

KARL-FRANZENS-UNIVERSITÄT GRAZ

MASTER THESIS

Numerical Study of astrophysical solutions in modified theory of gravity in the Palatini formalism

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Abstract

$$\begin{aligned}
\Psi &= e^{i \vec{k} \cdot \vec{r}} u(\vec{r}) \\
T_{\vec{R}} f(\vec{r}) &= f(\vec{r} + \vec{R}) \\
H|\Psi\rangle &= E|\Psi\rangle \\
T_{\vec{R}}[H(\vec{r})\Psi(\vec{r})] &= H(\vec{r} + \vec{R})\Psi(\vec{r} + \vec{R}) \\
H(\vec{r} + \vec{R}) &= H(\vec{r}) \\
&= H(\vec{r})T_{\vec{R}}\Psi(\vec{r}) = ET_{\vec{R}}\Psi(\vec{r}) \\
[H, T] &= 0 \\
T_{\vec{R}}\Psi(\vec{r}) &= \Psi(\vec{r} + \vec{R}) \stackrel{!}{=} c(\vec{R})\Psi(\vec{r}) \\
\text{Vom endlichen ins unendliche: } &\sum_{k=1}^{k=N} (1) = N \\
\sum_k &\longrightarrow c \int_{-\pi/a}^{\pi/a} dk = \frac{2\pi}{a} c \stackrel{!}{=} N \\
\Rightarrow c &= \frac{Na}{2\pi} = \frac{L}{2\pi} \\
\Rightarrow \sum_k &\longrightarrow \frac{L}{2\pi} \int_{-\pi/a}^{\pi/a} dk \\
\Rightarrow \sum_k &\longrightarrow \frac{V}{(2\pi)^3} \int_{-\pi/a}^{\pi/a} d^3k
\end{aligned}$$

1 Ising Model

References

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