

# COMP2432 Operating Systems

## Written Assignment 2

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### 1. Page Replacement

#### 3 memory frames

(a) **FIFO**: total page fault: 19

	0	1	2	3	4	5	2	4	3	2	5	4	2	5	6	1	3	2	1	0	2	4	3	2	1
F1	0	0	0	3	3	3	2	2	2	2	2	2	2	5	5	5	3	3	3	3	3	4	4	4	1
F2		1	1	1	4	4	4	4	3	3	3	3	3	3	6	6	6	2	2	2	2	2	3	3	3
F3			2	2	2	5	5	5	5	5	5	4	4	4	4	1	1	1	1	0	0	0	0	2	2

(b) **optimal**: total page fault: 14

	0	1	2	3	4	5	2	4	3	2	5	4	2	5	6	1	3	2	1	0	2	4	3	2	1
F1	0	0	0	3	3	5	5	5	5	5	5	5	5	5	6	1	1	1	1	0	0	4	4	4	1
F2		1	1	1	4	4	4	4	3	3	3	4	4	4	4	4	3	3	3	3	3	3	3	3	3
F3			2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2

(c) **LRU**: total page fault: 18

	0	1	2	3	4	5	2	4	3	2	5	4	2	5	6	1	3	2	1	0	2	4	3	2	1
F1	0	0	0	3	3	3	2	2	2	2	2	2	2	2	2	1	1	1	1	1	1	4	4	4	1
F2		1	1	1	4	4	4	4	4	4	5	5	5	5	5	5	3	3	3	0	0	0	3	3	3
F3			2	2	2	5	5	5	3	3	3	4	4	4	6	6	6	6	2	2	2	2	2	2	2

#### 4 memory frames

(a) **FIFO**: total page fault: 13

	0	1	2	3	4	5	2	4	3	2	5	4	2	5	6	1	3	2	1	0	2	4	3	2	1
F1	0	0	0	0	4	4	4	4	4	4	4	4	4	4	4	4	3	3	3	3	3	3	3	3	1
F2		1	1	1	1	5	5	5	5	5	5	5	5	5	5	5	5	2	2	2	2	2	2	2	2
F3			2	2	2	2	2	2	2	2	2	2	2	2	6	6	6	6	6	0	0	0	0	0	0
F4				3	3	3	3	3	3	3	3	3	3	3	3	1	1	1	1	1	1	4	4	4	4

(b) **optimal**: total page fault: 10

	0	1	2	3	4	5	2	4	3	2	5	4	2	5	6	1	3	2	1	0	2	4	3	2	1
F1	0	0	0	0	4	4	4	4	4	4	4	4	4	4	4	4	4	4	4	4	4	4	4	4	1
F2		1	1	1	1	5	5	5	5	5	5	5	5	5	6	1	1	1	1	0	0	0	0	0	0
F3			2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2
F4				3	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3

(c) **LRU**: total page fault: 14

	0	1	2	3	4	5	2	4	3	2	5	4	2	5	6	1	3	2	1	0	2	4	3	2	1
F1	0	0	0	0	4	4	4	4	4	4	4	4	4	4	4	1	1	1	1	1	1	1	3	3	3
F2		1	1	1	1	5	5	5	5	5	5	5	5	5	5	5	5	2	2	2	2	2	2	2	2
F3			2	2	2	2	2	2	2	2	2	2	2	2	2	2	3	3	3	3	3	4	4	4	4
F4				3	3	3	3	3	3	3	3	3	3	3	6	6	6	6	6	0	0	0	0	0	1

(d)

0 1 2 3 4 5 2 4 3 2 5 4 2 5 6 1 3 2 1 0 2 4 3 2 1

FIFO: 0 1 **3** 2 3 4 5 2 4 3 2 5 4 2 5 6 1 3 2 1 0 2 4 3 2 1

LRU: 0 1 2 3 **2** 4 5 2 4 3 2 5 4 2 5 6 1 3 2 1 0 2 4 3 2 1

(e)

FIFO and LRU: 0 1 2 3 4 5 2 4 3 2 5 4 2 5 6 1 3 2 **4** 0 2 4 3 2 1

## 2. Alternative Rage Replacement

### KBS (3 memory frame)

**P=10:** page fault = 18

	2	3	4	5	2	4	3	2	5	4	2	5	6	1	3	2	1	0	2	4	3	2	1
F1	0	3	3	3	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2
F2	1	1	4	4	4	4	3	3	3	3	3	5	5	5	5	5	5	5	5	5	5	5	1
F3	2	2	2	5	5	5	5	5	5	4	4	4	6	1	3	3	1	0	0	4	3	3	3

**P=5:** page fault = 16

	2	3	4	5	2	4	3	2	5	4	2	5	6	1	3	2	1	0	2	4	3	2	1
F1	0	3	4	5	5	5	5	5	5	5	5	5	5	5	5	5	5	0	0	4	3	3	3
F2	1	1	1	1	1	4	4	4	4	4	4	4	4	4	3	2	2	2	2	2	2	2	2
F3	2	2	2	2	2	2	3	2	3	2	2	2	6	1	1	1	1	1	1	1	1	1	1

