

Reading list: Chapter 5 (pages 195 - 223. Ignore section 5.2.5).

1. (Problem 5.4 in text) A Si step junction under equilibrium at 300 K has a p-side doping of $N_A = 2 \times 10^{15} \text{ cm}^{-3}$ and n-side doping of $N_D = 10^{15} \text{ cm}^{-3}$. Calculate:

- a. The contact potential (also called built-in voltage).

$$V_{bi} = kT/q \cdot \ln(N_A N_D / n_i^2)$$

$$V_{bi} = 0.6132 \text{ V}$$

- b. The depletion layer width at the p-side and n-sides, and the total depletion layer width.

$$x_n = \left(\frac{2 K_S \epsilon_0}{q} \left(\frac{N_A}{N_A + N_D} \right) V_{bi} \right)^{1/2}$$

$$x_n = 7.3002 \times 10^{-5} \text{ cm}$$

$$N_A x_p = N_D x_n$$

$$x_p = x_n / 2$$

$$x_p = 3.6501 \times 10^{-5} \text{ cm}$$

$$W = x_n + x_p$$

$$W = 1.0950 \times 10^{-4} \text{ cm}$$

- c. The electric field at the metallurgical junction.

Solved from part e.

$$E = -1.1198 \times 10^4 \text{ V/cm}$$

- d. The potential at the metallurgical junction.

$$V =$$

$$\{ x < -x_p \quad 0$$

$$\{ -x_p < x < 0 \quad q N_A / (2 K_S \epsilon_0) \cdot (x_p + x)^2$$

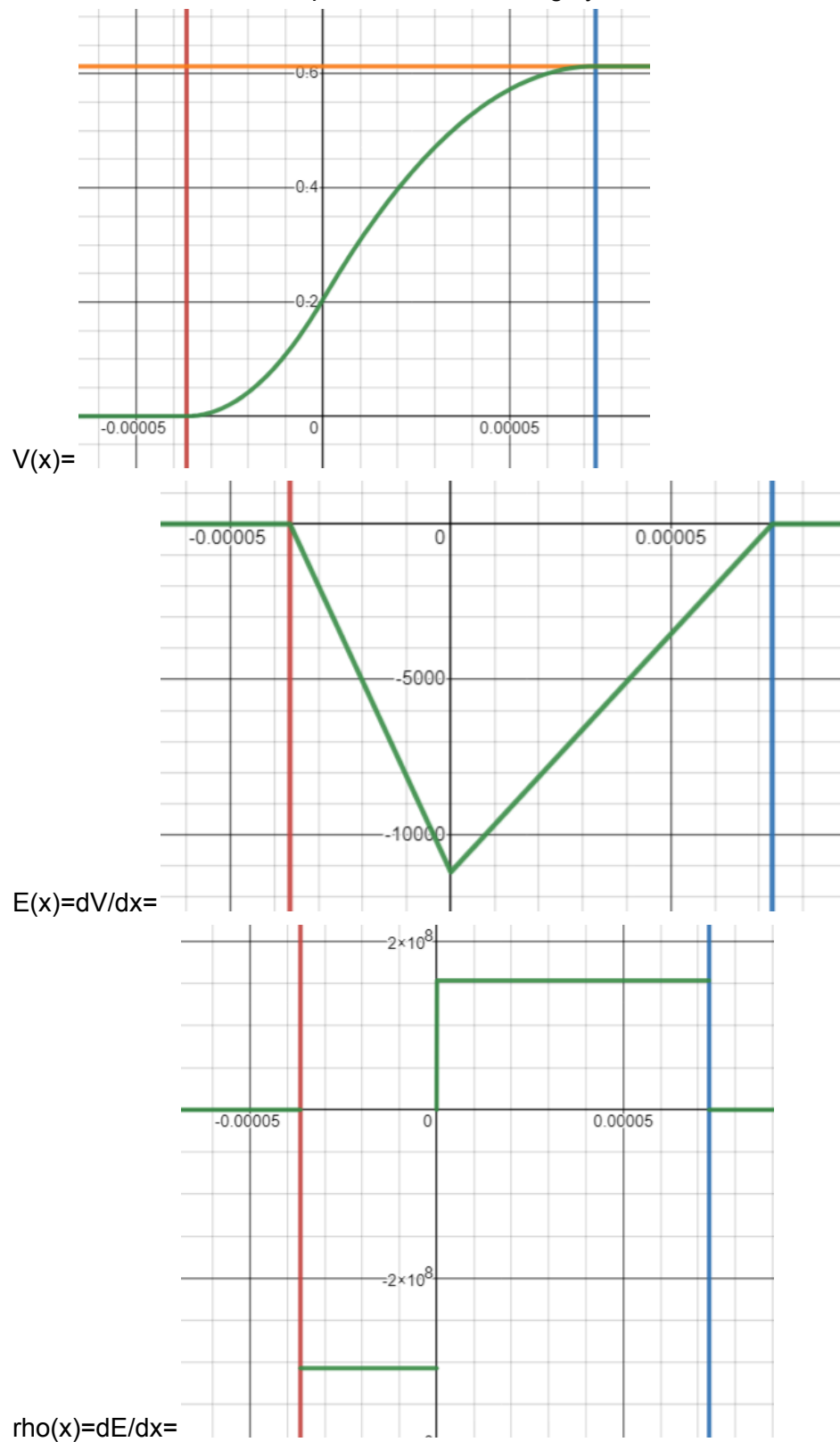
$$\{ x = 0 \quad V_{bi} \cdot N_D / (N_A + N_D)$$

