```
In[*]:=SetDirectory@NotebookDirectory[];设置目录当前笔记本的目录Import["QLanczos_package.m"];長入
```

#### **Parameters**

```
ln[*]:= \kappa = 0.1;
\eta = 1.5 * 10^-15; (*machine precision*)
\eta \text{List} = \text{Table} [10.^{j}, {j, -13, -1, 0.1}];
| \pm k |
```

#### Model

```
In[*]:= Ham = HeisenbergHam;
```

### Spectrum

## Reference state

```
| In[*]:= φ = φHeisenberg;

φ = Flatten[Conjugate[U].φ];

| 上年

| 上年

| probφ = Abs[φ]^2;

| 上色対値

| In[*]:= pg = probφ[1]

| ER = Total[probφ*Λ];

| ER = ER - Eg

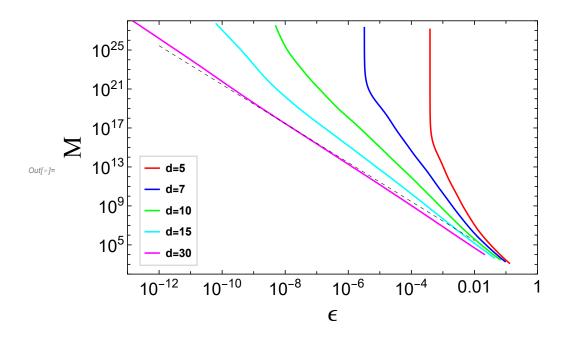
| Out[*]= 0.682614

| Out[*]= 0.119312
```

#### Power

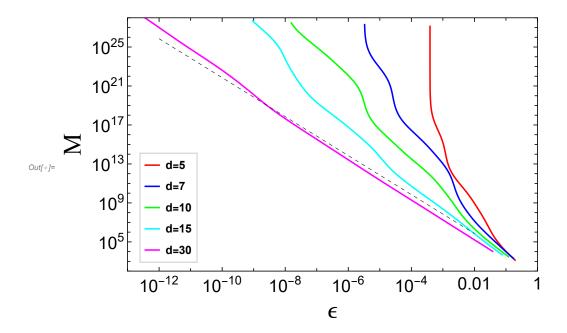
```
In[*]:= dList = {5, 7, 10, 15, 30};
      MListP = {};
       \epsilonListP = {};
      Do [
      Do循环
          d = dList[i];
          Id = IdentityMatrix[d];
                L单位矩阵
          E0 = Eg + 1.;
           {Hmat, Smat} = funMatP[\Lambda, E0, d, prob\varphi];
           \{ \texttt{MList}, \ \epsilon \texttt{List} \} \ = \ \mathsf{funEpsilonM} \ [ \texttt{Hmat}, \ \mathsf{Smat}, \ \mathsf{1.}, \ \mathsf{1.}, \ \mathsf{Id}, \ \eta \texttt{List}, \ \mathsf{Eg}, \ \mathsf{d}, \ \kappa ] \ ;
          AppendTo[MListP, MList];
          AppendTo[eListP, eList];
          , {i, 1, Length[dList]}];
                      长度
```

```
ln[*]:= PR = \{\{10.^-13, 10.^0\}, \{10.^2, 10.^28\}\};
    plotP = ListLogLogPlot | {Transpose[{eListP[1], MListP[1]}}],
           点集的双对数图
       Transpose[{eListP[2], MListP[2]}], Transpose[{eListP[3], MListP[3]]}],
                                          转置
       Transpose[{eListP[[4]], MListP[[4]]}], Transpose[{eListP[[5]], MListP[[5]]}]},
      PlotStyle → {Red, Blue, Green, Cyan, Magenta}, PlotRange → PR, Joined → True,
                  【红色【蓝色】【绿色】【蓝绿色【品红色
                                                 绘制范围
      PlotStyle → {{Thickness[0.004], Red}, {Thickness[0.004], Blue},
                   粗细
                                     红色 粗细
         {Thickness[0.004], Green}, {Thickness[0.004], Cyan}, {Thickness[0.004], Magenta}},
                           上绿色
                                    粗细
                                                     蓝绿色 粗细
      Frame → True, FrameStyle → Directive[Black, Thickness[0.002]],
      | 边框 | 真 | 边框样式
                              指令
                                         黒色 粗细
      FrameTicksStyle \rightarrow Directive[Black, Thickness[0.002]], FrameLabel \rightarrow {"\epsilon", "M"},
      边框刻度样式
                       指令
                                  黑色 粗细
      LabelStyle → {FontSize → 18, FontFamily → "Arial"}, ImageSize → 500,
                   字体大小
                                  字体系列
                                                        图像尺寸
      PlotLegends → Placed[LineLegend[{"d=5", "d=7", "d=10", "d=15", "d=30"},
      上绘图的图例
                   放置
                          线的图例
          LegendFunction → (Framed[#, FrameStyle → LightGray] &), LegendMarkerSize → {16, 8},
                          加边框
                                    边框样式
                                                浅灰色
                                                               图例标记尺寸
          LabelStyle → {Black, Bold, FontSize → 12, FontFamily → "Arial"},
                      字体系列
          LegendMargins \rightarrow 0, LegendLayout \rightarrow {"Column", 1}], {0.1, 0.25}],
                           图例布局
      Epilog → {Dashed, Line[{{Log[10.^-12], Log[10.^24] + FindFit[
      绘制主… 虚线
                      线段  对数
                                           对数
               Transpose[\{Log[\epsilon ListP[5]], Log[MListP[5]]\}], -2 * \epsilon + b, \{b\}, \epsilon][1, 2]\},
                                        对数
                         又寸数
           {Log[10.^-2], Log[10.^4] + FindFit[Transpose[{Log[eListP[5]]}, Log[MListP[5]]}],
                        对数
                                    求拟合  转置
                                                       对数
               -2 * \epsilon + b, \{b\}, \epsilon] [[1, 2]] \} ] \}
```



