Exploiting POI-Specific Geographical Influence
for Point-of-Interest Recommendation

Hao Wang[1,2]**, Huawei Shen**[1,2]**, Wentao Ouyang**[1]**, Xueqi Cheng**[1,2]
[1]Institute of Computing Technology, Chinese Academy of Sciences, Beijing, China
[2]University of Chinese Academy of Sciences, Beijing, China
wanghao@software.ict.ac.cn, {shenhuawei,ouyangwt,cxq}@ict.ac.cn

Abstract

Point-of-Interest (POI) recommendation, i.e., recommending unvisited POIs for users, is a fundamental problem for location-based social networks. POI recommendation distinguishes itself from traditional item recommendation, e.g., movie recommendation, via geographical influence among POIs. Existing methods model the geographical influence between two POIs as the probability or propensity that the two POIs are co-visited by the same user given their physical distance. These methods assume that geographical influence between POIs is determined by their physical distance, failing to capture the *asymmetry* of geographical influence and the high *variation* of geographical influence across POIs. In this paper, we exploit *POI-specific* geographical influence to improve POI recommendation. We model the geographical influence between two POIs using three factors: the geo-influence of POI, the geo-susceptibility of POI, and their physical distance. Geo-influence captures POI's capacity at exerting geographical influence to other POIs, and geo-susceptibility reflects POI's propensity of being geographically influenced by other POIs. Experimental results on two real-world datasets demonstrate that POI-specific geographical influence significantly improves the performance of POI recommendation.

1 Introduction

Location-based social networks (LBSNs), such as Foursquare and Gowalla, are increasingly popular, bridging the gap between the physical world and online social networking services [Xiao *et al.*, 2010; Sun *et al.*, 2017]. In LBSNs, users share their locations and content associated with location information, facilitating the understanding of users' preference and behavior [Bao *et al.*, 2012; Liu and Xiong, 2013; Gao *et al.*, 2015; Wang *et al.*, 2015a]. Point-of-Interest (POI) recommendation, i.e., recommending for users unvisited POIs (e.g., restaurants, shopping malls, and theaters) according to users' check-in records, gains great research interest in the last few years [Li *et al.*, 2016; He *et al.*, 2016; Zhang *et al.*, 2016; Li *et al.*, 2017].

One of the most prominent features for POI recommendation is that locations of POIs and target user are critical factors for recommendation. For example, in Gowalla and Foursquare, 90% of users' consecutive check-ins are within the distance less than 50km [Liu *et al.*, 2017]. Therefore, besides modeling users' preference from the interaction between users and POIs, as done in traditional item recommendation, researchers devote to exploiting the geographical proximity or geographical influence among POIs to improve the performance of POI recommendation [Ye *et al.*, 2011; Lian *et al.*, 2014; Xie *et al.*, 2016].

Existing methods that exploit geographical influence for POI recommendation roughly falls into two paradigms. The first kind of methods leverages the geographical proximity to improve the learning of users' preference, assuming that POIs in close proximity to each other share similar user preferences [Liu *et al.*, 2014; Li *et al.*, 2015; Xie *et al.*, 2016; Feng *et al.*, 2017]. For these methods, geographical proximity is used as a kind of spatial regularization for users' preferences. The second kind of methods explicitly models the geographical influence among POIs as the probability or propensity that the two POIs are co-visited by the same user given their physical distance [Ye *et al.*, 2011; Cheng *et al.*, 2012; Zhang and Chow, 2013; Lian *et al.*, 2014; Saleem *et al.*, 2017]. Various forms of functions, e.g., power law function and Gaussian distribution, are employed to capture the co-visited probability distribution of POIs with respect to their physical distance. Although the aforementioned methods gain some success at leveraging geographical influence, they are incapable to capture the high variation of geographical influence across POIs. For example, as shown in Figure 1, 10 randomly-selected POIs in Foursquare dataset exhibit quite different geographical influence, indicating that geographical influence cannot be well captured solely by physical distance and thus geographical influence should be *POI-specific*.