$$\{ 0 < x < x_n \quad V_{bi} - q N_D / (2 K_S \epsilon_0) \cdot (x_n - x)^2$$

$$\{ x_n < x \quad V_{bi}$$

$$V(0) = V_{bi} \cdot N_D / (N_A + N_D) = 1/3 V_{bi} = 0.2044 \text{ V}$$

- e. Make sketches of the charge density, electric field and electrostatic potential as a function of position, that are roughly to scale



2. (Problem 5.5 in text) Repeat problem 1 taking $N_A = 10^{17} \text{cm}^{-3}$ to be the p-side doping. Briefly compare the results here with those obtained in problem 1.

$$V_{bi} = 0.7143 \text{ V}$$

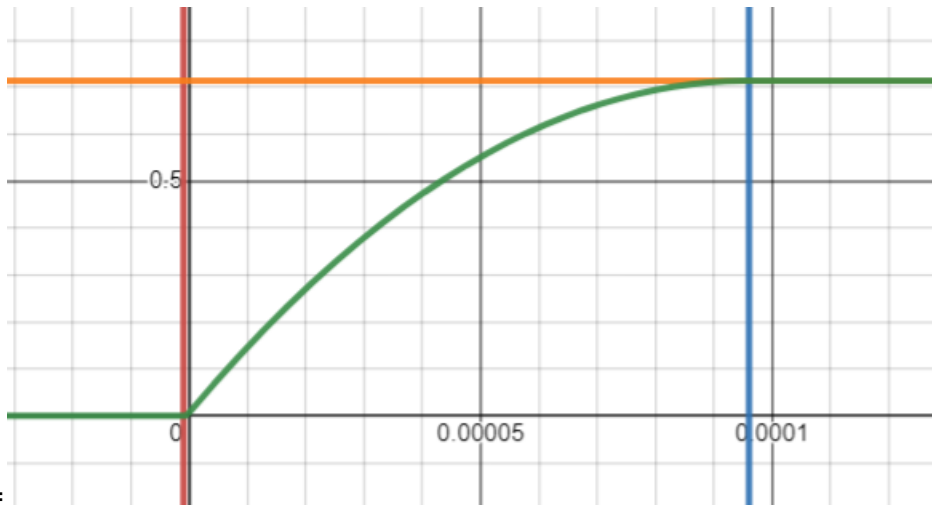
$$x_n = 9.6022 \times 10^{-5} \text{ cm}$$

$$x_p = 9.6022 \times 10^{-7} \text{ cm}$$

$$W = 9.6983 \times 10^{-5} \text{ cm}$$

$$E = 1.4730 \times 10^4 \text{ V/cm}$$

$$V(0) = V_{bi} \cdot 10^{15} / (10^{15} + 10^{17}) = 7.0722 \times 10^{-3} \text{ V}$$