# **Chebyshev Polynomial**

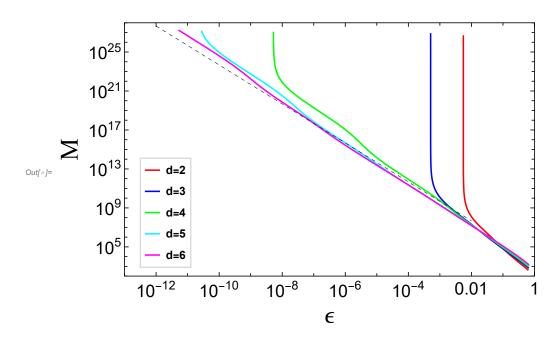
```
In[*]:= plotCP = ListLogLogPlot [{Transpose[{&ListCP[[1]], MListCP[[1]]}}],
            点集的双对数图
       Transpose[{eListCP[[2]], MListCP[[2]]}], Transpose[{eListCP[[3]], MListCP[[3]]}],
       Transpose[{eListCP[[4]], MListCP[[4]]}], Transpose[{eListCP[[5]], MListCP[[5]]}]},
      PlotStyle → {Red, Blue, Green, Cyan, Magenta}, PlotRange → PR, Joined → True,
                 【红色【蓝色】【绿色】 蓝绿色 品红色
                                                 _绘制范围
      PlotStyle → {{Thickness[0.004], Red}, {Thickness[0.004], Blue},
                   粗细
                                      红色 粗细
         {Thickness[0.004], Green}, {Thickness[0.004], Cyan}, {Thickness[0.004], Magenta}},
                           绿色
                                   粗细
                                                     蓝绿色 粗细
      Frame → True, FrameStyle → Directive[Black, Thickness[0.002]],
      | 边框 | 真 | し边框样式 | 指令
                                        黒色 粗细
      FrameTicksStyle \rightarrow Directive[Black, Thickness[0.002]], FrameLabel \rightarrow {"\epsilon", "M"},
      边框刻度样式
                       指令
                                 黒色 粗细
      LabelStyle → {FontSize → 18, FontFamily → "Arial"}, ImageSize → 500,
      标签样式
                   字体大小
                                 上字体系列
      PlotLegends → Placed[LineLegend[{"d=5", "d=7", "d=10", "d=15", "d=30"},
      绘图的图例
                  放置
                         线的图例
          LegendFunction \rightarrow (Framed[#, FrameStyle \rightarrow LightGray] &), LegendMarkerSize \rightarrow {16, 8},
                           加边框 边框样式
         图例函数
                                                浅灰色
                                                                图例标记尺寸
          LabelStyle → {Black, Bold, FontSize → 12, FontFamily → "Arial"},
                      【黑色  【粗体 【字体大小    【字体系列
          LegendMargins \rightarrow 0, LegendLayout \rightarrow {"Column", 1}], {0.1, 0.25}],
                           图例布局
                                           列
      Epilog \rightarrow {Dashed, Line[{{Log[10.^-12], Log[10.^24] + FindFit[
      线段   对数
                                             对数
               Transpose[\{Log[\epsilon ListCP[5]], Log[MListCP[5]]\}], -2 * \epsilon + b, \{b\}, \epsilon][1, 2]\},
                         对数
                                           对数
           {Log[10.^-2], Log[10.^4] + FindFit[Transpose[{Log[eListCP[5]]},
                         上对数
                                   Log[MListCP[5]]}], -2 * \epsilon + b, \{b\}, \epsilon][1, 2]]}]]
                 对数
```