### KBS (4 memory frame)

**P=10:** page fault =13

	3	4	5	2	4	3	2	5	4	2	5	6	1	3	2	1	0	2	4	3	2	1
F1	0	4	4	4	4	4	4	4	4	4	4	4	4	4	4	4	4	4	4	3	3	3
F2	1	1	5	5	5	5	5	5	5	5	5	5	5	5	5	5	5	5	5	5	5	1
F3	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2
F4	3	3	3	3	3	3	3	3	3	3	3	6	1	3	3	1	0	0	0	0	0	0

**P=5:** page fault = 13

	3	4	5	2	4	3	2	5	4	2	5	6	1	3	2	1	0	2	4	3	2	1
F1	0	4	4	4	4	4	4	4	4	4	4	4	4	4	4	4	4	4	4	3	3	3
F2	1	1	5	5	5	5	5	5	5	5	5	5	5	5	5	5	5	5	5	5	5	1
F3	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2
F4	3	3	3	3	3	3	3	3	3	3	3	6	1	3	3	1	0	0	0	0	0	0

Compared to the LRU algorithm, KBS algorithm will has less page fault rate in this case.

### 3. Deadlock Avoidance

(a)

	Allocation				Need			
	A	B	C	D	A	B	C	D
P <sub>0</sub>	1	0	1	2	1	2	1	0
P <sub>1</sub>	2	1	0	1	1	0	1	0
P <sub>2</sub>	1	2	0	1	1	2	3	1
P <sub>3</sub>	2	1	1	0	1	1	0	2
P <sub>4</sub>	1	1	1	2	1	2	1	1
P <sub>5</sub>	2	0	2	2	1	1	0	0

A possible safe sequence:

$$1\ 1\ 1\ 0 \xrightarrow{P_1: 2\ 1\ 0\ 1} 3\ 2\ 1\ 1 \xrightarrow{P_5: 2\ 0\ 2\ 2} 5\ 2\ 3\ 3 \xrightarrow{P_0: 1\ 0\ 1\ 2} 6\ 2\ 4\ 5 \xrightarrow{P_2: 1\ 2\ 0\ 1} 7\ 4\ 4\ 6 \xrightarrow{P_3: 2\ 1\ 1\ 0} 9\ 5\ 5\ 6$$

$$\xrightarrow{P_4: 1\ 1\ 1\ 2} 10\ 6\ 6\ 8$$

Available: 1 1 1 0

	Work	Allocation	Need	W + A						
P <sub>1</sub>	1 1 1 0	2 1 0 1	1 0 1 0	3 2 1 1						
P <sub>0</sub>	3 2 1 1	1 0 1 2	1 2 1 0	4 2 2 3						
					Choice 1	P <sub>3</sub>	4 2 2 3	2 1 1 0	1 1 0 2	<b>6 3 3 3</b>
					Choice 2	P <sub>4</sub>	4 2 2 3	1 1 1 2	1 2 1 1	<b>5 3 3 5</b>
					Choice 3	P <sub>5</sub>	4 2 2 3	2 0 2 2	1 1 0 0	<b>6 2 4 5</b>

6 3 3 3 is bigger than request of left 3 processes.

P<sub>1</sub>-P<sub>0</sub>-P<sub>3</sub>-(P<sub>2</sub>, P<sub>4</sub>, P<sub>5</sub>)                      3P<sub>3</sub>

5 3 3 5 is bigger than request of left 3 processes.

P<sub>1</sub>-P<sub>0</sub>-P<sub>4</sub>-(P<sub>2</sub>, P<sub>3</sub>, P<sub>5</sub>)                      3P<sub>3</sub>

6 2 4 5 is bigger than request of left 3 processes.

P<sub>1</sub>-P<sub>0</sub>-P<sub>5</sub>-(P<sub>2</sub>, P<sub>3</sub>, P<sub>4</sub>)                      3P<sub>3</sub>

	Work	Allocation	Need	W + A						
P <sub>1</sub>	1 1 1 0	2 1 0 1	1 0 1 0	3 2 1 1						
P <sub>4</sub>	3 2 1 1	1 1 1 2	1 2 1 1	4 3 2 3						
					Choice 1	P <sub>0</sub>	4 3 2 3	1 0 1 2	1 2 1 0	<b>5 3 3 5</b>
					Choice 2	P <sub>3</sub>	4 3 2 3	2 1 1 0	1 1 0 2	<b>6 4 3 3</b>
					Choice 3	P <sub>5</sub>	4 3 2 3	2 0 2 2	1 1 0 0	<b>6 3 4 5</b>

5 3 3 5 is bigger than request of left 3 processes.

P<sub>1</sub>-P<sub>4</sub>-P<sub>0</sub>-(P<sub>2</sub>, P<sub>3</sub>, P<sub>5</sub>)                      3P<sub>3</sub>

6 4 3 3 is bigger than request of left 3 processes.