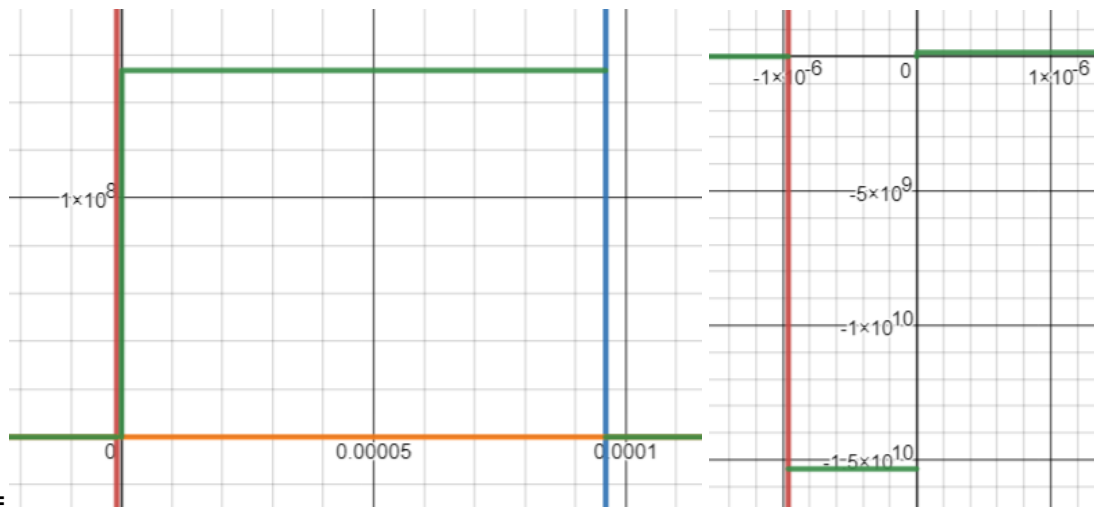
$$V(x) =$$

V_{bi} increased .61 to .71. x_n x_p shifted right and the gap shrank a little. The shape is dominated by the right side parabola.



$$E(x) =$$

$E(0)$ increased 11k to 14k. Again, the right side shape dominates



$\rho(x)=$

Charge density on the right is the same, but for a longer distance. Charge density on the left is a distance orders of magnitude shorter, and has a value orders of magnitude larger.

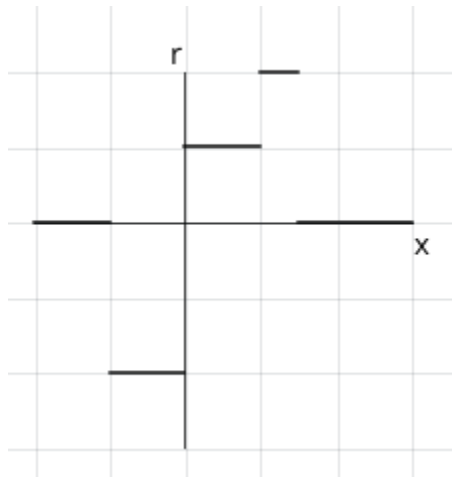
3. (Problem 5.10 in text). A p-n junction diode has the doping profile sketched below. Make the assumption that $x_n > x_0$ for all applied bias of interest. Answer the following:

a. What is the built-in voltage across the junction? Justify your answer.

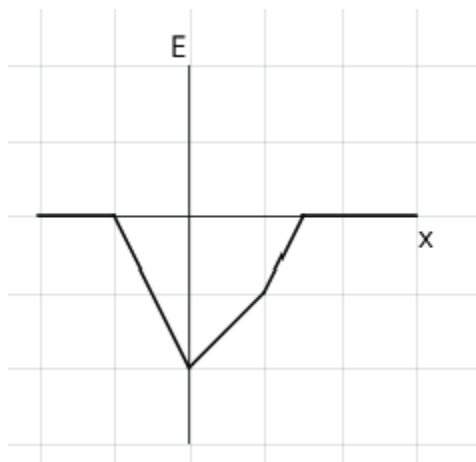
$$V_{bi} = \frac{kT}{q} \ln\left(\frac{N_A N_D}{n_i^2}\right)$$