#### Gaussian-Power

```
In[ • ]:=
     dList = \{2, 3, 4, 5, 6\};
     MListGP = {};
     \epsilonListGP = {};
     Do [
     Do循环
        d = dList[[i]];
        Id = IdentityMatrix[d];
             上单位矩阵
        E0 = Eg + 1.;
        {Hmat, Smat} = funMatP[\Lambda, E0, d, prob\varphi];
        EB = Hmat[[d, d]] / Smat[[d, d]];
        \epsilon B = EB - Eg;
        \tauMIN = Sqrt[(d - 1) / E];
               平方根
                                自然常数
        \tauMAX = Sqrt[d - 1] / 0.1;
                平方根
        Do[(
        Do循环
           \tau = (\tau MIN + \tau MAX) / 2.;
           {Hmat, Smat} = funMatGP[\Lambda, Eg, \tau, 1, prob\varphi, htot];
           EK = Hmat[[1, 1]] / Smat[[1, 1]];
           err = EK - Eg;
           If [err > \epsilonB, \tauMIN = \tau];
          如果
           If [err < \epsilonB, \tauMAX = \tau];
          如果
         ), {j, 1, 30}];
        \tau = (\tau MIN + \tau MAX) / 2.; Print["\tau_{GP}:", \tau];
                                  上打印
        \delta = RandomReal[\{-0.1, 0.1\}];
            E0 = Eg + \delta;
        {Hmat, Smat} = funMatGP[\Lambda, E0, \tau, d, prob\varphi, htot];
        {MList, \inList} = funEpsilonM[Hmat, Smat, htot, 1., Id, \etaList, Eg, d, \kappa];
        AppendTo[MListGP, MList];
        附加
        AppendTo[eListGP, eList];
        , {i, 1, Length[dList]}];
                 长度
```

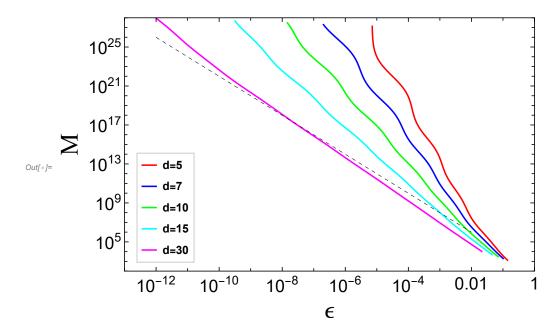
```
\tau_{GP}:2.56034
    τ<sub>GP</sub>:3.9666
    τ<sub>GP</sub>:5.24256
    \tau_{GP}:6.34638
    \tau_{GP}:7.26576
In[*]:= plotGP = ListLogLogPlot [{Transpose[{eListGP[[1]], MListGP[[1]]}}],
            点集的双对数图
                             转置
       Transpose[{eListGP[[2]], MListGP[[2]]}], Transpose[{eListGP[[3]], MListGP[[3]]}],
       Transpose[{eListGP[4], MListGP[4]}], Transpose[{eListGP[5], MListGP[5]}]},
       转置
                                             转置
       PlotStyle → {Red, Blue, Green, Cyan, Magenta}, PlotRange → PR, Joined → True,
                 【红色【蓝色】【绿色】【蓝绿色【品红色】
                                                  上绘制范围
      PlotStyle → {{Thickness[0.004], Red}, {Thickness[0.004], Blue},
      绘图样式
                   粗细
                                      红色 粗细
         {Thickness[0.004], Green}, {Thickness[0.004], Cyan}, {Thickness[0.004], Magenta}},
                           绿色
                                    粗细
                                                       蓝绿色 粗细
      Frame → True, FrameStyle → Directive[Black, Thickness[0.002]],
      边框 真
                  | 边框样式 | 指令
                                          黑色 粗细
      FrameTicksStyle \rightarrow Directive[Black, Thickness[0.002]], FrameLabel \rightarrow {"\epsilon", "M"},
                                  黒色 粗细
                      指令
      LabelStyle → {FontSize → 18, FontFamily → "Arial"}, ImageSize → 500,
                   上字体大小 上字体系列
                                                         图像尺寸
      PlotLegends → Placed[LineLegend[{"d=2", "d=3", "d=4", "d=5", "d=6"},
                   放置  线的图例
          LegendFunction → (Framed[#, FrameStyle → LightGray] &), LegendMarkerSize → {16, 8},
          图例函数
                           加边框
                                     边框样式
                                                  浅灰色
                                                                 图例标记尺寸
          LabelStyle → {Black, Bold, FontSize → 12, FontFamily → "Arial"},
                      黑色 粗体 字体大小
                                                 字体系列
          LegendMargins \rightarrow 0, LegendLayout \rightarrow {"Column", 1}], {0.1, 0.25}],
                            图例布局
                                             囫
      Epilog \rightarrow {Dashed, Line[{{Log[10.^-12], Log[10.^24] + FindFit[
              虚线
                      线段  对数
                                              对数
               Transpose[\{Log[\epsilon ListGP[5]], Log[MListGP[5]]\}], -2*\epsilon+b, \{b\}, \epsilon][1, 2]]\},
               转置
                                            对数
                          」对数
           [Log[10.^-2], Log[10.^4] + FindFit[Transpose[[Log[eListGP[5]]]]]
                        对数
                                    求拟合
转置
                  Log[MListGP[5]]}], -2 * \epsilon + b, \{b\}, \epsilon][1, 2]}}]}
                  对数
```



