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def derivatives_in_spherical_coordinates():
    Print_Function()
    X = (r,th,phi) = symbols('r theta phi')
    curv = [[r*cos(phi)*sin(th),r*sin(phi)*sin(th),r*cos(th)],[1,r,r*sin(th)]]
    (er,eth,ephi,grad) = MV.setup('e_r e_theta e_phi',metric='[1,1,1]',coords=X,curv=curv)
    f = MV('f','scalar',fct=True)
    A = MV('A','vector',fct=True)
    B = MV('B','grade2',fct=True)
    print 'f =',f
    print 'A =',A
    print 'B =',B
    print 'grad*f =',grad*f
    print 'grad|A =',grad|A
    print '-I*(grad^A) =',-MV.I*(grad^A)
    print 'grad^B =',grad^B
    return
```

Code Output:

$$f = f$$
$$A = A^r \boldsymbol{e_r} + A^\theta \boldsymbol{e_\theta} + A^\phi \boldsymbol{e_\phi}$$
$$B = B^{r\theta} \boldsymbol{e_r} \wedge \boldsymbol{e_\theta} + B^{r\phi} \boldsymbol{e_r} \wedge \boldsymbol{e_\phi} + B^{\theta\phi} \boldsymbol{e_\theta} \wedge \boldsymbol{e_\phi}$$
$$\boldsymbol{\nabla} f = \partial_r f \boldsymbol{e_r} + \frac{\partial_\theta f}{r} \boldsymbol{e_\theta} + \frac{\partial_\phi f}{r \sin(\theta)} \boldsymbol{e_\phi}$$
$$\boldsymbol{\nabla} \cdot A = \partial_r A^r + \frac{A^\theta}{r \tan(\theta)} + 2 \frac{A^r}{r} + \frac{\partial_\theta A^\theta}{r} + \frac{\partial_\phi A^\phi}{r \sin(\theta)}$$
$$-I(\boldsymbol{\nabla} \wedge A) = \left( \frac{A^\phi \cos(\theta) + \sin(\theta) \partial_\theta A^\phi - \partial_\phi A^\theta}{r \sin(\theta)} \right) \boldsymbol{e_r} + \left( -\partial_r A^\phi - \frac{A^\phi}{r} + \frac{\partial_\phi A^r}{r \sin(\theta)} \right) \boldsymbol{e_\theta} + \left( \frac{r \partial_r A^\theta + A^\theta - \partial_\theta A^r}{r} \right) \boldsymbol{e_\phi}$$
$$\boldsymbol{\nabla} \wedge B = \left( \partial_r B^{\theta\phi} + 2 \frac{B^{\theta\phi}}{r} - \frac{B^{r\phi}}{r \tan(\theta)} - \frac{\partial_\theta B^{r\phi}}{r} + \frac{\partial_\phi B^{r\theta}}{r \sin(\theta)} \right) \boldsymbol{e_r} \wedge \boldsymbol{e_\theta} \wedge \boldsymbol{e_\phi}$$