

EXAM 1

Culombs Law, conductors, insulators, polarization, induced charges, adding vector fields and forces

$$\vec{F}_{1on2} = \vec{F}_{12} = -\vec{F}_{21} = q_2 \vec{E}_1 = k \frac{q_1 q_2}{r_{12}^2} \hat{r}_{12} = k \frac{q_1 q_2}{r_{12}^2} \hat{r}_{12}; \quad \vec{F}_{tot} = q_0 \vec{E}_{tot}; \quad \vec{E}_{tot}(X_0, y_0, z_0) = \int d\vec{E}(x', y', z') = \int k \frac{dq'(x', y', z')}{r_0^2} \frac{\vec{r}_0}{r_0}, \quad \vec{r}_0 = \vec{r}_0 - \vec{r}' = (x_0 - x')\hat{i} + \dots, \quad \vec{r}' = x'\hat{i} + \dots$$

 distance away from line charge linearly, line starts at 0, at $x=-D$, $\vec{E} = -k \int_0^L \frac{\lambda dx'}{(D+x')^2} \hat{i}$, $V = k\lambda \ln(\frac{D+L}{D})$

 with θ up from x axis, $r_x = x \cos \theta$, $r_y = y \sin \theta$, $r = \sqrt{r_x^2 + r_y^2}$, $k = 9 * 10^9 = \frac{1}{4\pi\epsilon_0}$, $\epsilon_0 = 8.85 * 10^{-12}$

Electric field for point charges, electric field for a continuous distribution of charge

$$\vec{F}_E = q\vec{E}; \quad \vec{E}_s = k \frac{q_s}{r^2} \frac{\vec{r}}{r} = k \frac{q_s}{r^2} \hat{r}$$

Gauss's law and electric flux through a surface, Use of Gauss's law to find field

$$\Phi_E = \oint \vec{E} \cdot d\vec{A} = \int E \cdot dA \cos \phi = \frac{Q_{encl}}{\epsilon_0}, \quad \phi = \angle \vec{E} - d\vec{A}, \quad d\vec{A} = dA \hat{n} \quad \text{net elec field } \vec{E} = 0, \quad V = c \quad \text{within a cond.}$$

 gauss sphere: $\Phi_E = \oint \vec{E}(r) \cdot d\vec{A} = E(r)4\pi r^2$, $E(r) = k \frac{q}{r^2}$,

 sphere radius R: outside or point charge: $V = k \frac{q}{r}$, $E = k \frac{q}{r^2}$ inside: cond: $V = k \frac{q}{R}$, $E = 0$, insulating: $E = k \frac{qr}{R^3}$

 long thin wire: $E(r) = \lambda/(2\pi r \epsilon_0)$ thin flat sheet: $E = \sigma/(2\epsilon_0)$, stepped: go from in to out matching net $Q_i n$ infinite plane w/ cylinder in it, $E = \sigma/\epsilon_0$

Electric potential for point charge, distribution. Electric field vs potential, equipotential. Potential for group of points, conservation of energy.

$$\text{Change Elec Pot Enrgy } \Delta U = - \int_{\vec{r}_A}^{\vec{r}_B} q\vec{E} \cdot d\vec{s} = -W_{AB}; \quad \text{Change Elec Pot } \Delta V = \frac{\Delta U_E}{q} = - \int_{\vec{r}_A}^{\vec{r}_B} \vec{E} \cdot d\vec{s} \quad \text{so } \Delta U_E = q\Delta V$$

 Point charge, Σ for system $V(r) = \frac{kq}{r}$, $U_E = k \frac{q_1 q_2}{R_{12}} + \dots$; Field from pot: $E_x = -\Delta V = -\frac{\delta V}{\delta x} - \dots$

work on closed path = 0;

Caps, Dielectrics, steady state, equiv, energy storage, electric field energy density

$$C = Q/V = \frac{\epsilon_0 A}{d} = kC_0, \quad \text{ElcPotEnrInCap } U_E = .5QV = .5Q^2/C = .5CV^2, \quad \text{EnrFieldDen } u_E = .5\epsilon_0 E^2, \quad E = \frac{\sigma}{k\epsilon_0}, \quad V_1 = V \frac{C_{equiv}}{C_1}$$

 Current and density J, Resistance and itivity, Power relations and dissipation, DC steady state, KCVL Ohms $I = \frac{dQ}{dt}$, $I = \vec{J}d\vec{A}$, $\vec{J} = qn\vec{v}_d = I/A$. $E = \rho J$, $V = IR$, $R = \rho L/A$, $P = IV = I^2 R = V^2/R$; $V_{bat} = \text{EMF} - Ir$