### **Inverse Power**

```
In[*]:= dList = {5, 7, 10, 15, 30};
      MListIP = {};
       \epsilonListIP = {};
      Do [
      Do循环
          d = dList[[i]];
          Id = IdentityMatrix[d];
                单位矩阵
          E0 = Eg - 1.;
          {Hmat, Smat} = funMatIP[\Lambda, E0, d, prob\varphi];
          \{ \texttt{MList}, \ \texttt{eList} \} \ = \ \mathsf{funEpsilonM} \ [ \texttt{Hmat}, \ \mathsf{Smat}, \ \mathsf{1.}, \ \mathsf{1.}, \ \mathsf{Id}, \ \eta \\ \mathsf{List}, \ \mathsf{Eg}, \ \mathsf{d}, \ \kappa ] \ ;
          AppendTo[MListIP, MList];
          附加
          AppendTo[&ListIP, &List];
         附加
          , {i, 1, Length[dList]}];
```

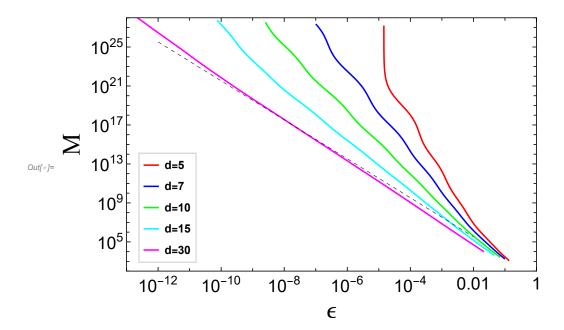
```
In[*]:= plotIP = ListLogLogPlot [{Transpose[{&ListIP[[1]], MListIP[[1]]}}],
             点集的双对数图
        Transpose[{eListIP[[2]], MListIP[[2]]}], Transpose[{eListIP[[3]], MListIP[[3]]}],
        Transpose[{eListIP[[4]], MListIP[[4]]}], Transpose[{eListIP[[5]], MListIP[[5]]}]},
       PlotStyle → {Red, Blue, Green, Cyan, Magenta}, PlotRange → PR, Joined → True,
                   【红色【蓝色】【绿色】 | 蓝绿色 | 品红色
                                                     上绘制范围
       PlotStyle → {{Thickness[0.004], Red}, {Thickness[0.004], Blue},
                    粗细
                                         红色 粗细
         {Thickness[0.004], Green}, {Thickness[0.004], Cyan}, {Thickness[0.004], Magenta}},
                             绿色
                                      粗细
                                                          蓝绿色 粗细
       Frame → True, FrameStyle → Directive[Black, Thickness[0.002]],
       黒色 粗细
       FrameTicksStyle \rightarrow Directive[Black, Thickness[0.002]], FrameLabel \rightarrow {"\epsilon", "M"},
       边框刻度样式
                         指令
                                    黑色 粗细
       LabelStyle → {FontSize → 18, FontFamily → "Arial"}, ImageSize → 500,
       标签样式
                     字体大小
                                    字体系列
                                                            图像尺寸
       PlotLegends → Placed[LineLegend[{"d=5", "d=7", "d=10", "d=15", "d=30"},
       绘图的图例
                    放置
                           线的图例
          \label{legendFunction} \textbf{LegendFunction} \ \rightarrow \ (\texttt{Framed} \ [\#, \ \texttt{FrameStyle} \ \rightarrow \ \texttt{LightGray}] \ \&) \ , \ \texttt{LegendMarkerSize} \ \rightarrow \ \{\texttt{16}, \ 8\} \ ,
          图例函数
                             加边框 边框样式
                                                    浅灰色
                                                                     图例标记尺寸
          LabelStyle \rightarrow {Black, Bold, FontSize \rightarrow 12, FontFamily \rightarrow "Arial"},
                       【黑色  【粗体 【字体大小    【字体系列
          LegendMargins \rightarrow 0, LegendLayout \rightarrow {"Column", 1}], {0.1, 0.25}],
                             图例布局
                                               列
       Epilog \rightarrow {Dashed, Line[{{Log[10.^-12], Log[10.^24] + FindFit[
                                                对数
       线段   对数
                Transpose[\{Log[\epsilon ListIP[5]], Log[MListIP[5]]\}], -2 * \epsilon + b, \{b\}, \epsilon][1, 2]\},
                           对数
                                              对数
            {Log[10.^-2], Log[10.^4] + FindFit[Transpose[{Log[eListIP[5]]],
                                       L对数
                   Log[MListIP[5]]]], -2 * \epsilon + b, \{b\}, \epsilon][1, 2]]}]]
                   对数
```



