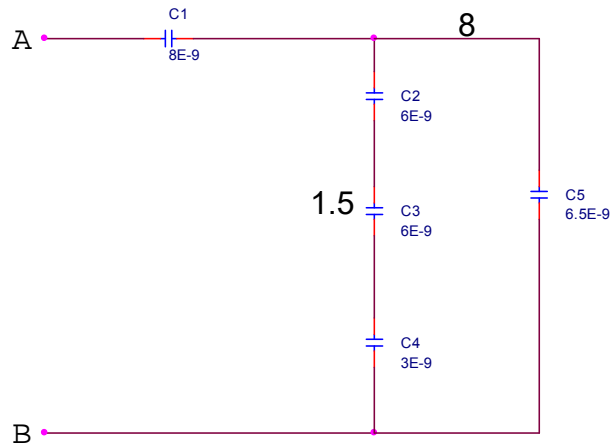


## 1) Equivalent impedances

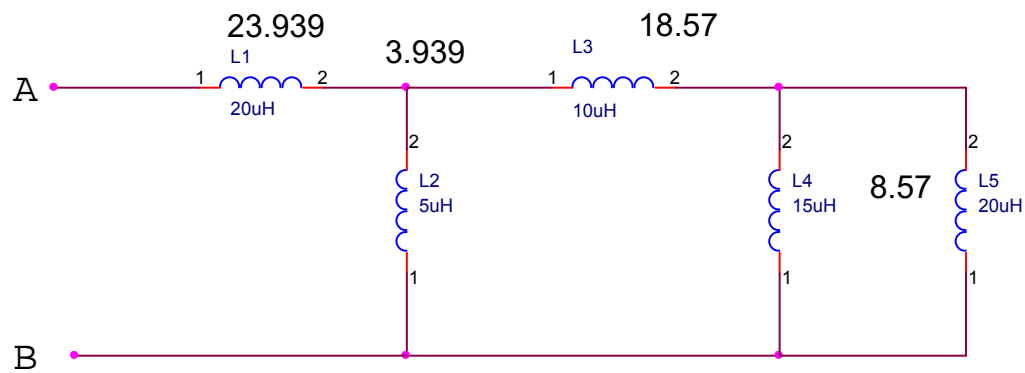
a



$$C_1 := 8 \cdot 10^{-9} \text{ F} \quad C_2 := 6 \cdot 10^{-9} \text{ F} \quad C_3 := 6 \cdot 10^{-9} \text{ F} \quad C_4 := 3 \cdot 10^{-9} \text{ F} \quad C_5 := 6.5 \cdot 10^{-9} \text{ F}$$

1.1: For the above circuit, determine the equivalent capacitance between A and B

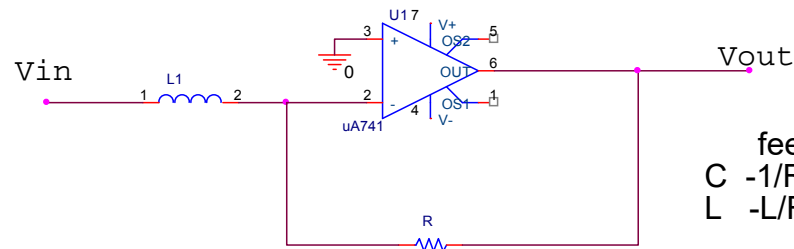
4nF



1.2: For the above circuit, determine the equivalent inductance between A and B

23.939uH

## 2) Amplifier circuits



|   |                            |                           |
|---|----------------------------|---------------------------|
|   | feedback                   | in                        |
| C | $-1/RC \int (V_{in}) dt$   | $-RC \frac{d}{dt} V_{in}$ |
| L | $-L/R \frac{d}{dt} V_{in}$ | $-R/L \int (V_{in}) dt$   |

2.1: For the RL amplifier circuit, determine the relationship between  $V_{out}$  and  $V_{in}$ . As with RC amplifier circuits, KCL is a good starting point. (The power is taken out for simplicity but the op amp is powered).