In this paper, we exploit POI-specific geographical influence to improve POI recommendation. We model the POI-specific geographical influence between two POIs using three factors: the geo-influence of POI, the geo-susceptibility of POI, and their physical distance. Geo-influence captures POI's capacity to spread its visitors to other POIs, and geo-
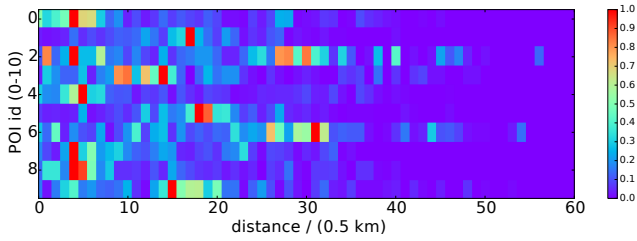
Figure 1: Heat map of the check-in correlation over distance of 10 randomly sampled POIs on the Foursquare dataset. Take 0.5 km as one bin, and for each bin, we count the average correlation between each selected POI and POIs falling into the bin. We normalize these values by the largest one.

susceptibility reflects POI's propensity of receiving visitors from other POIs. For example, subway stations generally have high geo-influence and restaurants usually have high geo-susceptibility. Here, geo-influence and geo-susceptibility are two low-dimensional vectors, and the geographical influence between two POIs is represented by the inner product of the geo-influence vector of one POI and the geo-susceptibility vector of the other POI.

Our model for POI-specific geographical influence has two unique benefits: (1) Geographical influence between POIs is asymmetric, offering high flexibility to capture the high variability of geographical influence across POIs. (2) Instead of directly modeling the POI-specific geographical influence using a POI interaction matrix, our model represent geographical influence by two low-dimensional vectors for each POI, significantly reducing the number of free parameters [Wang *et al.*, 2015b]. Thus, our model is appropriate for POI recommendation which suffers from severe data sparsity issue.

Finally, we integrate POI-specific geographical influence into a standard model that captures users' preference, forming a new POI recommendation method. We train our model using users' check-in records and validate the recommendation performance by applying the model to "predict" the POIs that they are likely to visit in the near future. We conduct extensive experiments on two real-world datasets from Foursquare and Gowalla to illustrate the effectiveness of our model. Experimental results demonstrate that POI-specific geographical influence significantly improves the performance of POI recommendation, outperforming state-of-the-art POI recommendation methods.

2 Related Work

In this section, we give a brief review about POI recommendation. POI recommendation recommends for users unvisited POIs according to users' check-in records. Considering users' check-ins are implicit feedback, existing methods model check-ins either by fitting scores converted from check-in counts [Lian *et al.*, 2014] or by optimizing a pairwise ranking of users' preferences to POIs [Li *et al.*, 2015; 2016; Zhao *et al.*, 2017].

Due to the sparsity of users' check-ins, only exploiting check-in counts often suffer from poor performance. Auxiliary information can be incorporated to alleviate this situation. For example, geographical influence is one of the most important factors and it does not exist on the online

recommendation sense. Existing methods of modeling geographical influence can be grouped into two categories, i.e., global methods [Ye *et al.*, 2011; Cheng *et al.*, 2012; Zhang and Chow, 2013; Lian *et al.*, 2014] and regional methods [Liu *et al.*, 2014; Li *et al.*, 2015; Xie *et al.*, 2016; Feng *et al.*, 2017].

Global methods model the relation between POIs' cooccurence and their geographical coordinates. Ye et al. [2011] and Lian et al. [2014] respectively use a power-law distribution and a Gaussian distribution to characterize geographical influence over distance. [Cheng *et al.*, 2012; Zhang and Chow, 2013] capture the scatter plot of each user's check-ins (e.g., the longitude and latitude) by a fixed distribution. Regional methods consider that POIs in a same geographical region share similar attraction to users. [Xie *et al.*, 2016; Feng *et al.*, 2017; Zhao *et al.*, 2017] use representation-based learning method and restrict POIs in the same region share similar representations. [Liu *et al.*, 2014; Li *et al.*, 2015] directly calculate the attraction of a target POI by considering the attraction of its geographical neighbors. However, global methods and regional methods provide two coarse grained representations of geographical influence, which ignore the POI-specific attributes. We address the problem in this paper.