### **Imaginary-time Evolution**

```
In[*]:= dList = {5, 7, 10, 15, 30};
      MListITE = {};
       eListITE = {};
      Do [
      Do循环
          d = dList[i];
          Id = IdentityMatrix[d];
                上单位矩阵
          E0 = Eg + 1.;
          {Hmat, Smat} = funMatP[\Lambda, E0, d, prob\varphi];
          EB = Hmat[[d, d]] / Smat[[d, d]];
          \epsilon B = EB - Eg;
          \tau MIN = 0;
          \tauMAX = 128;
          Do[(
         Do循环
             \tau = (\tau MIN + \tau MAX) / 2.;
              {Hmat, Smat} = funMatITE[\Lambda, Eg, \tau, d, prob\varphi];
             EK = Hmat[[d, d]] / Smat[[d, d]];
             err = EK - Eg;
             If [err > \epsilonB, \tauMIN = \tau];
             If [err < \epsilonB, \tauMAX = \tau];
             如果
            ), {j, 1, 30}];
          \tau = (\tau MIN + \tau MAX) / 2.; Print["\tau_{ITE}:", \tau];
                                          打印
          E0 = Eg;
          {Hmat, Smat} = funMatITE[\Lambda, E0, \tau, d, prob\varphi];
          \{ \texttt{MList}, \ \texttt{eList} \} \ = \ \mathsf{funEpsilonM} \ [ \texttt{Hmat}, \ \mathsf{Smat}, \ \mathsf{1.}, \ \mathsf{1.}, \ \mathsf{Id}, \ \eta \\ \mathsf{List}, \ \mathsf{Eg}, \ \mathsf{d}, \ \kappa ] \ ;
          AppendTo[MListITE, MList];
          附加
          AppendTo[&ListITE, &List];
          , {i, 1, Length[dList]}];
                      长度
       \tau_{\text{ITE}}:1.1768
       \tau_{\text{ITE}}:1.14179
       \tau_{\text{ITE}}:1.1235
       \tau_{\text{ITE}}:1.11794
       \tau_{\text{ITE}}:1.11733
```

