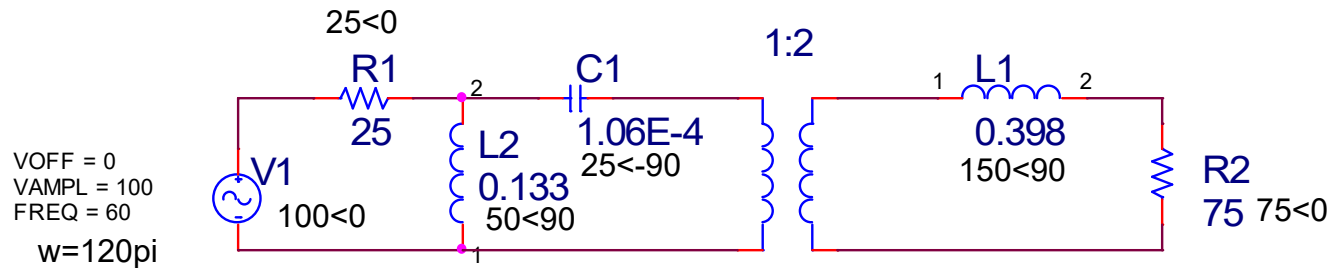


## Problem 1) Ideal Transformers and Power



1.1: For the transformer circuit above, find the equivalent circuit (without a transformer with only a source impedance and load impedance). **You may use either referral method though you should figure out which would best to use. (15 pts)**

$$V_{TH} = 100 \angle 0^\circ \cdot 50 \angle 90^\circ / (25 + 50 \angle 90^\circ) = 89.45 \angle 26.56^\circ \quad Z_{source} = 25 \angle -36.87^\circ, Z_{load} = 167.7 \angle 63.43^\circ$$

1.2: Find the voltage across the R2. **Put in phasor/polar form. (10 pts)**

$$V(\text{Load}) = 178.49 \angle 26.56^\circ, Z(\text{source equiv}) = 100 \angle -36.87^\circ, Z(\text{total}) = 179 \angle 30.14^\circ, I = V(\text{Load}) / Z(\text{total}) = 0.998 \angle -3.57^\circ$$

$$V_{R2} = I \cdot Z_{R2} = 0.998 \angle -3.57^\circ \cdot 75 = 74.85 \angle -3.57^\circ$$

equiv  $V_{TH}$   $Z_{TH}$ :  $V_1 = 89.44 \angle 26.56^\circ$   $Z_s = 25 \angle -36.87^\circ$   $Z_l = 167.71 \angle 63.43^\circ$

ref to primary: same 89 same 25  $/N^2$   $Z_l = 41.93 \angle 63.43^\circ$

phases stay the same

ref to secondary  $*N$  178.89  $*N^2$  100 same 167.7

complex power dissipated in:  $V_1 = V_{tot} \cdot R_1 / (R_1 + R_2)$ ,  $I_1 = V_{tot} / R_{tot}$ ,  $P_1 = I \cdot V_1$

primary:

$$V_1 = 89 \cdot 25 / (25 + 41) = 49.90 \angle -40.45^\circ \quad I_1 = 89 / (25 + 41) = 1.996 \angle -3.57^\circ \quad P_1 = 1.9 \cdot 49 = 99.61 \angle -44.02^\circ$$

secondary:

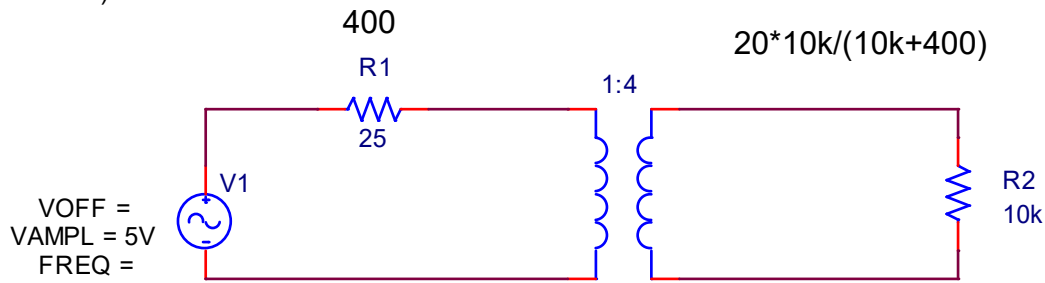
$$V_2 = 178 \cdot 167.7 / (167.7 + 100) = 167.37 \angle 59.86^\circ \quad I_2 = 178 / (100 + 167.7) = 0.998 \angle -3.57^\circ \quad P_2 = 0.998 \cdot 167.3 = 167.05 \angle 56.28^\circ$$

double check?

