

## Chapter 5-2 Quantitative electrostatic relationships

We make the analysis in 1 dimension, even though actual diode as shown may not be a one-dimensional system. This makes the analysis simple. The metallurgical junction is located at  $x = 0$ .

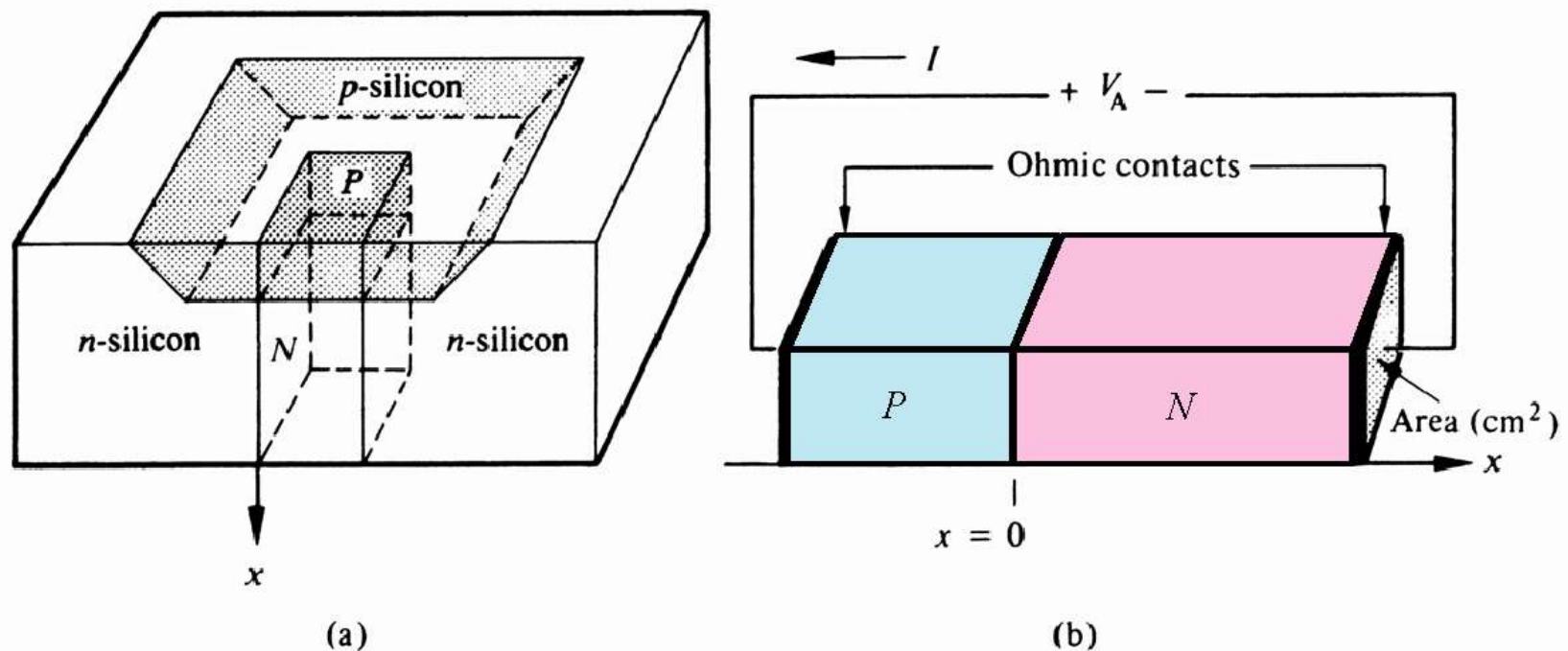


Figure 5.8

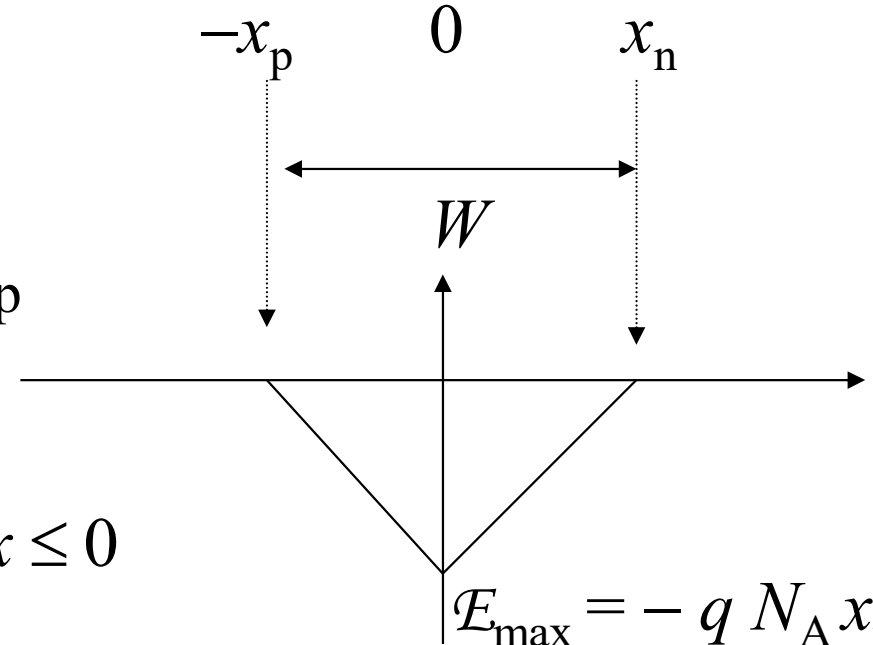
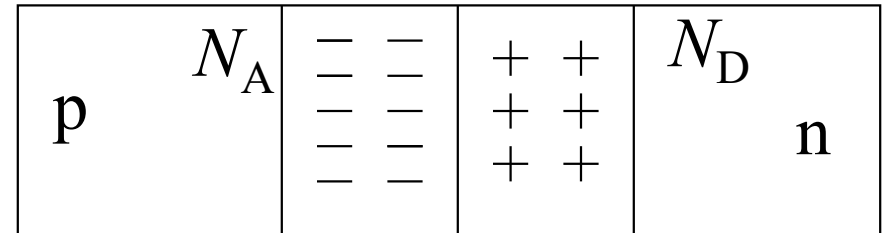
# Quantitative analysis: Electric field $\mathcal{E}$

$$\frac{d\mathcal{E}}{dx} = \frac{\rho}{\varepsilon} \quad \text{where} \quad \varepsilon = K_s \varepsilon_0$$

$$= -\frac{q}{\varepsilon} N_A \quad -x_p < x < 0$$

$$= \frac{q}{\varepsilon} N_D \quad 0 < x < x_n$$

$$= 0 \quad x > x_n \quad ; \quad x < -x_p$$



$$\mathcal{E}(x) = -\frac{qN_A}{\varepsilon} (x_p + x) \quad -x_p \leq x \leq 0$$

$$= -\frac{qN_D}{\varepsilon} (x_n - x) \quad 0 \leq x \leq x_n$$

$$= 0 \quad x < -x_p; \quad x > x_n$$

$$\begin{aligned} E_{\max} &= -q N_A x_p / \varepsilon \\ &= -q N_D x_n / \varepsilon \end{aligned}$$

