

1) Equivalent circuits



	par	ser	
C	low	high	pass
L	high	low	

1.1: For  $I = 8\angle 45^\circ \text{mA}$  in phasor form with a 1.59kHz frequency, determine the voltage  $V1$  in the time domain form.  
 $\omega = 2\pi f$   $\omega = 10\text{k}$

$$Z = Z_R + Z_L = 6\text{k} + j10\text{k} \cdot 25\text{m} = 6\text{k} + j250$$

$$V = I \cdot Z$$

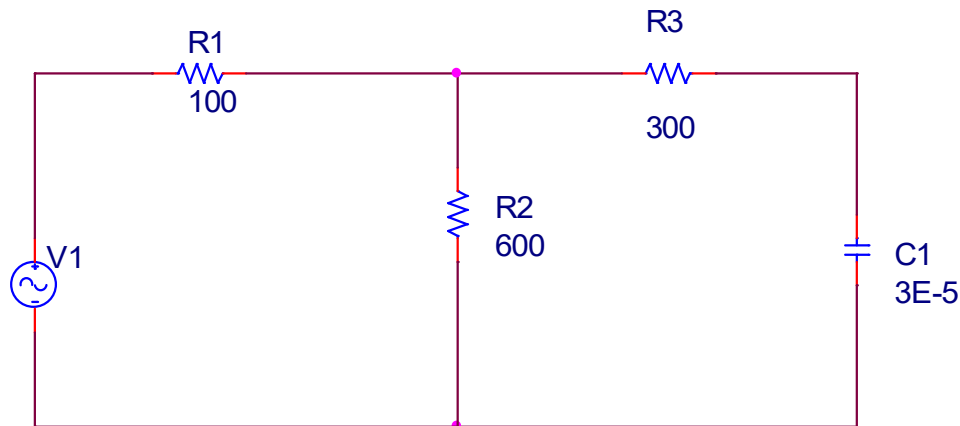
$$V = 48.04 \angle 47.38$$

$$V = 48.04 \cdot \cos(10\text{E}3 \cdot t + 47.38)$$

$$d = r / (2\pi) \cdot 360$$

$$r = d / 260 \cdot 2\pi$$

## 2) First order circuits



The source is a 15V sinusoidal signal with a frequency of 31.83Hz and has zero phase.

$$\omega = 200$$

2.1: Determine the phasor expression for the voltage source.

$$V = 15 \angle 0$$

2.2: Determine the equivalent impedance seen by the source.

$$Z_C = 1/(j \cdot 4E3 \cdot 5E-5), Z_1 = 100, Z_2 = 600, Z_3 = 321.34 \angle -12.88$$

$$Z = Z_1 + (Z_2^{-1} + (Z_3 + Z_C)^{-1})^{-1}$$

$$Z = 321.34 \angle -12.88 \text{ ohms}$$

2.3: Determine the phasor expression for the current through the source.

$$I = V/Z \quad I = 15 \angle 0 / 321.34 \angle -12.88 = 0.04667 \angle 12.88$$

$$I(V) = 46.67 \angle 12.88 \text{ mA}$$

2.4: Determine the phasor expression for the voltage across  $C_1$ .

$$I_C = I_3, I_V = I_1, I_3 = I_1 \cdot Z_2 / (Z_2 + Z_3 + Z_C) = 0.03060 \angle 23.37, V = I \cdot Z = 5.10 \angle -66.63$$

$$V(C) = 5.10 \angle -66.63 \text{ V}$$

2.5: Determine the time domain expression for the voltage across  $C_1$ .

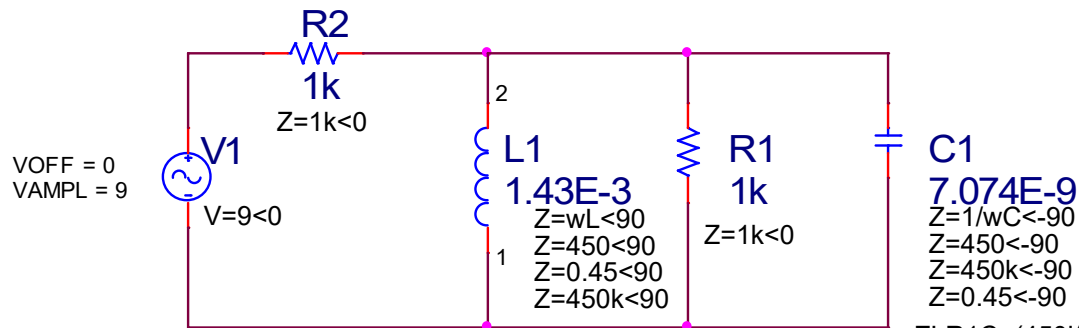
$$F = A \angle \theta, F(t) = A \sin(\omega t + \theta)$$