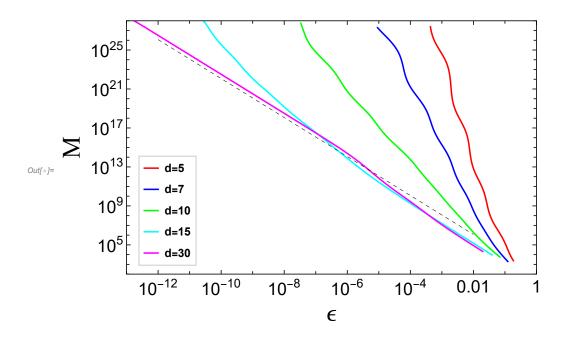
```
In[*]:= plotITE = ListLogLogPlot [{Transpose[{€ListITE[1]], MListITE[1]]}}],
             点集的双对数图
       Transpose[{eListITE[[2]], MListITE[[2]]}], Transpose[{eListITE[[3]], MListITE[[3]]}],
       Transpose[{eListITE[4], MListITE[4]}], Transpose[{eListITE[5], MListITE[5]}]}
                                               转置
       PlotStyle → {Red, Blue, Green, Cyan, Magenta}, PlotRange → PR, Joined → True,
                  【红色【蓝色】【绿色】 | 蓝绿色 | 品红色
                                                  上绘制范围
      PlotStyle → {{Thickness[0.004], Red}, {Thickness[0.004], Blue},
                   粗细
                                      红色 粗细
         {Thickness[0.004], Green}, {Thickness[0.004], Cyan}, {Thickness[0.004], Magenta}},
                           绿色
                                    粗细
                                                      蓝绿色 粗细
      Frame → True, FrameStyle → Directive[Black, Thickness[0.002]],
      | 边框 | 真 | し边框样式 | 指令
                                         黒色 粗细
      FrameTicksStyle \rightarrow Directive[Black, Thickness[0.002]], FrameLabel \rightarrow {"\epsilon", "M"},
      边框刻度样式
                       指令
                                  黑色 粗细
      LabelStyle → {FontSize → 18, FontFamily → "Arial"}, ImageSize → 500,
      标签样式
                   字体大小
                                  字体系列
      PlotLegends → Placed[LineLegend[{"d=5", "d=7", "d=10", "d=15", "d=30"},
      绘图的图例
                   放置
                         线的图例
          LegendFunction \rightarrow (Framed[#, FrameStyle \rightarrow LightGray] &), LegendMarkerSize \rightarrow {16, 8},
         图例函数
                           加边框 边框样式
                                                浅灰色
                                                                图例标记尺寸
          LabelStyle → {Black, Bold, FontSize → 12, FontFamily → "Arial"},
                      【黑色  【粗体 【字体大小    【字体系列
          LegendMargins \rightarrow 0, LegendLayout \rightarrow {"Column", 1}], {0.1, 0.25}],
                            图例布局
                                            列
      Epilog \rightarrow {Dashed, Line[{{Log[10.^-12], Log[10.^24] + FindFit[}
      上线段     对数
                                             对数
               Transpose[\{Log[\epsilon ListITE[\![5]\!]], Log[MListITE[\![5]\!]]\}], -2 * \epsilon + b, \{b\}, \epsilon][\![1, 2]\!]\},
                          对数
                                             对数
           {Log[10.^-2], Log[10.^4] + FindFit[Transpose[{Log[eListITE[5]]],
                         对数
                                     Log[MListITE[[5]]]], -2 * \epsilon + b, \{b\}, \epsilon][[1, 2]]}]]
                 对数
```