## Relationship between $x_n$ and $x_p$

$$\mathcal{E}_{\max} = -q N_A x_p / \epsilon = -q N_D x_n / \epsilon$$

$$N_A x_p = N_D x_n$$

Net charge on p-side = Net charge on n-side

Depletion layer width:  $W = x_n + x_p$

$$x_n = W \frac{N_A}{N_A + N_D} \qquad x_p = W \frac{N_D}{N_A + N_D}$$

If  $N_A \gg N_D$ , then  $W \approx x_n$       and      if  $N_A \ll N_D$ , then  $W \approx x_p$

## Built-in voltage: $V_{\text{bi}}$

$$\mathcal{E} = -\frac{dV}{dx} \quad \text{or} \quad V_{\text{bi}} = - \int_{-x_p}^{x_n} \mathcal{E}(x) dx$$

$$V_{\text{bi}} = - \{ \text{area under } \mathcal{E} \text{ versus } x \text{ curve} \}$$

$$= - (1/2) [ W (-q N_D x_n / \varepsilon) ]$$

$$= [q / (2\varepsilon)] N_D x_n W$$

$$= \frac{1}{2} \frac{q}{\varepsilon} \left( \frac{N_A N_D}{N_A + N_D} \right) W^2 \quad \text{since} \quad x_n = W \frac{N_A}{N_A + N_D}$$

$$W = \sqrt{\frac{2\varepsilon}{q} \left( \frac{N_A + N_D}{N_A N_D} \right) V_{\text{bi}}}$$