P<sub>1</sub>-P<sub>4</sub>-P<sub>3</sub>-(P<sub>0</sub>, P<sub>2</sub>, P<sub>5</sub>)                      3P<sub>3</sub>

6 3 4 5 is bigger than request of left 3 processes.

P<sub>1</sub>-P<sub>4</sub>-P<sub>5</sub>-(P<sub>0</sub>, P<sub>2</sub>, P<sub>3</sub>)                      3P<sub>3</sub>

	Work	Allocation	Need	W + A
P <sub>1</sub>	1 1 1 0	2 1 0 1	1 0 1 0	3 2 1 1
P <sub>5</sub>	3 2 1 1	2 0 2 2	1 1 0 0	<b>5 2 3 3</b>

5 2 3 3 is bigger than request of left 4 processes.

P<sub>1</sub>-P<sub>5</sub>-(P<sub>0</sub>, P<sub>2</sub>, P<sub>3</sub>, P<sub>4</sub>)                      4P<sub>4</sub>

	Work	Allocation	Need	W + A
P <sub>5</sub>	1 1 1 0	2 0 2 2	1 1 0 0	3 1 3 2
P <sub>1</sub>	3 1 3 2	2 1 0 1	1 0 1 0	<b>5 2 3 3</b>

5 2 3 3 is bigger than request of left 4 processes.

P<sub>5</sub>-P<sub>1</sub>-(P<sub>0</sub>, P<sub>2</sub>, P<sub>3</sub>, P<sub>4</sub>)          4P<sub>4</sub>

	Work	Allocation	Need	W + A
P <sub>5</sub>	1 1 1 0	2 0 2 2	1 1 0 0	3 1 3 2
P <sub>3</sub>	3 1 3 2	2 1 1 0	1 1 0 2	<b>5 2 4 2</b>

5 2 4 2 is bigger than request of left 4 processes.

P<sub>5</sub>-P<sub>3</sub>-(P<sub>0</sub>, P<sub>1</sub>, P<sub>2</sub>, P<sub>4</sub>)          4P<sub>4</sub>

Possible safe sequences: 3P<sub>3</sub> × 6 + 4P<sub>4</sub> × 3 = 108

(b)

P<sub>x</sub> is under reporting but also safe, so which will not affect the process sequence. According to the description, P<sub>x</sub> is not P<sub>1</sub>, so must be P<sub>5</sub> (because of the first process must be P<sub>1</sub> or P<sub>5</sub>), when change A, still be safe. Then P<sub>x</sub> is P<sub>5</sub>

(c)

Y<sub>1</sub> will be affected the safe sequence of these processes without Y<sub>2</sub>, P<sub>5</sub> is safe for (b), if B is changed, it will be unsafe.

Then P<sub>y</sub> is P<sub>5</sub>, and Y<sub>1</sub> is B.

#### 4. Deadlock Detection

(a)

	Allocation				Request			
	A	B	C	D	A	B	C	D
P <sub>0</sub>	1	0	1	1	0	1	1	2
P <sub>1</sub>	2	0	0	1	1	1	1	1
P <sub>2</sub>	1	1	0	0	1	0	1	0
P <sub>3</sub>	2	0	1	1	1	2	1	2
P <sub>4</sub>	1	1	1	1	0	1	1	0
P <sub>5</sub>	2	2	2	1	1	0	1	2

Available: 1 0 1 0

	Work	Allocation	Need	Work + Allocation
P <sub>2</sub>	1 0 1 0	1 1 0 0	1 0 1 0	2 1 1 0
P <sub>4</sub>	2 1 1 0	1 1 1 1	0 1 1 0	3 3 3 1
P <sub>1</sub>	3 3 3 1	2 0 0 1	1 1 1 1	<b>5 3 3 2</b>

5 3 3 2 is bigger than request of all the left processes.

P<sub>2</sub>-P<sub>4</sub>-P<sub>1</sub>-(P<sub>0</sub>, P<sub>3</sub>, P<sub>5</sub>)          3P<sub>3</sub>

All possible safe sequence:

$P_2-P_4-P_1-P_0-P_3-P_5$

$P_2-P_4-P_1-P_0-P_5-P_3$

$P_2-P_4-P_1-P_3-P_0-P_5$

$P_2-P_4-P_1-P_3-P_5-P_0$

$P_2-P_4-P_1-P_5-P_0-P_3$

$P_2-P_4-P_1-P_5-P_3-P_0$

Possible safe sequences:  $3! = 6$

(b)

If  $P_2$  increase 2, then  $P_2$  will be unsafe (because of the first process must be  $P_2$ ), so  $P_x = P_2$ .

(c)

If  $Y_2$  is D, then it will be deadlock. For  $P_2, P_4, P_1$ , if D increases, first three process can be changed, so that the result would not be safe. Then  $P_y$  is  $P_2, P_4$  or  $P_1$ .