 Temp: conductor: $\rho(T) = \rho_0 + \rho_0 \alpha(T - T_0)$ semi: $\rho(T) = \rho_0 e^{(\frac{E_a}{kT})}$, $E_a = \text{actiEngr}$, $k = 1.38e - 23 = \text{bolt const.}$

Magnetic forces and fields

$$\vec{F} = q\vec{v} \times \vec{B}, \quad \text{finger velocity, curl field, thumb force, flip for negative. } \vec{F}_B = I\vec{L} \times \vec{B}, \quad r = \frac{mv}{|q|B}$$

misc

$$W = q\Delta V, \quad \text{Centripital force } F = mv^2/r, \quad E = -\Delta V/d, \quad V = kq/r, \quad V = \Delta KE = -\Delta PE, \quad KE = 0.5 * mv^2$$

 $F = ma$, earth south is north, use conventional, $\vec{c} = \vec{a} \times \vec{b}$, $|\vec{c}| = |\vec{a}||\vec{b}| \sin \theta_{ab}$, cross is det, dot is sum

$$\text{RMS} = \sqrt{\sum(x^2)}, \quad \%error = (\text{act-exp})/\text{exp}$$

EXAM 2 Sources of magnetic fields, law of Biot-Savart for moving charges and current elements, Magnetic fields of current carrying wires and loops, Magnetic forces between conductors

 field from point charge moving $\vec{B} = \frac{\mu_0}{4\pi} \frac{q\vec{v} \times \vec{r}}{r^3} = \frac{\mu_0}{4\pi} \frac{q\vec{v} \times \hat{r}}{r^2}$, $B = \frac{\mu_0}{4\pi} \frac{qv \sin \theta}{r^2}$, velocity, radius to measurement, from current element Biot-Savart swap $q\vec{v} > \int I d\vec{l}$, right hand, thumb conventional current/positive charge. axis of loop: $B_x = \frac{\mu_0 I a^2}{2(x^2 + a^2)^{3/2}} = \frac{\mu_0 \mu}{2\pi(s^2 + a^2)^{3/2}}$, $\mu = IA$, $x = \text{far} - i$, $B = \frac{\mu}{x^3}$

$$\text{Current same direction, fields oppose, attract. } F = L \frac{\mu_0 I_1 I_2}{2\pi r}$$

$$\text{Straight wire: } B = \frac{\mu_0 I}{2\pi r}, \quad \text{Center of a loop: } B = \frac{\mu_0 I}{2r}, \quad \text{inside: } \frac{\mu_0 I}{2\pi R^2} r$$

$$\text{Solenoid: inductance: } L = \frac{\Phi_B}{i} = \frac{N\Phi_{B,loop}}{i} = \frac{NB A_{loop}}{i} = \frac{N\mu_0 n i A_{loop}}{i} = \mu_0 N \frac{N}{l} A_{loop} = \frac{\mu_0 N^2 \pi r_s^2}{l} = \pi \mu_0 n^2 r_s^2 l$$

 inside a Solenoid: $B = \mu_0 n I$, voltage $\int_a^b \vec{E}_{nc} \cdot d\vec{l} = -\frac{d\Phi_B}{dt} = -L \frac{di}{dt}$, i from + to - increase, EMF

Ampere's law, calculating magnetic fields from ampere's law. Magnetic moments and magnetism, magnetic force and torque on a current loop/magnetic moment

 Ampere's law: $\oint \vec{B} \cdot d\vec{l} = \mu_0 I_{enc}$ total field in a circular path around a wire is equal to μ_0 times current enclosed current density \vec{J} , $I_{enc} = \int \vec{J}_{net} \cdot d\vec{A} = J \cdot A \cos \theta$

 Magnetic moment: $\vec{\mu} = I\vec{A}$, current in loop times area of loop, right hand direction. Torque $\tau_{B,net} = \vec{\mu} \times \vec{B}$, right hand rule for spin direction

Magnetic flux, Faraday's law, Lenz's law, Electromagnetic Induction.

$$\text{Magnetic flux } \Phi_B = \int \vec{V} \cdot d\vec{A} = \int B dA \cos \theta, \quad \text{Faraday's law: EMF from changing Mflux } \epsilon = \oint \vec{E} \cdot d\vec{l} = -\frac{d}{dt} \Phi_B,$$

for N loops, $\cdot N$. Lenz's law, this EMF induces opposing (attracting) magnetic field. B increase up, EMF and i cw, induced B down, net small B up