In addition, many studies have explored other information to facilitate POI recommendation performance, such as social relationship [Tang *et al.*, 2013], temporal factors [Yuan *et al.*, 2013] and category [Zhang and Chow, 2015], etc.

3 Preliminary

We denote with U and I the set of users and the set of POIs respectively. For a user u and a POI i, we denote with c_{ui} as the number of times that user u visited POI i, and w_{ui} is a scaled version of c_{ui}. All POIs that user u visited form his/her check-in history, denoted as H_u. For each POI i, its location is denoted as longitude lon_i and latitude lat_i. We use d_{ij} to represent the physical distance between POI i and POI j. For each user u, its preference is denoted as a vector $\vec{t}_u$. For each POI i, we denote with $\vec{z}_i$ its preference vector, and denote with $\vec{g}_i$ and $\vec{h}_i$ its geo-influence vector and geo-susceptibility vector. We summarize the notations in Table 1.

POI recommendation: Given a set of users U with check-in history H and a set of POIs I with location information (lon, lat), POI recommendation recommends for each target user $u \in U$ a list of POIs $\{i|i \in I\}$ consisting of POIs that the target user is potentially interested in but didn't visit up to the recommendation.

4 Model and Optimization

In this section, we describe the proposed model for POI recommendation. The proposed model consists of two parts, one for POI-specific geographical influence and the other for the modeling of user/item preference. The major novelty of the proposed model lies in the POI-specific geographical influence. For user/item preference, we model each check-in as a process of selecting one target POI from all candidate POIs, avoiding the bias caused by directly modeling the number of visiting frequency as a numeric quantity. Next, we describe

Variable	Description
U, I	Set of users, POIs
lon_i, lat_i	Longitude and latitude of POI i
d_{ij}	Physical distance between POI i and j
c_{ui}	Number of times that user u visited POI i
w_{ui}	A scaled version of c_{ui}
H_u	User u's check-in history ($\{i|c_{ui} > 0\}$)
$\vec{t}_u$	Preference vector of user u
$\vec{z}_i$	Preference vector of POI i
$\vec{g}_i$	Geo-influence vector of POI i
$\vec{h}_i$	Geo-susceptibility vector of POI i

Table 1: Notations in this paper.

Name	Form	Pre-learning
Power-law function	$f(x) = a * x^b$	Yes
Power-law function	$f(x) = a * x^b$	No
Exponential function	$f(x) = a * x^b * e^{cx}$	No
Hyperbolic function	$f(x) = \frac{a}{x-b}$	No

Table 2: Four types of geographical influence function.

the POI-specific geographical influence and the modeling of user preference.

4.1 POI-Specific Geographical Influence

For a target POI j, we consider the geographical influence from each POI i in the check-in history H_u of user u. As illustrated in Figure 1, users prefer to visit neighboring POIs, and meanwhile different POIs have their own characteristics that are not well explained by physical distance. To capture the high variation of geographical influence across POIs, we model the geographical influence y_{ij} from POI i to POI j as

$$y_{ij} = \vec{g}_i^T \vec{h}_j \times f(d_{ij}). \qquad (1)$$

Here, the vector $\vec{g}_i$ captures the *geo-influence* of POI i, i.e., a POI's capacity to spread its visitors to other POIs; the vector $\vec{h}_j$ reflects the *geo-susceptibility* of POI j, i.e., a POI's propensity of receiving visitors from other POIs; d_{ij} is the physical distance between POI i and POI j.

The rationales behind Eq. (1) are as follows:

- First, $f(d_{ij})$ reflects the probability that two POIs are visited by the same user given their physical distance d_{ij}. In this paper, we consider four types of functions, shown in Table 2. In general, $f(d_{ij})$ decreases with the increase of d_{ij}, capturing the phenomenon that a user prefers to visit geographically neighboring POIs. Moreover, the parameters of $f(d_{ij})$ could be pre-trained before training the POI recommendation model, or are trained together with the training of the POI recommendation model.

