÄÅÄ**^

- ÃÄÆ• \(\ \tan C = \frac{\sqrt{5}}{2} \) Ç, È ½É μ i Š> Ê Ëª « Ì Í

%Î Š< Œ16.Œ2••

1. **®⁻ Ĩ Đ ∈ Š> **^

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- Š> \(\ \sin B \) Ñ – " Ÿ Ò Ó Ô Õ ¼ Š> Ä Ö Á i

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$\sin B = \sin (A + C) = \sin A \cos C + \cos A \sin C$

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©ª « Š> \(\ \sin B \) ∈

2. **®⁻ × μ Ô Š> **^

- Š> μ Ô \(\ \Delta ABC \) , ~ ™ \(\ bc = 6\sqrt{2} \) ∈ Ê Ëª « Ì Í

3. **Ø Ù Š> **^

- Å ´ Š> \(\ b \) ∈ Ñ Ê Ëª « ¬ – Š>

ÚÄ

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