$$V(C)(t) = 5.10 \sin(200t - 66.63)$$

not on test 2.5: Determine the transfer function,  $H(s) = V_{C1}(s) / V_s(s)$ , for the above RC circuit.  $V_{TH} = 15 \cdot 600 / (600 + 100) = 12.86 \text{ V}$ ,  $R_{TH} = 385.71$ ,

2.6: Verify your solution to part d. using the transfer function (remember  $s = j\omega$  in AC steady state).

## 3) Phasors- RLC



3.1: Using phasor analysis, determine the voltage across the capacitor when the source is 50kHz.  
 $V_C = 9 \angle 0^\circ \cdot 1000 / (1000 + 1000) \angle 0^\circ = 4.5 \angle 0^\circ$

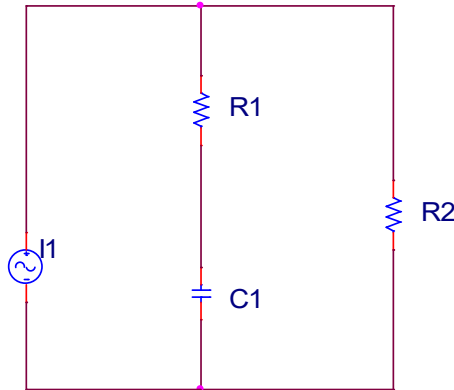
3.2: Using phasor analysis, determine the voltage across the capacitor when the source is 50 Hz. (reminder: -90degrees is -j) **Partial answer check:  $Z_{RLC} = 0.45j$**   
 $V_C = 9 \angle 0^\circ \cdot Z_{RLC} / (Z_{RLC} + 1000) \angle 0^\circ = 0.00045 \angle 90^\circ$

3.3: Using phasor analysis, determine the voltage across the capacitor when the source is 50MHz (50E6Hz).(reminder: 90degrees is j)  
 $V_C = 9 \angle 0^\circ \cdot Z_{RLC} / (Z_{RLC} + 1000) \angle 0^\circ = 0.00045 \angle -90^\circ$

## 4) Transfer functions

Determine the transfer functions in the following circuit. Determine the behavior of the transfer function as

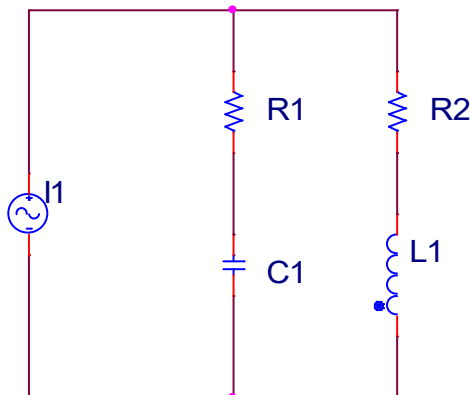
$\omega \rightarrow 0$  and  $\omega \rightarrow \infty$



4.1: Voltage across  $C_1$  relative to the source voltage  $H(s) = \frac{V_{C1}(s)}{I_1(s)}$

4.2: Determine the magnitude of the transfer function as frequency approaches zero,  $|H(s \rightarrow 0)|$

4.3: Determine the magnitude of the transfer function as frequency approaches infinity,  $|H(s \rightarrow \infty)|$



4.4: Voltage across  $L_1$  relative to the source current  $H(s) = \frac{V_{L1}(s)}{I_1(s)}$

4.5: Determine the magnitude of the transfer function as frequency approaches zero,  $|H(s \rightarrow 0)|$

4.6: Determine the magnitude of the transfer function as frequency approaches infinity,  $|H(s \rightarrow \infty)|$