# Quantitative analysis: Electrostatic potential

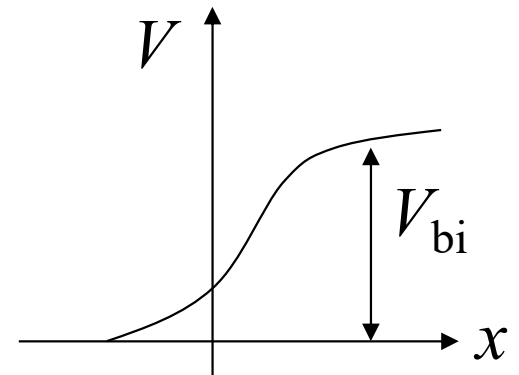
$$\frac{dV}{dx} = \frac{qN_A}{\varepsilon} (x_p + x) \quad -x_p \leq x \leq 0$$

$$= \frac{qN_D}{\varepsilon} (x_n - x) \quad 0 \leq x \leq x_n$$

with the reference potential at  $x = -x_p$  set to zero

$$V(x) = \frac{qN_A}{2\varepsilon} (x_p + x)^2 \quad -x_p \leq x \leq 0$$

$$= V_{bi} - \frac{qN_D}{2\varepsilon} (x_n - x)^2 \quad 0 \leq x \leq x_n$$



## Step junction with $V_A \neq 0$

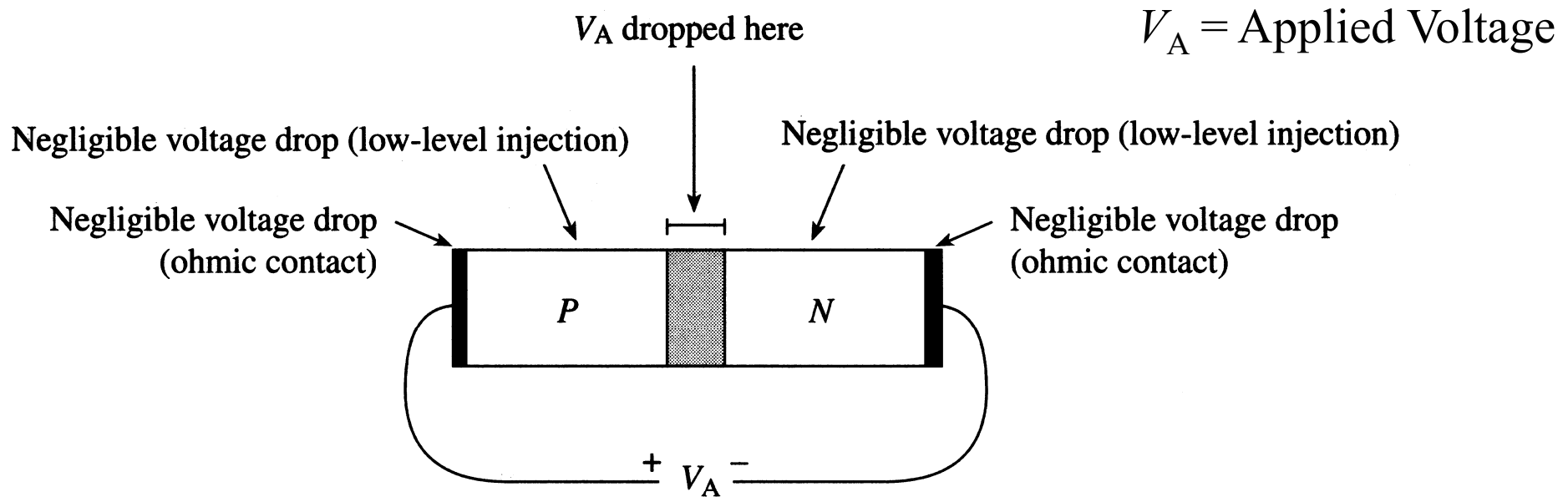
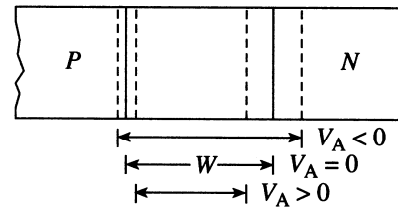


Figure 5.10

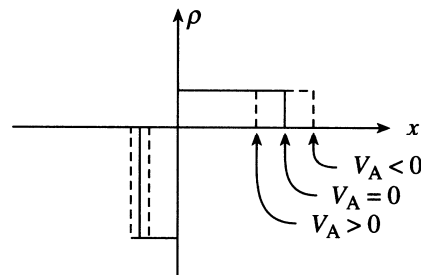
The equation for  $W$  is similar to the earlier equation except that  $V_{bi}$  is replaced by  $V_{bi} - V_A$ ; ( $V_A$  is restricted to  $V_A < V_{bi}$ ).

$$W = \sqrt{\frac{2\epsilon}{q} \left( \frac{N_A + N_D}{N_A N_D} \right) (V_{bi} - V_A)}$$