- We model the interaction between a visited POI i and a target POI j as $\vec{g}_i^T \vec{h}_j$. In this way, geographical influence between POIs is asymmetric, offering the flexibility

to capture the high variation of geographical influence across POIs. Moreover, instead of directly modeling the POI-specific geographical influence using a POI interaction matrix, our model represents geographical influence by two low-dimensional vectors for each POI, significantly reducing the number of free parameters. Thus, our model is appropriate for POI recommendation which suffers from severe data sparsity issue.

- The POI-specific geographical influence y_{ij} essentially captures the joint effect from both the physical distance and the intrinsic characteristics of two POIs. For a target POI j, a geographically neighboring and influencing POI would result in a high y, while a distant but influencing POI (or a neighboring but less influencing POI) would result in a relatively smaller y. The influence score y also depends on the intrinsic characteristics $\vec{h}$ of the target POI as well. This makes y different for different target POIs, given the same visited POI i. In other words, the influence score in our model is POI-specific in terms of the POIs involved.

Given the set H_u of visited POIs of user u and Eq. (1), we consider the impact from all these visited POIs and model the overall geographical influence of H_u on a target POI j as

$$\frac{1}{|H_u|} \sum_{i \in H_u} y_{ij} = \frac{1}{|H_u|} \sum_{i \in H_u} \vec{g}_i^T \vec{h}_j \times f(d_{ij}). \qquad (2)$$

4.2 Preference Modeling and Recommendation

To infer a user's preference to a target POI, we consider the impact from both user preference and geographical influence. Specifically, we denote user u's preference to POI j as s_{uj}, which is given as

$$s_{uj} = \vec{t}_u^T \vec{z}_j + \frac{1}{|H_u|} \sum_{i \in H_u} \vec{g}_i^T \vec{h}_j \times f(d_{ij}), \qquad (3)$$

where $\vec{t}_u$ and $\vec{z}_j$ are used to model the interaction between user u's preference and POI j's preference, following the practice of matrix factorization method.

Note that users' check-ins records their visit frequencies at POIs, which is a kind of implicit user preference. Thus, different from traditional recommendation that directly fit c_{uj}, we model each check-in as a process of selecting one target POI from all candidate POIs. In this way, our model avoids the bias caused by directly modeling the number of visiting frequency as a numeric quantity. Specifically, the probability p_{uj} that user u prefers POI j is modeled as

$$p_{uj} = \frac{\exp(s_{uj})}{\sum_{k \in I} \exp(s_{uk})}, \qquad (4)$$

where I is the set of POIs and the denominator is a normalization over all POIs for a given user u.

It is observed from Eq. (4) that for a given user u, $\{p_{uj}\}$ serves as a set of parameters for a multinomial distribution. Accordingly, the behavior that user u visits POI j is modeled as the outcome of a decision-making process, where the user picks one POI j out of all the candidates. Check-ins can be

then conveniently interpreted as samples drawn from a user's preference distribution $\{p_{uj}\}$.

We maximizes the log-likelihood of observing users' check-ins:

$$L = \sum_{u \in U} \sum_{j \in I} c_{uj} \log p_{uj} = \sum_{u \in U} \sum_{j \in I} c_{uj}$$

$$\log \left(\frac{\exp(\vec{t}_u^T \vec{z}_j + \frac{1}{|H_u|} \sum_{i \in H_u} f(d_{ij}) \times \vec{g}_i^T \vec{h}_j)}{\sum_{k \in I} \exp(\vec{t}_u^T \vec{z}_k + \frac{1}{|H_u|} \sum_{i \in H_u} f(d_{ik}) \times \vec{g}_i^T \vec{h}_k)} \right). \tag{5}$$

Since the check-in count c_{uj} often shows a very skewed distribution, the interactions with a few popular POIs may dominate the log likelihood. We thus replace c_{uj} by a scaled version w_{uj} to alleviate the problem. Specifically, we adopt a log-form function [Lian *et al.*, 2014], which is given by $w_{uj} = 1 + \log(1 + c_{uj} \times 10^\epsilon)$, where ϵ is a scaling parameter. For unvisited POIs, we simply set $w_{uj} = 0$.