### **Real-time Evolution**

```
In[*]:= dList = {5, 7, 10, 15, 30};
    MListRTE = {};
     eListRTE = {};
     Do [
    Do循环
       d = dList[i];
       Id = IdentityMatrix[d];
            单位矩阵
       \Delta tList = Table[((2.*\pi) / 100) j, {j, 1, 100}];
       eList = ConstantArray[0, Length[∆tList]];
               常量数组
                                   长度
       Do[
       LDo循环
        \Delta t = \Delta t List[[j]];
         {Hmat, Smat} = funMatRTE[\Lambda, Eg, \Deltat, d, prob\varphi];
         {EK, cn} = funSubDiag[Hmat + \eta * Id, Smat + \eta * Id];
        err = Abs[EK - Eg];
              _绝对值
        eList[j] = err;
        , {j, 1, Length[∆tList]}];
                 长度
       Δt = ΔtList[Position[εList, Min[εList]][1, 1]]]; Print["Δt:", Δt];
                    位置
                                      最小值
                                                             上打印
       E0 = Eg;
       {Hmat, Smat} = funMatRTE[\Lambda, E0, \Deltat, d, prob\varphi];
       {MList, \epsilonList} = funEpsilonMRTE[Hmat, Smat, 1., 1., Id, \etaList, Eg, d, \kappa];
       AppendTo[MListRTE, MList];
       附加
       AppendTo[eListRTE, eList];
       上附加
       , {i, 1, Length[dList]}];
     ∆t:0.314159
     ∆t:0.753982
     ∆t:1.3823
     ∆t:2.38761
     ∆t:5.65487
```

```
In[*]:= plotRTE = ListLogLogPlot [{Transpose[{&ListRTE[[1]], MListRTE[[1]]}}],
              点集的双对数图
        Transpose[{eListRTE[[2]], MListIP[[2]]}], Transpose[{eListRTE[[3]], MListRTE[[3]]}],
        Transpose[{eListRTE[4], MListRTE[4]}], Transpose[{eListRTE[5], MListRTE[5]}]}
                                                   转置
       PlotStyle → {Red, Blue, Green, Cyan, Magenta}, PlotRange → PR, Joined → True,
                    【红色【蓝色】【绿色】 蓝绿色 品红色
                                                       绘制范围
       PlotStyle → {{Thickness[0.004], Red}, {Thickness[0.004], Blue},
                     粗细
                                          红色 粗细
          {Thickness[0.004], Green}, {Thickness[0.004], Cyan}, {Thickness[0.004], Magenta}},
                              绿色
                                       粗细
                                                           蓝绿色 粗细
       Frame → True, FrameStyle → Directive[Black, Thickness[0.002]],
       | 边框 | 真 | | 边框样式 | 指令 |
                                             黑色 粗细
       FrameTicksStyle \rightarrow Directive[Black, Thickness[0.002]], FrameLabel \rightarrow {"\epsilon", "M"},
       边框刻度样式
                          指令
                                     黑色 粗细
       LabelStyle → {FontSize → 18, FontFamily → "Arial"}, ImageSize → 500,
       标签样式
                     字体大小
                                     字体系列
                                                              图像尺寸
       PlotLegends → Placed[LineLegend[{"d=5", "d=7", "d=10", "d=15", "d=30"},
       绘图的图例
                    放置
                            线的图例
           \label{legendFunction} \textbf{LegendFunction} \ \rightarrow \ (\texttt{Framed} \ [\#, \ \texttt{FrameStyle} \ \rightarrow \ \texttt{LightGray}] \ \&) \ , \ \texttt{LegendMarkerSize} \ \rightarrow \ \{\texttt{16}, \ 8\} \ ,
          图例函数
                             加边框 边框样式
                                                     浅灰色
                                                                      图例标记尺寸
           LabelStyle \rightarrow {Black, Bold, FontSize \rightarrow 12, FontFamily \rightarrow "Arial"},
                        【黑色  【粗体 【字体大小    【字体系列
           LegendMargins \rightarrow 0, LegendLayout \rightarrow {"Column", 1}], {0.1, 0.25}],
                              图例布局
                                                列
       Epilog \rightarrow {Dashed, Line[{{Log[10.^-12], Log[10.^24] + FindFit[}
       上线段     对数
                                                 对数
                 Transpose[\{Log[\epsilon ListRTE[[5]]], Log[MListRTE[[5]]]\}], -2 * \epsilon + b, \{b\}, \epsilon][[1, 2]]\},
                            上对数
                                                 对数
            {Log[10.^-2], Log[10.^4] + FindFit[Transpose[{Log[eListRTE[5]]],
                                         | 求拟合 | 转置
                           上对数
                   Log[MListRTE[[5]]]], -2 * \epsilon + b, \{b\}, \epsilon][[1, 2]]}]]
                   对数
```