Displacement current, Maxwell's equations: "displacement current" is built up charge, $I_d = \epsilon_0 \frac{d}{dt} \Phi_E$, fixed Ampere's $\oint \vec{B} \cdot d\vec{l} = \mu_0(I_c + I_d)_{enc} = \mu_0 I_{c,enc} + \mu_0 \epsilon_0 \frac{d}{dt} \Phi_{E,enc}$
 Maxwell's: Gauss's for \vec{E} : $\oint \vec{E} \cdot d\vec{A} = \frac{q_{enc}}{\epsilon_0}$ for \vec{B} : $\oint \vec{B} \cdot d\vec{A} = 0$
 Faraday stationary: $\oint \vec{E} \cdot d\vec{l} = -\frac{d}{dt} \Phi_B$, Ampere stationary: $\oint \vec{B} \cdot d\vec{l} = \mu_0(i_c + \epsilon_0 \frac{d}{dt} \Phi_E)_{enc}$

Self and mutual Inductance, EMF and current in circuits, Magnetic field energy and energy density
 self inductance: $\Phi_B = Li$, $L = \frac{\Phi_B}{i}$, Mutual: $M = M_{12} = \frac{N_1 \Phi_{B1}}{i_2} = M_{21} = \frac{N_2 \Phi_{B2}}{i_1}$, $\frac{d\Phi_B}{dt} = \frac{d}{dt} Li = L \frac{di}{dt}$,
 $\epsilon_L = -L \frac{di}{dt}$, $\epsilon_1 = -M \frac{di_2}{dt}$

magnetic energy in an inductor $U_B = 0.5 Li^2$, region in field \vec{B} has energy density $u_B = \frac{U_B}{v} = \frac{B^2}{2\mu_0}$

Circuit Transients, RC, RL, LC, and RLC. Characteristic decay times and oscillation frequencies

$I(C) = C \frac{dV_C}{dt}$, $V(L) = L \frac{dI}{dt}$

RC: charge $q(t) = C\epsilon(1 - e^{-t/RC})$, $i = \frac{dq}{dt}$, $i(t) = \frac{\epsilon}{R} e^{-t/RC}$ discharge: $q(t) = Q_0 e^{-t/RC}$, $i(t) = -\frac{Q_0}{RC} e^{-t/RC}$

RL: charge $i(t) = \frac{\epsilon}{R}(1 - e^{-tR/L})$, discharge $i(t) = i_0 e^{-tR/L}$

LC: Q(C) $q(t) = Q \cos(\omega t + \phi)$, I(L) $i(t) = \frac{dq}{dt} = -\omega Q \sin(\omega t + \phi)$, $\omega = 1/\sqrt{LC}$ $T = \frac{2\pi}{\omega}$, $\omega = 2\pi * \nu$,
 $U_E = \frac{(q(t))^2}{2C}$, $U_B = 0.5 L(i(t))^2$, $U_{tot} = U_E + U_B = \frac{Q^2}{2C}$, $L \frac{di}{dt} = -\frac{q}{C}$, $\frac{d^2 q}{dt^2} = -\frac{1}{LC} q$

Alternating current circuits, phasors, reactance, impedance, resonance, power, transformers

AC: $RMS = \frac{1}{\sqrt{2}} max$, $X_L = \omega L$, V_L is 90 ahead, $X_C = \frac{1}{\omega C}$, V_C is 90 behind

$i(t) = I \cos(\omega t)$, L: $V_L(t) = \omega L I \cos(\omega t + \pi/2) = V_L \cos(\omega t + \pi/2)$

series LRC AC: $V = \sqrt{V_R^2 + (V_L - V_C)^2} = I \sqrt{R^2 + (X_L - X_C)^2}$, *net* impedance $Z = \sqrt{R^2 + (X_L - X_C)^2}$

current phasor is shared, V_R matches, V_L leads 90, V_C lags 90, $V_S = V_R + V_L + V_C$, some phase inbetween
 ϕ , $\tan \phi = \frac{V_L - V_C}{V_R} = \frac{X_L - X_C}{R}$, resonance: at ω_0 , $X_L = X_C$, $Z = R$,

$q(t) = Q e^{-t/\tau_d} \cos(\omega' t + \phi)$, $\tau_d = 2L/R$, $\omega' = \sqrt{\frac{1}{LC} - (\frac{R}{2L})^2}$