Finally, given a user u, we recommend unvisited POIs according to the probability p_{uj} that the user visits a POI j. Each user's recommendation list is composed of the top n POIs with the highest probability p_{uj} among the unvisited POIs.

4.3 Optimization

We now present the optimization of four types of latent factors, including $\vec{t}_u$, $\vec{z}_j$, $\vec{g}_i$, $\vec{h}_j$ and parameters in the geographical function.

We adopt the approach of negative sampling proposed in [Mikolov *et al.*, 2013] to maximize the log likelihood L. For each visited POI, we sample K negative check-ins according to some noisy distribution. Specifically, we use the following objective function to substitute L

$$\mathscr{L} = \sum_{u \in U} \sum_{j \in I} w_{uj} \sum_{l \in \{j\} \cup NEG(j)p}$$
$$\left\{ \delta_{lj} \log[\sigma(s_{ul})] + (1 - \delta_{lj}) \log[1 - \sigma(s_{ul})] \right\}, \tag{6}$$

where $NEG(j)$ represents the set of negative POIs relative to POI j. δ_{lj} is an indicator which equals to 1 if $l = j$ and 0 otherwise, and $\sigma(\cdot)$ is the sigmoid function.

We adopt the stochastic gradient ascent (SGA) algorithm to optimize the new objective function. In each iteration, we randomly sample a mini-batch of the pair set by a ratio ζ to optimize. The sampling probability is proportional to the scaled check-in count, i.e., w_{uj}. If the pair (u, j) is sampled, the latent vectors will be updated as follows:

$$\vec{t}_u = \vec{t}_u + \eta w_{uj} \sum_{l \in \{j\} \cup NEG(j)} [\delta_{lj} - \sigma(s_{ul})]\vec{z}_l, \tag{7}$$

$$\vec{z}_l = \vec{z}_l + \eta w_{uj}[M_{ij} - \sigma(s_{ul})]\vec{t}_u, \tag{8}$$

$$\vec{g}_i = \vec{g}_i + \eta w_{uj} \sum_{l \in \{j\} \cup NEG(j)} [\delta_{lj} - \sigma(s_{ul})]\frac{1}{|H_u|}f(d_{ij})\vec{h}_j \tag{9}$$

$$\vec{h}_l = \vec{h}_l + \eta w_{uj}[\delta_{lj} - \sigma(s_{ul})]\frac{1}{|H_u|}\sum_{i \in H_u} f(d_{il})\vec{g}_i, \tag{10}$$

where $i \in H_u$, $l \in j \cup NEG(j)$, and η is the learning rate.

5 Experiment

5.1 Datasets

We use two real-world datasets from Foursquare [Cho *et al.*, 2011] and Gowalla [Yuan *et al.*, 2013] for evaluation. We pre-process check-ins in Foursquare by removing users who have visited fewer than 10 POIs, and POIs which are visited by fewer than 10 users. In Gowalla the threshold for elimination is set as 40. After preprocessing, there are 172,961 check-ins generated by 6,118 users over 88,193 POIs in the Foursquare dataset and 115,890 check-ins generated by 1,624 users over 3,585 POIs in the Gowalla dataset. Each POI in both datasets is associated with its longitude and latitude. Additionally, in the Foursquare dataset, each POI is marked by 8 categories and 240 subcategories. For each user u, we sort his/her check-ins chronologically, and take the early 70% of her check-ins as training data, the next 15% as validation data, and the last 15% as testing data.

5.2 Evaluation Metrics

We adopt two widely-used metrics for evaluation [Lian *et al.*, 2014; Liu *et al.*, 2017], namely, $precision@n$ and $recall@n$, where n is the number of POIs in the recommendation list.

$$precision@n = \frac{1}{|U|} \sum_{u=1}^{|U|} \frac{|P_u^n \cap T_u|}{|P_u^n|}, \tag{11}$$

$$recall@n = \frac{1}{|U|} \sum_{u=1}^{|U|} \frac{|P_u^n \cap T_u|}{|T_u|}, \tag{12}$$

where P_u^n is the set of top n POIs in user u's recommendation list, and T_u is user u's ground truth set of POIs. $|x|$ denotes the cardinality of set x. For each metric, we consider 7 values (i.e., 1, 2, 3, 5, 10, 15, 20) of n in our experiments.