$$P_1 + P_2 = 99.61 + 167.05 = 178.54 \angle 22.99^\circ \quad P_1 + P_2 = P_{gen}$$

$$P_{gen} = I_1 \cdot V = 1.996 \cdot 89.44 = 178.53 \angle 22.99^\circ$$

Problem 2) Real Transformers

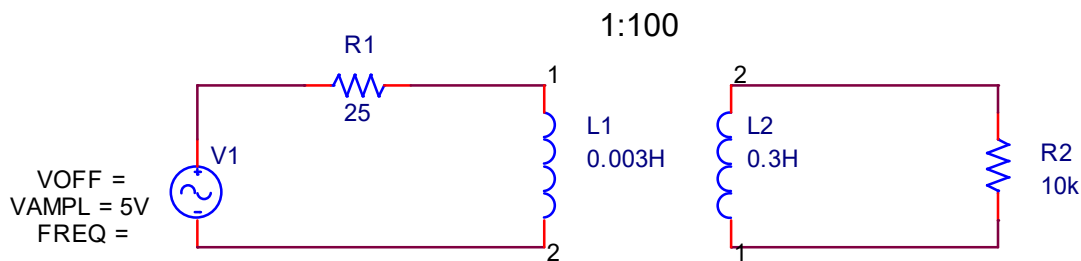


20V

19.23<0

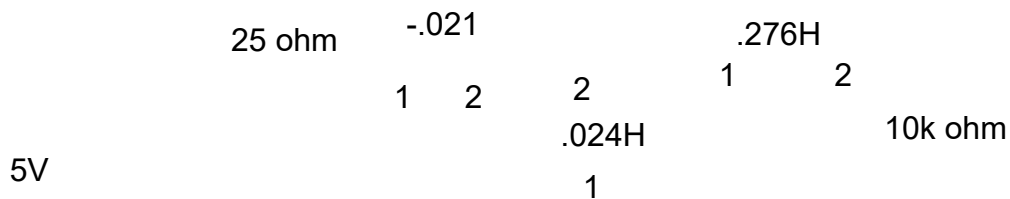
it's ideal?

2.1: Determine the voltage across R2 in phasor form

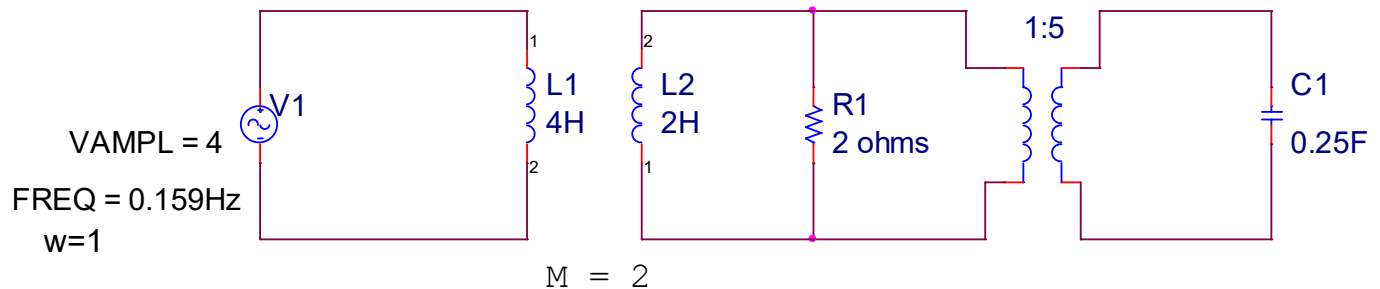


$$M = k \cdot \sqrt{L_1 \cdot L_2} = .024$$

2.2: If the real transformer is constructed of two inductors (as show) and the coupling coefficient is  $k=0.8$ , determine the Tee model of the circuit. Draw your circuit.



**Problem 3) Real and Ideal Transformers**



In the above circuit, L1 and L2 are coupled by the mutual inductance, M. The voltage source has a voltage  $V1(t) = 4 \cos(t)$  ( $\omega = 1$  rad/s). The the transformer on the right is an ideal transformer.