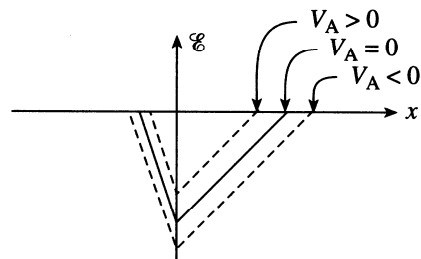
# Effects of forward and reverse bias



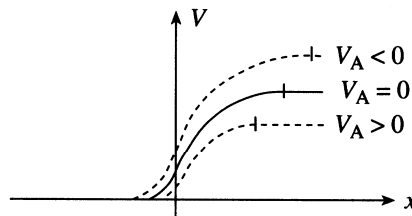
(a)



(b)



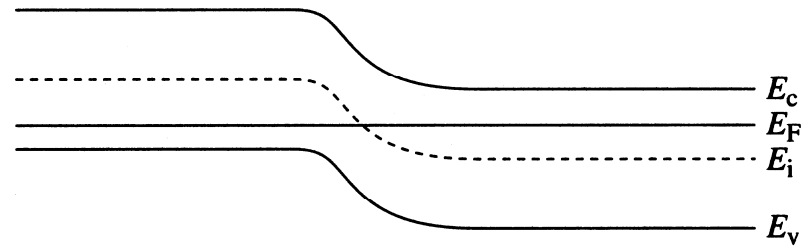
(c)



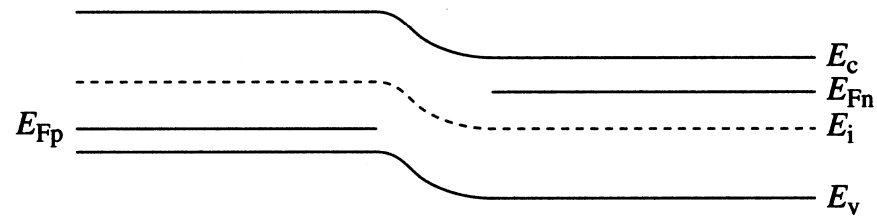
(d)

Figure 5.11

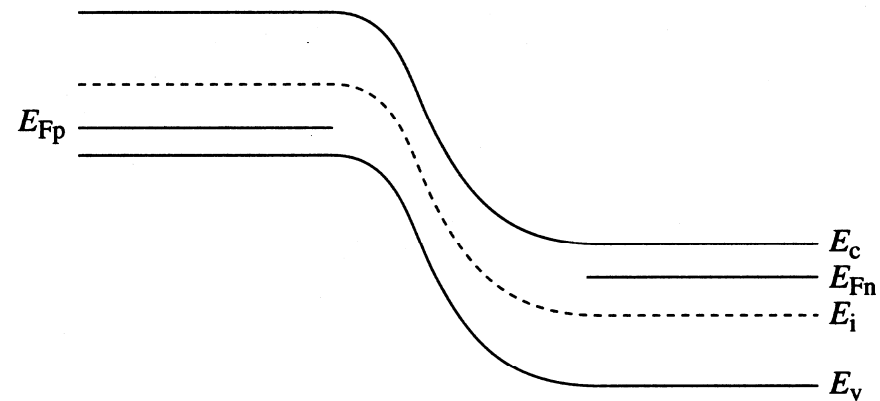
# PN-junction energy-band diagrams



(a) Equilibrium ( $V_A = 0$ )



(b) Forward bias ( $V_A > 0$ )



(c) Reverse bias ( $V_A < 0$ )

Figure 5.12



## Example 1

Consider the following diode. Calculate the maximum electric field,  $\mathcal{E}_{\max}$ , the location of  $\mathcal{E}_{\max}$ , the depletion layer width  $W$ ,  $x_n$  and  $x_p$  and the built-in voltage,  $V_{bi}$ . Carefully plot the charge density, electric field, and the potential as a function of  $x$ .

$N_D = 2 \times 10^{16} \text{ cm}^{-3}$ $N_A = 1 \times 10^{16} \text{ cm}^{-3}$	$N_A = 3 \times 10^{17} \text{ cm}^{-3}$ $N_D = 2 \times 10^{17} \text{ cm}^{-3}$
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Also, calculate the depletion layer width and the maximum electric field if a reverse voltage of 10 V is applied across the diode.

What will be  $W$  if  $V_A = 0.5 \text{ V}$ ?

## Example 2

Consider the diode of Example 1. Calculate the depletion layer width and the maximum electric field if a reverse voltage of 10 V is applied across the diode. Calculate the depletion layer width in the n-side and p-side under this biased condition.

What will be  $W$  if  $V_A = 0.5$  V?

What happens if we apply  $V_A > V_{bi}$ ?