## Filter

```
In[*]:= dList = {5, 7, 10, 12, 15};
     MListF = {};
      \epsilonListF = {};
     Do [
     Do循环
        d = dList[[i]];
        Id = IdentityMatrix[d];
              单位矩阵
        E0 = Eg + 1.;
         {Hmat, Smat} = funMatP[\Lambda, E0, d, prob\varphi];
        EB = Hmat[[d, d]] / Smat[[d, d]];
        \epsilon B = EB - Eg;
         \tau MIN = 0;
         \tauMAX = 1024;
        Do[(
        LDo循环
            \tau = (\tau MIN + \tau MAX) / 2.;
            {Hmat, Smat} = funMatF[\Lambda, Eg, 0, \tau, 1, prob\varphi];
            EK = Hmat[[1, 1]] / Smat[[1, 1]];
            err = EK - Eg;
            If [err > \epsilonB, \tauMIN = \tau];
            If [err < \epsilonB, \tauMAX = \tau];
           如果
          ), {j, 1, 30}];
         \tau = (\tau MIN + \tau MAX) / 2.; Print["\tau_F:", \tau];
        \Delta EList = Table[(2. / (d * 100)) * j, {j, 1, 100}];
```

```
eList = ConstantArray[0, Length[∆EList]];
                                  长度
            常量数组
  Do[(
  Do循环
      \Delta E = \Delta E List[[j]];
      {Hmat, Smat} = funMatF[\Lambda, Eg, \DeltaE, \tau, d, prob\varphi];
      {EK, cn} = funSubDiag[Hmat + \eta * Id, Smat + \eta * Id];
      err = EK - Eg;
      eList[j] = err;
    ), {j, 1, Length[∆EList]}];
  \Delta E = \Delta EList[Position[\epsilon List, Min[\epsilon List]][1, 1]]; Print["\Delta E:", \Delta E];
                                       最小值
  E0 = Eg;
   {Hmat, Smat} = funMatF[\Lambda, E0, \DeltaE, \tau, d, prob\varphi];
   {MList, \epsilonList} = funEpsilonM[Hmat, Smat, 1., 1., Id, \etaList, Eg, d, \kappa];
  AppendTo[MListF, MList];
  附加
  AppendTo[&ListF, &List];
  上附加
   , {i, 1, Length[dList]}];
             上长度
\tau_{F}:11.2447
△E:0.02
\tau_{F}:13.7022
\triangle E:0.0485714
\tau_{\text{F}}:15.3563
△E:0.092
\tau_{F}:30.9147
△E:0.055
\tau_{\text{F}}:61.796
△E:0.032
```

```
In[*]:= plotF = ListLogLogPlot [{Transpose[{eListF[[1]], MListF[[1]]}}],
             点集的双对数图
                                | 转置
         \label{listf_2} Transpose[\{\varepsilon Listf[2]\}, MListf[2]\}], Transpose[\{\varepsilon Listf[3]\}, MListf[3]\}],
         Transpose[{eListF[4], MListF[4]}], Transpose[{eListF[5], MListF[5]}]},
        转置
        PlotStyle → {Red, Blue, Green, Cyan, Magenta}, PlotRange → PR, Joined → True,
                     红色 蓝色 绿色 蓝绿色 品红色
                                                          绘制范围
       PlotStyle → {{Thickness[0.004], Red}, {Thickness[0.004], Blue},
                       粗细
                                            红色 粗细
          {Thickness[0.004], Green}, {Thickness[0.004], Cyan}, {Thickness[0.004], Magenta}},
                                绿色
                                          粗细
                                                               蓝绿色 粗细
       Frame → True, FrameStyle → Directive[Black, Thickness[0.002]],
       | 边框 | 真
                    | 边框样式 | 指令
                                                黒色 粗细
       FrameTicksStyle \rightarrow Directive[Black, Thickness[0.002]], FrameLabel \rightarrow {"\epsilon", "M"},
                           指令
                                       黑色
                                              粗细
       LabelStyle → {FontSize → 18, FontFamily → "Arial"}, ImageSize → 500,
       标签样式
                       字体大小
                                       字体系列
       PlotLegends → Placed[LineLegend[{"d=5", "d=7", "d=10", "d=12", "d=15"},
       绘图的图例
                       放置
                               线的图例
           \label{legendFunction} \textbf{LegendFunction} \ \rightarrow \ (\texttt{Framed} \ [\#, \ \texttt{FrameStyle} \ \rightarrow \ \texttt{LightGray}] \ \&) \ , \ \texttt{LegendMarkerSize} \ \rightarrow \ \{\texttt{16}, \ 8\} \ ,
           图例函数
                               加边框
                                           边框样式
                                                         浅灰色
                                                                          图例标记尺寸
           LabelStyle → {Black, Bold, FontSize → 12, FontFamily → "Arial"},
                         | 黑色 | 粗体 | 字体大小
                                                        字体系列
           LegendMargins \rightarrow 0, LegendLayout \rightarrow {"Column", 1}], {0.1, 0.25}],
                                图例布局
                                                   |列
       Epilog \rightarrow {Dashed, Line[{{Log[10.^-12], Log[10.^24] + FindFit[
                                                    对数
       线段
                                   对数
                  Transpose[\{Log[\epsilon ListF[5]], Log[MListF[5]]\}\}], -2 * \epsilon + b, \{b\}, \epsilon][1, 2]\},
                              对数
                                                 对数
             {Log[10.^-2], Log[10.^4] + FindFit[Transpose[{Log[eListF[5]]}, Log[MListF[5]]}],
                            对数
                                           求拟合
                                                    转置
                                                                  对数
             对数
                  -2∗∈+b, {b}, ∈] [[1, 2]]}}]}
          10<sup>25</sup>
          10^{21}
          10<sup>17</sup>
          10<sup>13</sup>
                       d=5
                       d=7
           10<sup>9</sup>
                       d=10
                       d=12
           10<sup>5</sup>
                             10^{-10}
                                        10^{-8}
                                                   10^{-6}
                                                              10^{-4}
                                                                        0.01
                                                  \epsilon
```

```
In[*]:= path = "scalingP.pdf"; Export[path, plotP];
                          导出
    path = "scalingCP.pdf"; Export[path, plotCP];
                           导出
    path = "scalingGP.pdf"; Export[path, plotGP];
                           上导出
    path = "scalingIP.pdf"; Export[path, plotIP];
    path = "scalingITE.pdf"; Export[path, plotITE];
                            上导出
    path = "scalingRTE.pdf"; Export[path, plotRTE];
                            上导出
    path = "scalingF.pdf"; Export[path, plotF];
                           导出
```