3.1. Draw the equivalent circuit without transformers (should include only a source impedance and a load impedance with values) **(15 pts)**. *Note: Draw the equivalent circuit so you can easily calculate current through C1. Include all calculations and supporting diagrams along the way.*

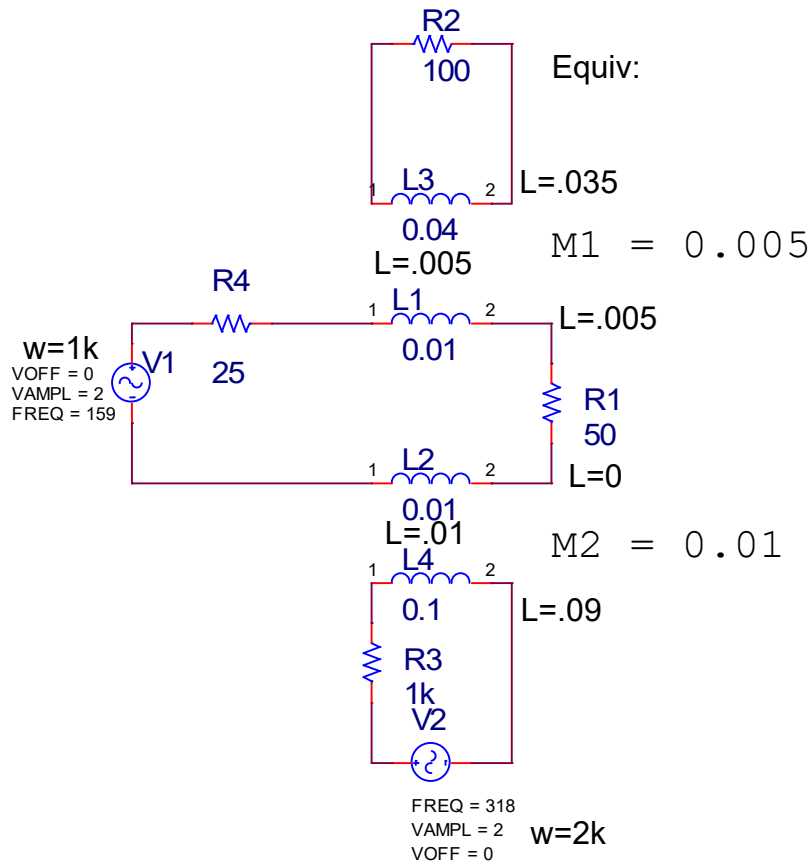
3.2: Determine the current through C1. **Put in time domain form.**

2H	<del>0H</del>	1:5	
4V<0	2H	2ohm	.25F
2<90		1:5	
4V<0	2<90	2<0	.25<-90
.894<63.43		1:5	
4V<0			.25<-90
4.47<63.43			
20V<0			.25<-90
			I=V/Z=4.706<-61.9275

$$I = 4.706 \sin(t - 1.0808) \quad (\text{in rad})$$

$$I = 4.706 \sin(t - 61.92) \quad (\text{in deg})$$

Problem 4) Mutual Inductance



Find the current and voltage through R1 in the above couple circuits. There are two locations with inductive coupling and both sets have additive coupling. Additionally, there are two voltage sources with different excitation frequencies. Suggestion, use superposition in your analysis.  
superposition  $f=159$   $w=1k$

$$\begin{aligned}
 &4.919 \angle -87.48 \\
 &105.94 \angle -19.29 \\
 &100 \\
 &35 \angle -90 \\
 &25 \\
 &5 \angle -90 \\
 &52.475 \angle -16.50 + 5 \angle -90 = 54.108 \angle -21.58 \\
 &5 \angle -90 \\
 &2 \angle 0V \\
 &50 \\
 &10 \angle -90 \\
 &I = V/Z = 2 \angle 0 / 54.108 \angle -21.58 = 0.036963 \angle -21.58 \\
 &VR = V * ZR / Z_{tot} = 2 * 50 / 54.108 \angle -21.58 = 1.848 \angle -21.583 \\
 &4k \\
 &90 \angle -90 \\
 &9.99 \angle -89.4 \\
 &10004 \angle -5.14 \\
 &V/I = 50 \quad \checkmark
 \end{aligned}$$



