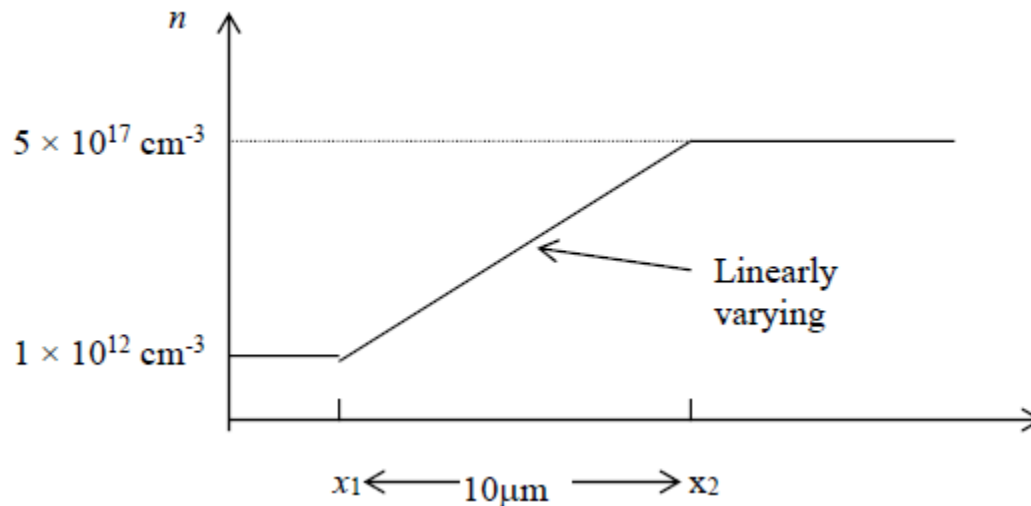


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Microelectronics HW4

1. A silicon sample maintained at 300 K under thermal equilibrium has a non-uniform doping concentration profile, such that the electron concentration, n , varies linearly from $1 \times 10^{12} \text{ cm}^{-3}$ to $5 \times 10^{17} \text{ cm}^{-3}$ while going from point x_1 to point x_2 (see figure below). Assume that the mobility is constant at $1000 \text{ cm}^2/\text{Vs}$ throughout the sample. Answer the following.

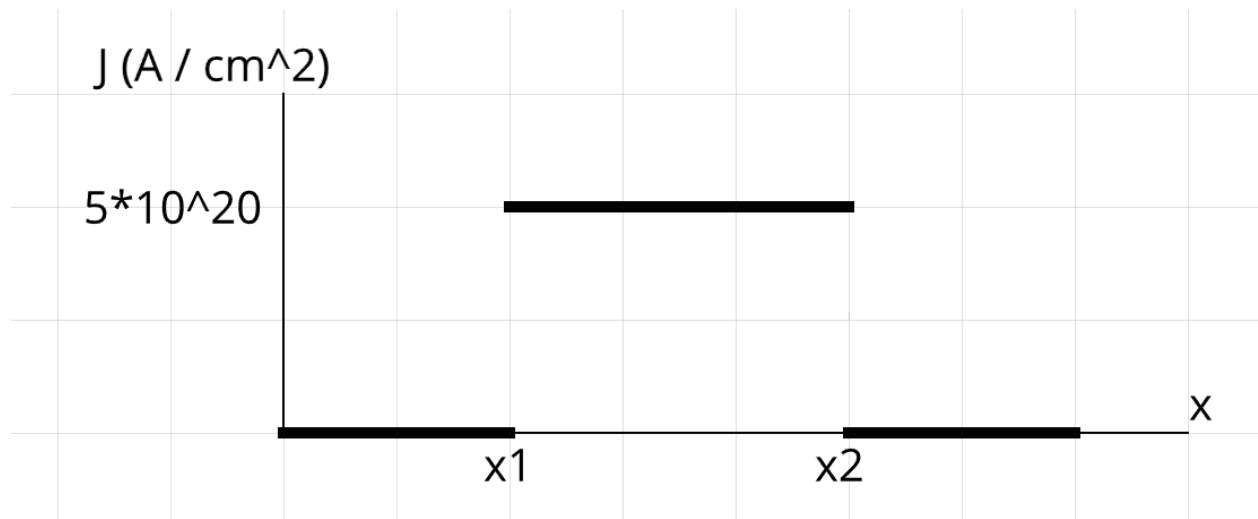


- a. Calculate the diffusion coefficient, D_n (in cm^2/s) for the electrons.
 $D_n = kT/q \cdot u_n = .0256 \cdot 1000 = 25.6 \text{ cm}^2/\text{s}$
- b. Explain why the electrons do not diffuse everywhere such that the concentration is uniform throughout.
 Because there is non uniform doping.
- c. Plot the diffusion current density (A/cm^2) for the electrons as a function of x . Mark the numerical value on the graph. (Hint: What is the equation for diffusion current density?)