$$V_{out} = -R/L \int_0^t V_{in} dt$$

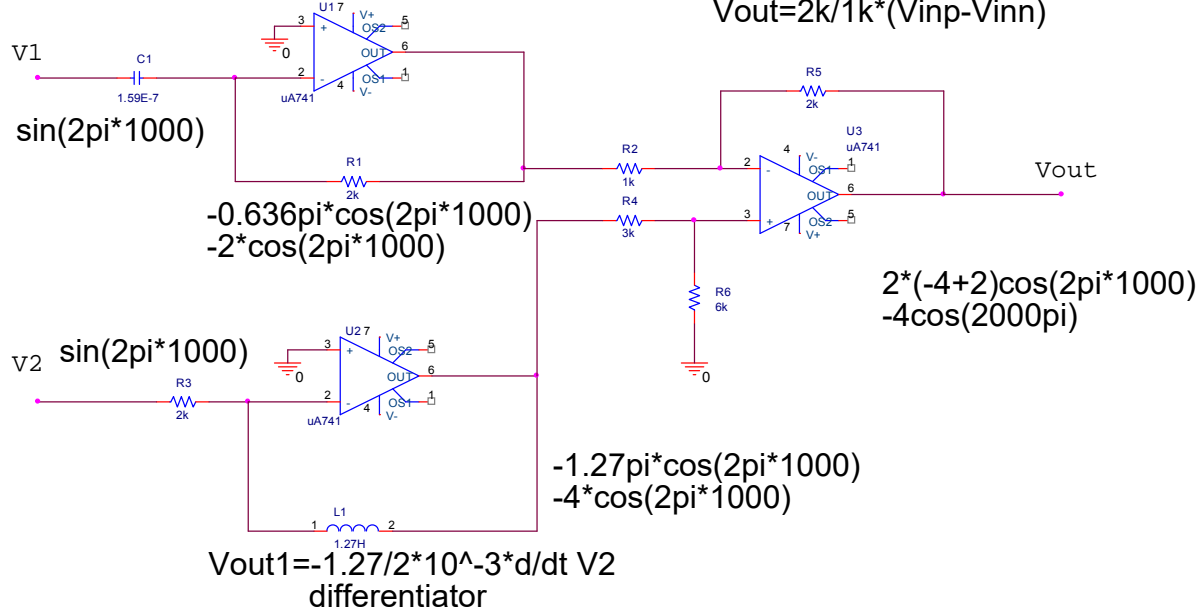
2.2: What type of op amp is this? integrator

differentiator

$$V_{out1} = -1.59 \times 10^{-4} \frac{d}{dt} V_1$$

differentiator

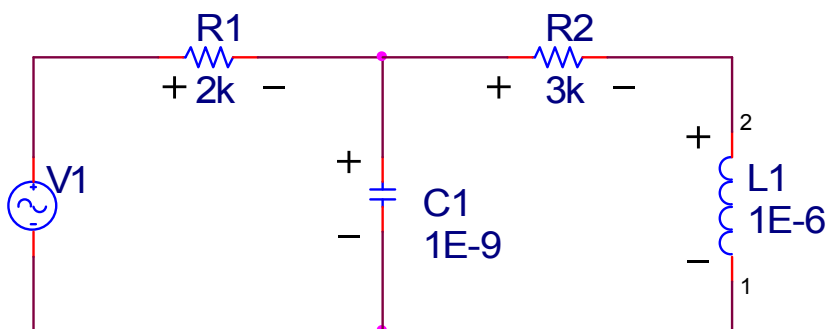
$$V_{out} = 2k/1k * (V_{inp} - V_{inn})$$



2.3: In the above circuit  $V_1 = V_2 = 1 \sin(2\pi f t)$  where the frequency is 1 kHz. Determine  $V_{out}$ .

$$-4 \cos(2000\pi)$$

## 3) Voltage/Current continuity



In the above circuit, the voltage is defined as follows:

$$V1 = \begin{cases} 5V & t < 0 \\ 10V & 0 < t \end{cases} \quad (\text{the voltage source turns on at } t = 0)$$

3.1: Determine a mathematical expression for the source.

$$V = 5u(t) + 5$$

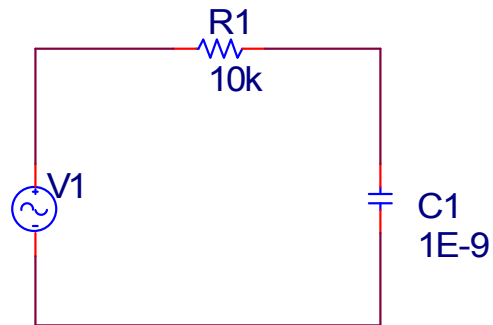
3.2: At  $t = 0^-$  (just before the voltage changes), for the polarities indicated, determine the voltage across each component and the current through each component.