Power: $P_{average} = 0.5 V_{amp} I_{amp} \cos \phi_{V-I} = V_{RMS} I_{RMS} \cos \phi_{V-I}$, $\cos \phi = R/Z$ for series LRC

Transformer: $\frac{V_2}{V_1} = \frac{N_2}{N_1}$

EXAM 3

EM basics: $\frac{\delta B_z}{\delta x} = -\epsilon_0 \mu_0 \frac{\delta E_y}{\delta t}$, $\frac{\delta B_z}{\delta t} = -\frac{\delta E_y}{\delta x}$, $\epsilon_0 \mu_0 \frac{\delta^2 E_y}{\delta t^2} = \frac{\delta^2 E_y}{\delta x^2}$, $\epsilon_0 \mu_0 \frac{\delta^2 B_z}{\delta t^2} = \frac{\delta^2 B_z}{\delta x^2}$, $E_m = c B_m$

Poynting vector $\vec{S} = \frac{1}{\mu_0} \vec{E} \times \vec{B}$, Intensity $I = c \frac{1}{2} \epsilon_0 E_m^2 = c \frac{1}{2\mu_0} B_m^2 = P/A = P/(4\pi r^2)$

result wave of form $E_{tot} = E_m \cos(-\omega t + \frac{\Delta\phi}{2})$, interference result magnitude $E_m = 2E_0 \cos(\frac{\Delta\phi}{2})$

EM waves and Light, index of refraction, Wave fronts and rays, hygen's principle, polarization, malus's law

Radiation pressure $p_{rad} = S_{av}/c = I/c$, *2 for reflection. Polarization, $I = I_0 \cos^2(\phi)$.

$c = \omega/k = \lambda f = \lambda/T$;

Index of refraction $v_n = c/n = f/\lambda_n$, $\lambda_n = \lambda/n$

Huygens principle, wave is source of wavelets. Polarization: $I = 0.5 * I_0$, $I = I_0(\cos^2(\phi))$

interference: $I = 4I_0 \cos^2(\Delta\phi/2)$, $I_0 = 0.5 c \epsilon_0 E_0^2$, $d * n$, $\Delta\phi = 2\pi(n_1 L_1 - n_2 L_2)/\lambda$,

double slit $y_m = m\lambda D/d$, diffraction grating: $d \sin \theta = m\lambda$

Diffraction, single slit diffraction pattern and intensity, two slit interference with diffraction, circular apertures, resolution

slits: $I = I_0 [\frac{\sin(\beta/2)}{(\beta/2)}]^2 \cos^2(\alpha/2) = I_0$ *single slit* double slit, $\beta = \frac{2\pi a}{\lambda} \sin \theta$, $\alpha = \frac{2\pi d}{\lambda} \sin \theta$

double slit: I=above, max $y_m * d = Dm\lambda$, $d \sin \theta = m\lambda$, min $(m + 0.5)$

single slit: I=above, min $y_m = D \tan \theta_m$, $a \sin \theta = m\lambda$, max 0 and $(m + 0.5)$, small slit long wavelength get one wide max

circular pinhole: first dark ring $\sin \theta_1 = 1.22\lambda/D$, $\theta_R = \sin^{-1}(1.22\lambda/D)$, approx at small angle $\theta_R = 1.22\lambda/D$, distinguishable if max of second is outside first min of first

special relativity, frames of refrence, lorentz factor, time dialation, length contraction, relativistic momoentum and energy, energy and mass units

$\gamma = 1/\sqrt{1 - (v/c)^2}$. moving clock appears to orun slowly, things look shorter. Length viewed L of moving object
 actaul length L_0 , $L = 1/\gamma L_0$, $x' = \gamma(x - ut)$, $t' = \gamma(t - ux/c^2)$

momentum $p = \gamma mv$, $KE = (\gamma - 1)mc^2$, $Energy_{total} = K + E_0 = (\gamma - 1)mc^2 + mc^2 = \gamma mc^2$. $E^2 = (pc)^2 + (mc^2)^2$

$m = E_0/(c^2)$, $1eV = 1.6 * 10^{-19}J$

photons, photoelectric effect, stopping potential, Einstein's photoelectric equation, work function, intensity in the photon model, photon momentum and the Compton experiment, intro to wave particle duality

$KE_{max} = eV_0$, individual photon energy $E = hf$, $KE = hf - \phi$, $V_0 = hf/e - \phi/e$, V_0 vs f , slope h/e , intercept $-\phi/e$

$I = \text{power/area} = \text{energy}/(\text{time} * \text{area})$, for photons $I = N * hf/(t * A) = F * E = \text{photon flux} * \text{photon energy}$.

