

Programming Practice

2018-12-06

Week 14

Notice

Notice

- Project 3rd Week submission due date has been extended.
→ 12/18(Tue) 14:00
- No further delay allowed after 12/18(Tue) 14:00.

Notice – Final Exam

- The Final exam is on 12/16(SUN) 13:00.

Practice Lecture

Big Integer

- **Big integer** is used for mathematical operation which involves very **big integer** calculations that are outside the limit of all available primitive data types(int, long long etc.).
- Ex) 19573293052938594982738592839102938573293829502,
295739482908593028928573920185763958482910536930293739204
769392850391395827,
684029503920583920395848483920192576739203982938493029375
948398271615285986709356281928358392830932934275930135720
579306096750000126582737772835192835638273592837592837592

Homework Problems

1. Big Integer(Multiplication)

Problem. 1

Big Integer(Multiplication)

Description

Calculate multiplication of two big integers X and Y.
X and Y are 0 or positive integers up to 100 digits.

Input

First line contains a single big integer X.
Second line contains a single big integer Y.

Output

Print the result of $X * Y$.

Sample

[input]

103958275843

92753917599692

[output]

9642537351347673387840356

[input]

98765432123456789

123456789

[output]

12193263114159426750190521

Pro

Big Integer(Multiplication)

Sample

[input]

3957293454019352930438475930201928293849283059

95928374610192837409876543211234568923852810

[output]

37961672889963241232069788195682476578968907926104592006600368240403072276874
9382542545790

[illegible]

999999999988888888877777777766666666655555555544444444443333333332222
222222111111111

[output]

9999999998888888887777777776666666665555555554444444443333333332222
222222111111111000

Big Integer

- You can manage these 'big' numbers with integer array. Separate the 'big' number into single digits, and save each digit in each element.
- Since problem description specifies maximum 100 digits, use an int array of length 100, and save to the right-end of the array for convenience.
- Ex) When value is: 536,849,781,572,327

0	0	0	0	0	0	...	0	0	0	0	0	0	5	3	6	8	4	9	7	8	1	5	7	2	3	2	7
---	---	---	---	---	---	-----	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

Tip) Saving to the right-end of int array

- First, get whole input as a string with %s. (Since problem description specifies maximum 100 digits, use a char array of length 100+).
- Use `strlen` to find out how many digits are in the big integer.
- Start from the right-end of the string (*i.e.* total index - 1). Parse each character to integer, and save each digit as a single element of an int array (of length 100).

0	0	0	0	0	0	...	0	0	0	0	0	0	5	3	6	8	4	9	7	8	1	5	7	2	3	2	7
---	---	---	---	---	---	-----	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

Big Integer (addition)

3	4	8	1	5	7	2	5	9	6	7	1	7	6
---	---	---	---	---	---	---	---	---	---	---	---	---	---

8	1	3	5	9	4	1	7	5	3	9	8	2	7
---	---	---	---	---	---	---	---	---	---	---	---	---	---

+

--	--	--	--	--	--	--	--	--	--	--	--	--	--

Big Integer (addition)

3	4	8	1	5	7	2	5	9	6	7	1	7	6
---	---	---	---	---	---	---	---	---	---	---	---	---	---

8	1	3	5	9	4	1	7	5	3	9	8	2	7
---	---	---	---	---	---	---	---	---	---	---	---	---	---

+

--	--	--	--	--	--	--	--	--	--	--	--	--	--	--

Prepare a sum array (with big enough size)

Big Integer (addition)

3	4	8	1	5	7	2	5	9	6	7	1	7	6
---	---	---	---	---	---	---	---	---	---	---	---	---	---

8	1	3	5	9	4	1	7	5	3	9	8	2	7
---	---	---	---	---	---	---	---	---	---	---	---	---	---

+

														13
--	--	--	--	--	--	--	--	--	--	--	--	--	--	----

Add each decimal place, one by one.

Big Integer (addition)

3	4	8	1	5	7	2	5	9	6	7	1	7	6
---	---	---	---	---	---	---	---	---	---	---	---	---	---

8	1	3	5	9	4	1	7	5	3	9	8	2	7
---	---	---	---	---	---	---	---	---	---	---	---	---	---

+

													9	13
--	--	--	--	--	--	--	--	--	--	--	--	--	---	----

Add each decimal place, one by one.

Big Integer (addition)

3	4	8	1	5	7	2	5	9	6	7	1	7	6
---	---	---	---	---	---	---	---	---	---	---	---	---	---

8	1	3	5	9	4	1	7	5	3	9	8	2	7
---	---	---	---	---	---	---	---	---	---	---	---	---	---

+

												9	9	13
--	--	--	--	--	--	--	--	--	--	--	--	---	---	----

Add each decimal place, one by one.