Voltage doesn't care about path or distance, so the intermediate region has no effect on V_{bi}

b. Sketch the charge density ρ versus x inside the diode

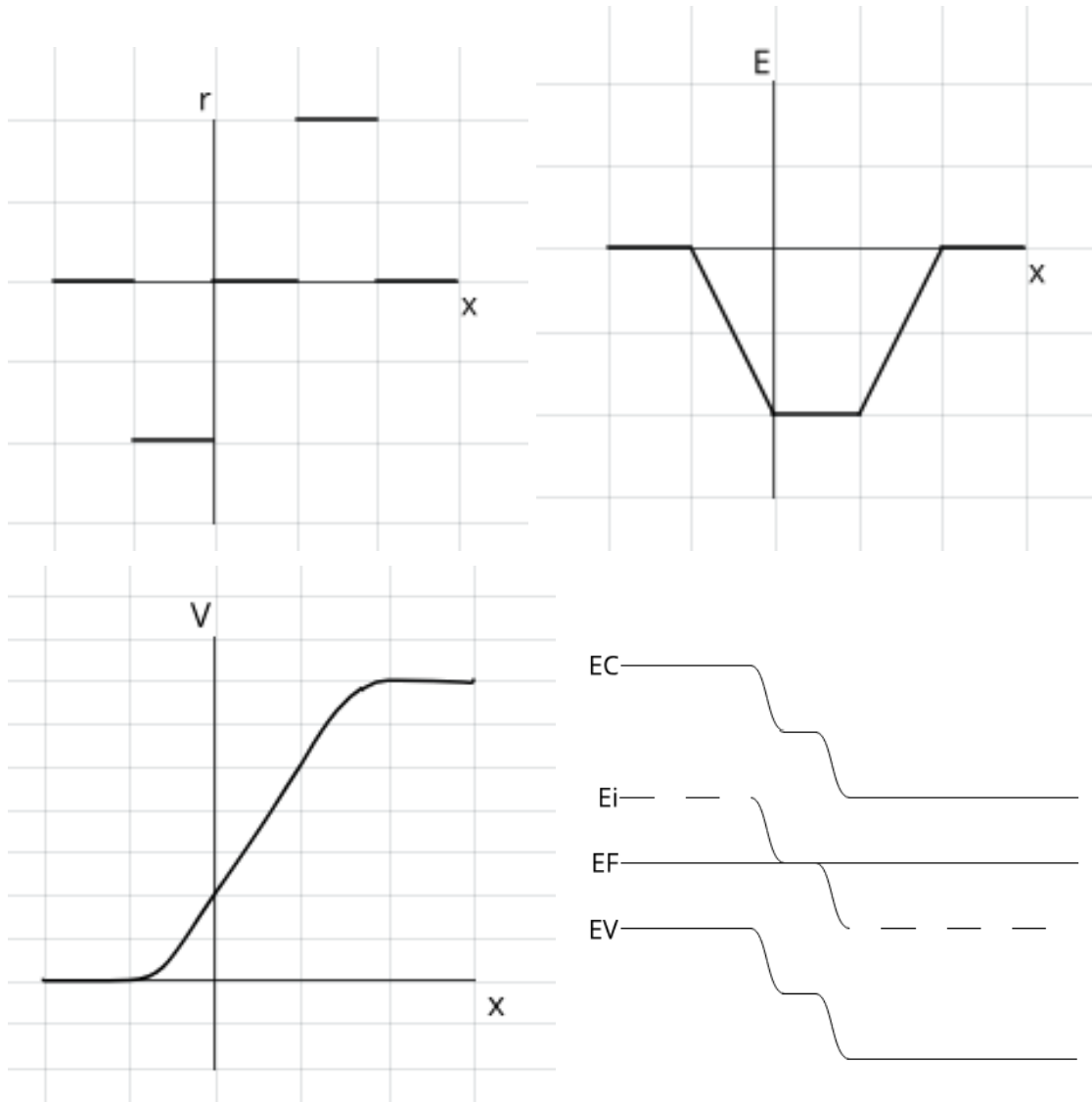


c. Sketch the expected electric field as a function of x inside the diode.



4. The p-i-n diode shown above is a three-region device with the middle region that is intrinsic and relatively narrow. Assuming the p- and n-regions to be uniformly doped and $N_D - N_A = 0$ in the i-region:

- a. Roughly sketch the expected charge density, electric field, and electrostatic potential inside the device. Also, draw the energy band diagram for the device under thermal equilibrium conditions.



- b. What is the built-in voltage drop between the p- and n-regions? Show how you arrived with your answer.

Again, voltage doesn't care about path or distance or what's in between, the intrinsic region has no effect.

$$V_{bi} = \frac{kT}{q} \ln\left(\frac{N_A N_D}{n_i^2}\right)$$

$$V_{bi} = 0.025 \ln(N_A N_D \cdot 10^{-20})$$