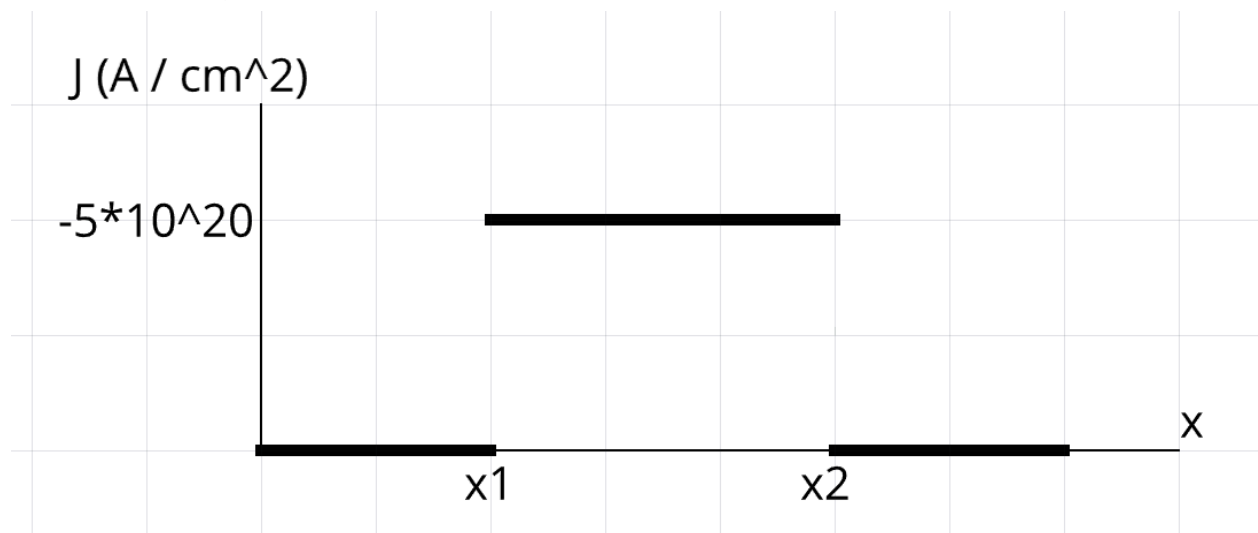
$$J_{ndiff} = q D_n \frac{\Delta n}{\Delta x}$$

$$1.60 \cdot 10^{-19} \cdot 25.6 \cdot \text{slope} = 5 \cdot 10^{20} \text{ A}/\text{cm}^2$$

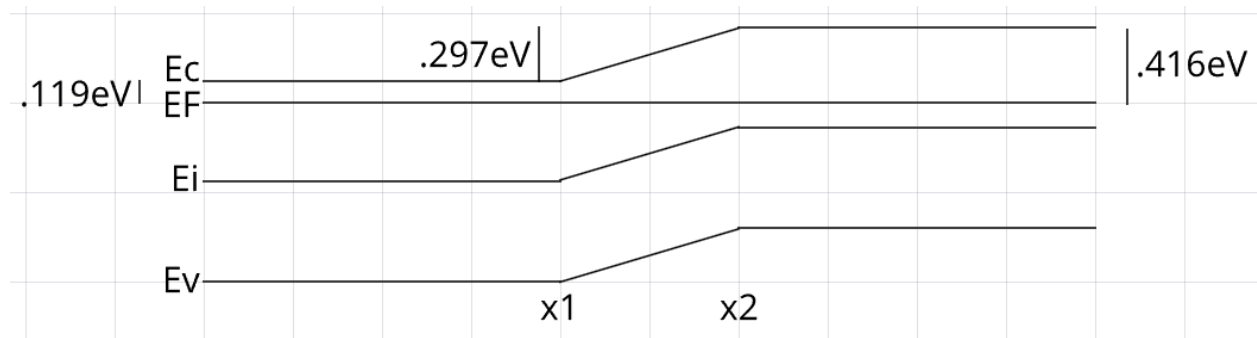
$$C \cdot \text{cm}^2 \text{s}^{-1} \cdot \text{cm}^{-3} \cdot \text{cm}^{-1} = \text{A cm}^{-2}$$