5.3 Methods in Comparison

For convenience, we use *GeoIE* as the name of the proposed POI recommendation method. We evaluate the performance of GeoIE by comparing it with the following representative POI recommendation methods:

- UCF+G [Ye *et al.*, 2011]: It uses a power-law function to capture check-in probability with distance, and then combines a user-based collaborative filtering method.

- MGM+PFM [Cheng *et al.*, 2012]: It uses a multi-center Gaussian model to capture a user's check-in distribution and then combines a probabilistic factor model.

- GeoMF [Lian *et al.*, 2014]: It extends MF by augmenting original users' and POIs' latent factors with users' activity regions and POIs' influence areas.

- RankGeoFM [Li *et al.*, 2015]: It is a ranking-based MF model which includes the geographical influence by considering the attraction of neighboring POIs. According to the recent review for POI recommendation [Liu *et al.*, 2017], RankGeoFM is one of the top-performing methods and serves as one of the state-of-the-art POI recommendation methods.

- Geo-Teaser [Zhao *et al.*, 2017]: It combines a temporal POI embedding model and a geographically hierarchical pairwise ranking method.
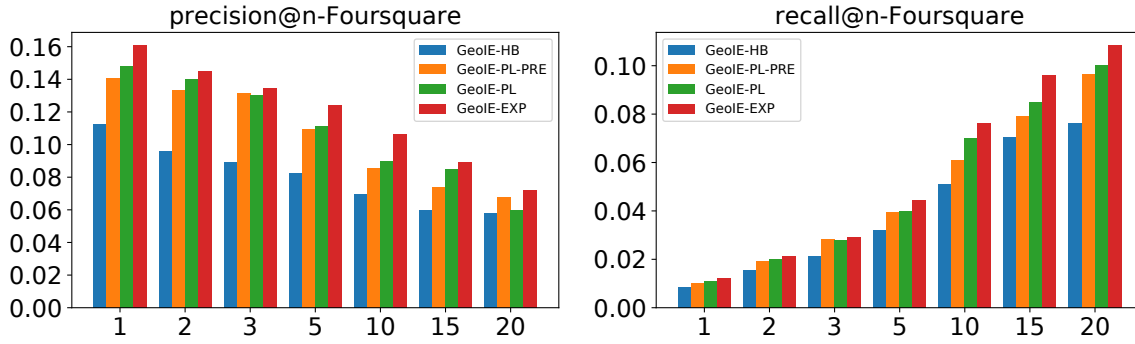
Figure 2: Performance of GeoIE in four types of geographical functions on the Foursquare dataset.
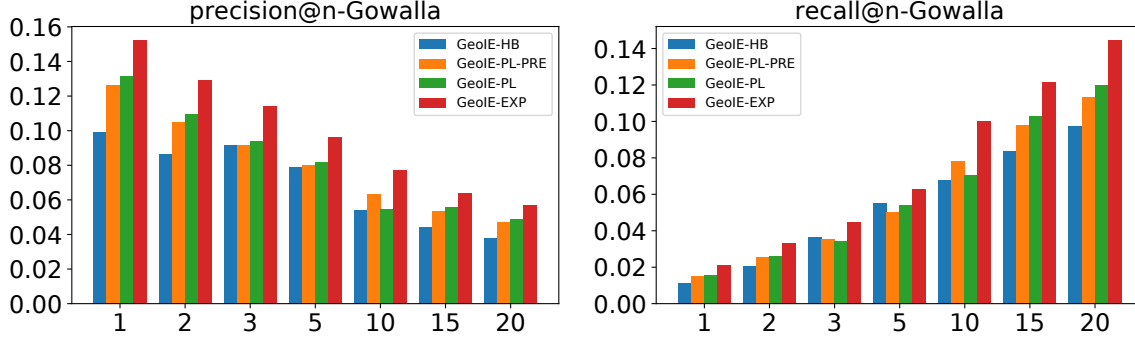

Figure 3: Performance of GeoIE in four types of geographical functions on the Gowalla dataset.