|         |    |    |     |
|---------|----|----|-----|
| C=open  | R1 | 2V | 1mA |
| L=short | R2 | 3V | 1mA |
|         | C  | 3V | 0mA |
|         | L  | 0V | 1mA |

3.3: At  $t = 0^+$  (just after the voltage changes), determine the voltage across each component and the current through each component for the polarities indicated in the circuit.

|    |    |       |
|----|----|-------|
| R1 | 7V | 3.5mA |
| R2 | 3V | 1mA   |
| C  | 3V | 2.5mA |
| L  | 0V | 1mA   |

## 4) First order circuits



4.1: Determine the voltage as a function of time for the source voltage  $V1 = 10 u(t)$ .

$$10 - 10e^{-t/10^{-5}}$$

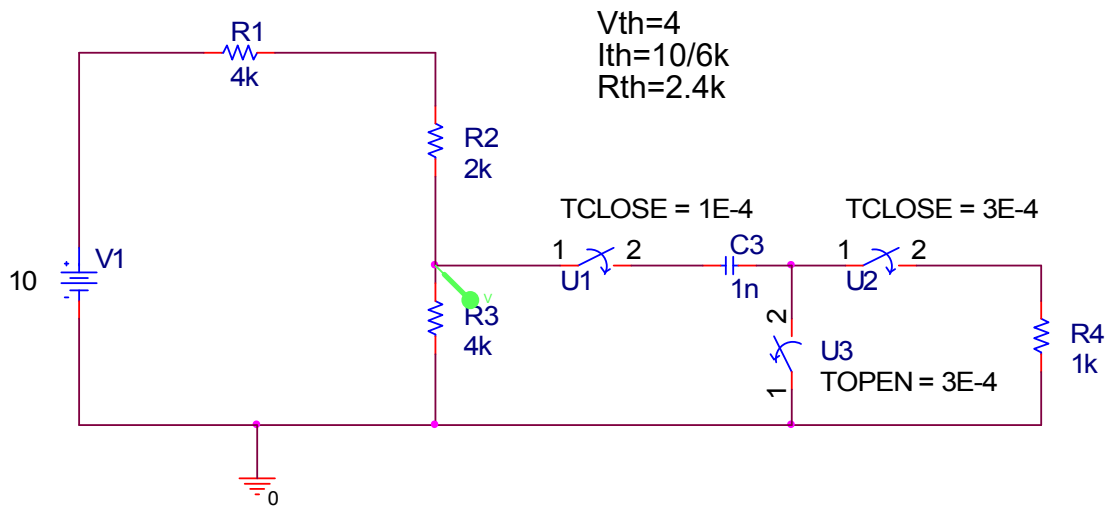
4.2: Determine the voltage as a function of time for the source voltage  $V1 = 8 - 3u(t)$

$$5 + 3e^{-t/10^{-5}}$$

initial+change

$$\text{final-change} \cdot e^{-t/T}$$

## 5. First order switching circuit



In the above circuit, the voltage source turns on at  $t = 0$ . Switch U1 closes at  $t = 0.1$  ms. Switch U2 closes and switch U3 opens at  $t = 0.3$  ms (effectively putting resistor R3 in series with C3 at  $t = 0.3$  ms).

5.1: Determine the voltage across R3 as a function of time for  $t > 0$ .

|                 |   |  |
|-----------------|---|--|
| $t < 0$         | 0                                       | $0 < t < .1$ TH $V_{TH}=4$ $I_{TH}=10/6k=1.667mA$ $R_{TH}=4/1.667m=2.4k$ |
| $0 < t < .1m$   | 4                                       |  |
| $.1m < t < .3m$ | $4(1-e^{\{-(t-.0001)/(2.4*10^{-6})\}})$ |  |
| $.3m < t$       | 4                                       |  |

.2ms is multitudes times the time constant, so we can say that at  $t=.3ms^-$ ,  $V=4$ . Adding resistance does nothing since the capacitor acts as an open circuit.