Big Integer (addition)

3	4	8	1	5	7	2	5	9	6	7	1	7	6
---	---	---	---	---	---	---	---	---	---	---	---	---	---

8	1	3	5	9	4	1	7	5	3	9	8	2	7
---	---	---	---	---	---	---	---	---	---	---	---	---	---

+

	11	5	11	6	14	11	3	12	14	9	16	9	9	13
--	----	---	----	---	----	----	---	----	----	---	----	---	---	----

Add each decimal place, one by one.

Big Integer (addition)

3	4	8	1	5	7	2	5	9	6	7	1	7	6
---	---	---	---	---	---	---	---	---	---	---	---	---	---

8	1	3	5	9	4	1	7	5	3	9	8	2	7
---	---	---	---	---	---	---	---	---	---	---	---	---	---

+

	11	5	11	6	14	11	3	12	14	9	16	9	9	13
--	----	---	----	---	----	----	---	----	----	---	----	---	---	----

Big Integer (addition)

3	4	8	1	5	7	2	5	9	6	7	1	7	6
---	---	---	---	---	---	---	---	---	---	---	---	---	---

8	1	3	5	9	4	1	7	5	3	9	8	2	7
---	---	---	---	---	---	---	---	---	---	---	---	---	---

+

	11	5	11	6	14	11	3	12	14	9	16	9	9	13
--	----	---	----	---	----	----	---	----	----	---	----	---	---	----

For each $s[i]$ (*right-to-left order*):

$s[i] = s[i] \% 10;$

$s[i-1] += s[i] / 10;$

Big Integer (addition)

3	4	8	1	5	7	2	5	9	6	7	1	7	6
---	---	---	---	---	---	---	---	---	---	---	---	---	---

8	1	3	5	9	4	1	7	5	3	9	8	2	7
---	---	---	---	---	---	---	---	---	---	---	---	---	---

+

	11	5	11	6	14	11	3	12	14	9	16	9	10	3
--	----	---	----	---	----	----	---	----	----	---	----	---	----	---

For each $s[i]$ (*right-to-left order*):

$$s[i] = s[i] \% 10;$$
$$s[i-1] += s[i] / 10;$$

Big Integer (addition)

3	4	8	1	5	7	2	5	9	6	7	1	7	6
---	---	---	---	---	---	---	---	---	---	---	---	---	---

8	1	3	5	9	4	1	7	5	3	9	8	2	7
---	---	---	---	---	---	---	---	---	---	---	---	---	---

+

	11	5	11	6	14	11	3	12	14	9	16	10	0	3
--	----	---	----	---	----	----	---	----	----	---	----	----	---	---

For each $s[i]$ (*right-to-left order*):

$s[i] = s[i] \% 10;$

$s[i-1] += s[i] / 10;$

Big Integer (addition)

3	4	8	1	5	7	2	5	9	6	7	1	7	6
---	---	---	---	---	---	---	---	---	---	---	---	---	---

8	1	3	5	9	4	1	7	5	3	9	8	2	7
---	---	---	---	---	---	---	---	---	---	---	---	---	---

+

	11	5	11	6	14	11	3	12	14	9	17	0	0	3
--	----	---	----	---	----	----	---	----	----	---	----	---	---	---

For each $s[i]$ (*right-to-left order*):

$s[i] = s[i] \% 10;$

$s[i-1] += s[i] / 10;$

Big Integer (addition)

3	4	8	1	5	7	2	5	9	6	7	1	7	6
---	---	---	---	---	---	---	---	---	---	---	---	---	---

8	1	3	5	9	4	1	7	5	3	9	8	2	7
---	---	---	---	---	---	---	---	---	---	---	---	---	---

+

	11	5	11	6	14	11	3	12	14	10	7	0	0	3
--	----	---	----	---	----	----	---	----	----	----	---	---	---	---

For each $s[i]$ (*right-to-left order*):

$s[i] = s[i] \% 10;$

$s[i-1] += s[i] / 10;$

Big Integer (addition)

3	4	8	1	5	7	2	5	9	6	7	1	7	6
---	---	---	---	---	---	---	---	---	---	---	---	---	---

8	1	3	5	9	4	1	7	5	3	9	8	2	7
---	---	---	---	---	---	---	---	---	---	---	---	---	---

+

	11	5	11	6	14	11	3	12	15	0	7	0	0	3
--	----	---	----	---	----	----	---	----	----	---	---	---	---	---

For each $s[i]$ (*right-to-left order*):

$s[i] = s[i] \% 10;$

$s[i-1] += s[i] / 10;$

Big Integer (addition)