$E^2 = (pc)^2$, $p = E/c = hf/c = h/\lambda$

Compton experiment: $\lambda' - \lambda = h/(mc)(1 - \cos \phi)$, λ' = after collision, ϕ = scatter angle, m = electron mass, it exists.

$x = 1.60218 * 10^{-19}$; $E : eV = xJ$; $p : eV/c = x^2 kgm/s$; $m : eV/c^2 = x^3 kg$

Nuclear binding energy: $E_B = (ZM_H + NM_N - \frac{A}{Z}M)c^2$, M_H = hydrogen mass, M_N = neutron mass, $N = A - Z$ = neutrons, $\frac{A}{Z}M$ = mass of atom, Z = atomic number, A = isotope mass number; rest energy of nucleus $= E_0 - E_B$

$A + B \rightarrow C + D$, $E_A + E_B = E_C + E_D + Q$, $Q = (M_A + M_B - M_C - M_D)c^2$

magnitude charge of an electron, 1eV in J, $e = 1.60218 * 10^{-19}$

$h = 6.62607 * 10^{-34}$; $m_e = 9.10938 * 10^{-31}$; $m_p = 1.6726 * 10^{-27}$; $m_n = 1.6749 * 10^{-27}$

$\mu_0 = 4\pi * 10^{-7}$; $\epsilon_0 = 1/(\mu_0 c^2) = 8.854 * 10^{-12}$

one atomic mass unit $u = 1.6605 * 10^{-27}$; electron rest energy $m_e c^2 = 0.51099 MeV$

EXAM FINAL

wave particle duality: $\hbar = h/(2\pi)$

single slit: triangle where base = p_x , height = p_y , hypotenuse = p , $\theta = \delta$, small angle $\theta \approx \sin \theta = \lambda/a$, $p_x \approx p$, $\delta \approx \tan \delta = p_y/p$

uncertainty: $\Delta p_y \Delta y \geq \hbar/2$, $\Delta E \Delta t \geq \hbar/2$, $\Delta E = h \Delta f$

matter waves: $\lambda = h/p = h/(mv) = h/\sqrt{2mK}$, $f = E/h$

wave functions: 1D motion mass m , wave function Ψ , potential energy U , $\frac{\hbar^2}{2m} \frac{\delta^2 \Psi(x,t)}{\delta x^2} + U(x)\Psi(x,t) = i\hbar \frac{\delta \Psi(x,t)}{\delta t}$
 $U = 0$: $\Psi(x,t) = Ae^{i(kx - \omega t)} = A \cos(kx - \omega t) + iA \sin(kx - \omega t)$, wave number $k = 2\pi/\lambda$, $p = \frac{h}{\lambda} = \hbar k$, $\omega = 2\pi f$, $E = hf = \hbar \omega$

wave packets: Real $\Psi(x,t)$ is sin, Imaginary $\Psi(x,t)$ is cos, $2\pi/k_{av} = \lambda_{av}$ is one period, x is whole length of packet

Δx is possible positions, width of wave.

$|\Psi|^2 = \Psi_r^2 + \Psi_i^2 \geq 0$, pos of find part betw x and $x + dx$ is $P(x, x + dx, t) = |\Phi(x, t)|^2 dx$, $P(x_1, x_2, t) = \int_{x_1}^{x_2} |\Psi(x, t)|^2 dx$

possible Prob functions: 1) must be unity, area = 1. 2) single valued function. 3) continuous. 4) spatial derivative continuous

$\Delta k \Delta x \approx 1$

$\Psi(x, t) = \psi(x)e^{iEt/\hbar}$, $|\Psi(x, t)|^2 = \Psi(x, t) \cdot \Psi(x, t)^* = |\psi(x)|^2$

distortion: $L_{felt} = \frac{1}{\gamma}L_0$ and it doesn't take as long to travel as it seems. $\Delta t = \gamma \Delta t_0$, feels like $\Delta t_0 = \frac{1}{\gamma} \Delta t = \frac{1}{\gamma} \frac{26 \text{cyr}}{.90c}$

kg to eV: $m = m \frac{c^2}{c^2} = \frac{kg * (m/s)^2}{c^2} \cdot \frac{1eV}{1.6 * 10^{-19}J}$

PUT UNITS EVEN IF YOU DON'T KNOW THE ANSWER