5.4 Experimental Setting

We set the scaling parameter ϵ as 10. We place a L_2 regularization term for each latent vector when performing optimization, and the regularization coefficient is set as 0.02. The number of dimension of latent vectors is 32. The number of negative samples K is 10, the sampling ratio ζ as 0.2 and learning rate as 0.001 in each iteration.

Before comparing our method with baselines, we first evaluate the performance of our method with four different geographical functions, as described in Table 2. The corresponding GeoIE are named as *GeoIE-PL-PRE*, *GeoIE-PL*, *GeoIE-EXP*, and *GeoIE-HB*. Figure 2 and Figure 3 show the performance of four variants of GeoIE on the Foursquare dataset and the Gowalla dataset respectively. It can be observed in both two figures that exponential function achieves the best performance, which implies that exponential function is the best choice for depicting the relationship between geographical influence and distance on both two datasets used in this paper. The superiority of the exponential function is attributed to that the exponential funciton has more parameters, and thus is flexible to capture the high variation of geographical influence. By comparing GeoIE-PL-PRE and GeoIE-PL, we find that they achieve similar performance. However, what needs to be pointed out is that optimizing parameters of geographical function with other latent factors in our model would lead to a faster convergence rate.

5.5 Effectiveness of GeoIE

We select GeoIE-EXP as the representative of our method and compare it with state-of-the-art methods. Performance comparison on Foursquare dataset and Gowalla dataset are respectively illustrated in Figure 4 and Figure 5. It is ob-

served that GeoIE-EXP consistently outperforms the competing baseline methods.

Figure 4 shows MGM+PFM performs better than UCF+G on Foursquare. On Gowalla, however, UCF+G outperforms MGM+PFM except when $k = 1$, as shown in Figure 5. They assume different geographical functions and achieve good performance on two datasets respectively. Different from UCF+G and MGM+PFM which fuse two separate models by linear interpolation, GeoMF integrates user preference and geographical influence into one unified model. Latent factors can be mutually influenced in its parameter learning process, leading to a better performance. However, GeoMF factorizes users' zero check-ins, besides non-zeros check-ins. This may weaken its performance to a certain extent.

RankGeoMF considers geographical influence of neighboring POIs, and utilizes a ranking-based method to explore negative samples. It outperforms GeoMF on both datasets. However, neighboring POIs' attraction cannot be directly taken as target POI's capacity of attracting users. Geo-Teaser integrates representation learning-based method and a geographically hierarchical pairwise ranking method by linear interpolation. We can observe that it is slightly better than RankGeoMF.

In sum, experimental results clearly demonstrate that POI-specific geographical influence improves POI recommendation. The superiority of POI-specific geographical influence over other methods that exploits geographical method offers us two key implications: (1) Geographical influence for POI recommendation is too noisy to be amenable to quantification using a simple function, e.g., power law function or exponential function; (2) The introduction of two additional vectors to characterize POI-specific geographical influence could
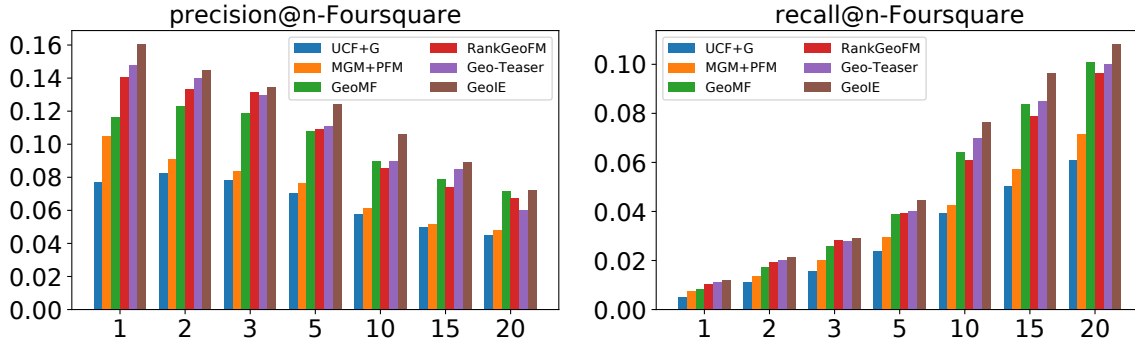
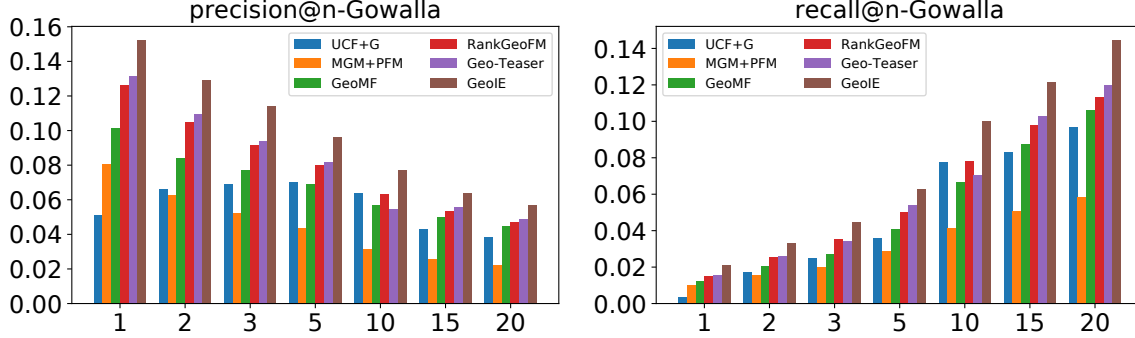Figure 4: Performance of our method and state-of-the-arts methods on the Foursquare dataset.