- d. Plot the drift current density for electrons as a function of x (Hint: What should be the total current? Then, obtain answer to this from part c).
Total current is 0, so drift must cancel out diffusion



- e. Plot the energy band diagram as a function of x . (Hint: Plot the band diagram for $x < x_1$ and for $x > x_2$ and then plot qualitatively between x_1 and x_2).
- $n = n_i e^{((EF - E_i)/kT)}$
 $10^{12} = 10^{10} e^{((EF - E_i)/0.0258)}$
 $10^2 = e^{((EF - E_i)/0.0258)}$
 $0.0258 \ln(10^2) = EF - E_i = 0.119$
 $0.0258 \ln(10^7) = EF - E_i = 0.416$



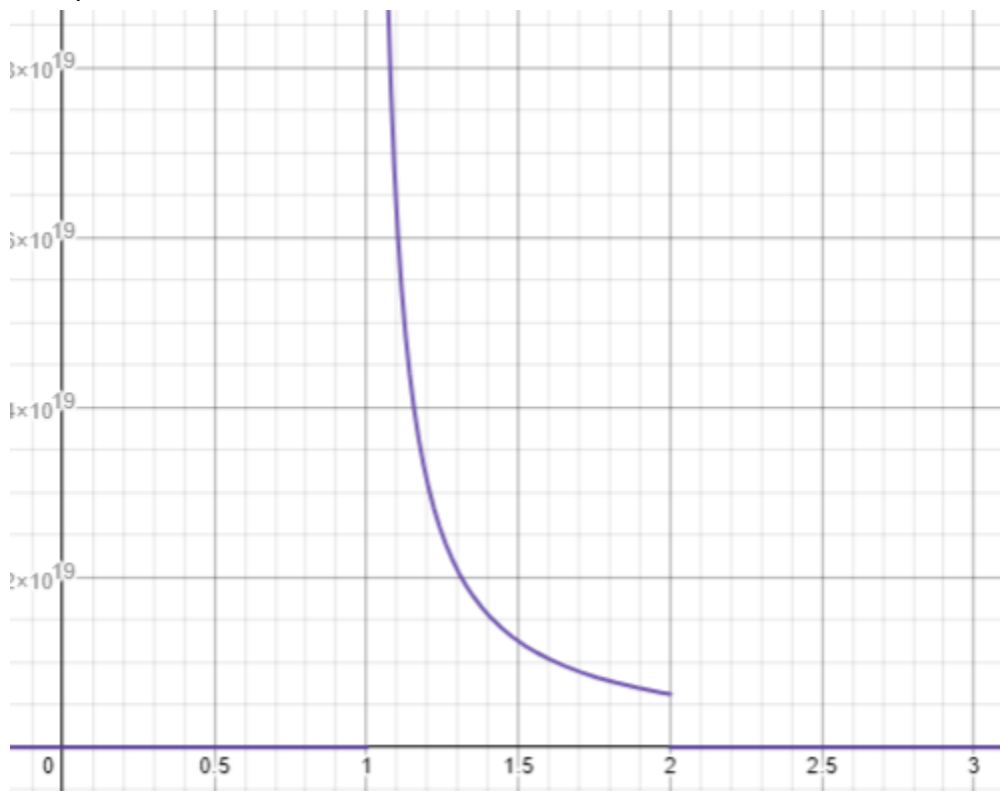
- f. What is the potential difference (give a numerical value) between the two ends of the sample? (Hint: Read it off from the band diagram!)

$.297\text{eV}$

- g. Plot a graph of the electric field versus x . (Hint: You can get this from part d and from the equation for the electron drift current density).

$$J = qnE$$

$$E = J/qn$$



2. A 5-Ohm resistor is to be made from a bar-shaped piece of n-type Si. The bar has a crosssectional area of 10^{-2} cm^2 . The silicon is doped with $N_D = 5 \times 10^{17} \text{ cm}^{-3}$ and $N_A = 4 \times 10^{17} \text{ cm}^{-3}$. Determine the length of the silicon bar.

$$n = 10^{17}$$

$$p = 10^3$$

$$\rho = 1/(q(u_n n + u_p p)) = 0.0625$$

$$R = \rho \cdot l / c$$

$$l = R \cdot c / \rho$$

$$= 0.8 \text{ cm}$$