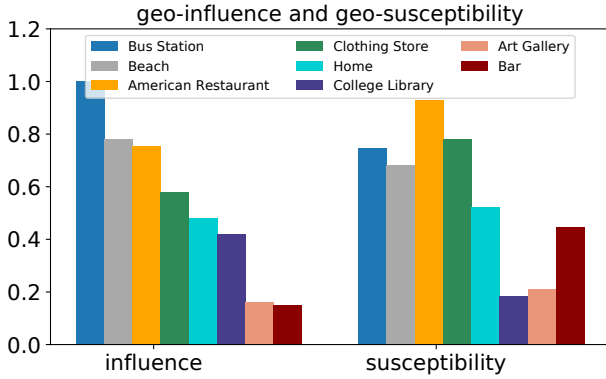Figure 5: Performance of our method and state-of-the-arts methods on the Gowalla dataset.

Figure 6: Geo-influence and geo-susceptibility of POIs with different categories on the Foursquare dataset.

gain remarkable improvement, although POI recommendation suffers from data sparsity issue.

5.6 POI's Geo-Influence and Geo-Susceptibility

To capture POI-specific geographical influence, we introduce two latent vectors, i.e., the geo-influence and the geo-susceptibility for each POI. In what follows, we study the attribute strength of different categories of POIs. Due to the limited space, we just select one subcategory from each category for case study. Specifically, we calculate the average norm of the two types of latent vectors for each subcategory, and divide these norm by the largest one to scale them between 0 to 1. We present these norms in Figure 6.

It can be observed that the Bus station has the largest geo-influence, suggesting its powerful ability to spread users to other POIs. However, the geo-susceptibility of this influencial subcategory is not the largest. Meanwhile, both of the two attributes of the Bar and the Art Gallery are in a low position, which indicates that they are not important places in users' travel choices. These observations implies each POI has specific geo-influence and the geo-susceptibility, which are also asymmetric. This also verifies our assumption that it's necessary to model POI-specific geographical influence.

6 Conclusions

In this paper, we exploit POI-specific geographical influence to improve POI recommendation. We model the geographical influence between two POIs using three factors: the geo-influence of POI, the geo-susceptibility of POI, and their physical distance. Geo-influence captures POI's capacity at exerting geographical influence to other POIs, and geo-susceptibility reflects POI's propensity of being geographically influenced by other POIs. Our model naturally capture the asymmetric geographical influence between POIs, offering high flexibility to capture the high variation of geographical influence across POIs. As future work, it is promising to directly learn a manifold for geographical influence from the interaction between POIs.

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