3	4	8	1	5	7	2	5	9	6	7	1	7	6
---	---	---	---	---	---	---	---	---	---	---	---	---	---

8	1	3	5	9	4	1	7	5	3	9	8	2	7
---	---	---	---	---	---	---	---	---	---	---	---	---	---

+

	11	5	11	6	14	11	3	13	5	0	7	0	0	3
--	----	---	----	---	----	----	---	----	---	---	---	---	---	---

For each $s[i]$ (*right-to-left order*):

$s[i] = s[i] \% 10;$

$s[i-1] += s[i] / 10;$

Big Integer (addition)

3	4	8	1	5	7	2	5	9	6	7	1	7	6
---	---	---	---	---	---	---	---	---	---	---	---	---	---

8	1	3	5	9	4	1	7	5	3	9	8	2	7
---	---	---	---	---	---	---	---	---	---	---	---	---	---

+

1	1	6	1	7	5	1	4	3	5	0	7	0	0	3
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

Completed.

Big Integer (multiplication)

3	4	8	1	5	7	2	5	9	6	7	1	7	6
---	---	---	---	---	---	---	---	---	---	---	---	---	---

8	1	3	5	9	4	1	7	5	3	9	8	2	7
---	---	---	---	---	---	---	---	---	---	---	---	---	---

X

Big Integer (multiplication)

3	4	8	1	5	7	2	5	9	6	7	1	7	6
8	1	3	5	9	4	1	7	5	3	9	8	2	7
X													
<hr/>													
3	4	8	1	5	7	2	5	9	6	7	1	7	6

* 7

Big Integer (multiplication)

3	4	8	1	5	7	2	5	9	6	7	1	7	6
---	---	---	---	---	---	---	---	---	---	---	---	---	---

8	1	3	5	9	4	1	7	5	3	9	8	2	7
---	---	---	---	---	---	---	---	---	---	---	---	---	---

X

3	4	8	1	5	7	2	5	9	6	7	1	7	6
---	---	---	---	---	---	---	---	---	---	---	---	---	---

* 7

3	4	8	1	5	7	2	5	9	6	7	1	7	6
---	---	---	---	---	---	---	---	---	---	---	---	---	---

* 20

Big Integer (multiplication)

3	4	8	1	5	7	2	5	9	6	7	1	7	6
8	1	3	5	9	4	1	7	5	3	9	8	2	7

X

3	4	8	1	5	7	2	5	9	6	7	1	7	6	* 7
3	4	8	1	5	7	2	5	9	6	7	1	7	6	* 20
3	4	8	1	5	7	2	5	9	6	7	1	7	6	* 800

Big Integer (multiplication)

3	4	8	1	5	7	2	5	9	6	7	1	7	6
8	1	3	5	9	4	1	7	5	3	9	8	2	7
X													
<hr/>													
3	4	8	1	5	7	2	5	9	6	7	1	7	6
													* 7
3	4	8	1	5	7	2	5	9	6	7	1	7	6
													* 20
3	4	8	1	5	7	2	5	9	6	7	1	7	6
													* 800
...													
3	4	8	1	5	7	2	5	9	6	7	1	7	6
													* 8000000000000000

Big Integer (multiplication)

3	4	8	1	5	7	2	5	9	6	7	1	7	6	
8	1	3	5	9	4	1	7	5	3	9	8	2	7	
X														
<hr/>														
3	4	8	1	5	7	2	5	9	6	7	1	7	6	* 7
3	4	8	1	5	7	2	5	9	6	7	1	7	6	* 20
3	4	8	1	5	7	2	5	9	6	7	1	7	6	* 800
...														
3	4	8	1	5	7	2	5	9	6	7	1	7	6	* 8000000000000000
+														
<hr/>														
Answer!														

Big Integer (multiplication)

3	4	8	1	5	7	2	5	9	6	7	1	7	6
---	---	---	---	---	---	---	---	---	---	---	---	---	---

8	1	3	5	9	4	1	7	5	3	9	8	2	7
---	---	---	---	---	---	---	---	---	---	---	---	---	---

X

3	4	8	1	5	7	2	5	9	6	7	1	7	6
---	---	---	---	---	---	---	---	---	---	---	---	---	---

* 7

3	4	8	1	5	7	2	5	9	6	7	1	7	6
---	---	---	---	---	---	---	---	---	---	---	---	---	---

* 20

3	4	8	1	5	7	2	5	9	6	7	1	7	6
---	---	---	---	---	---	---	---	---	---	---	---	---	---

* 800

...

3	4	8	1	5	7	2	5	9	6	7	1	7	6
---	---	---	---	---	---	---	---	---	---	---	---	---	---

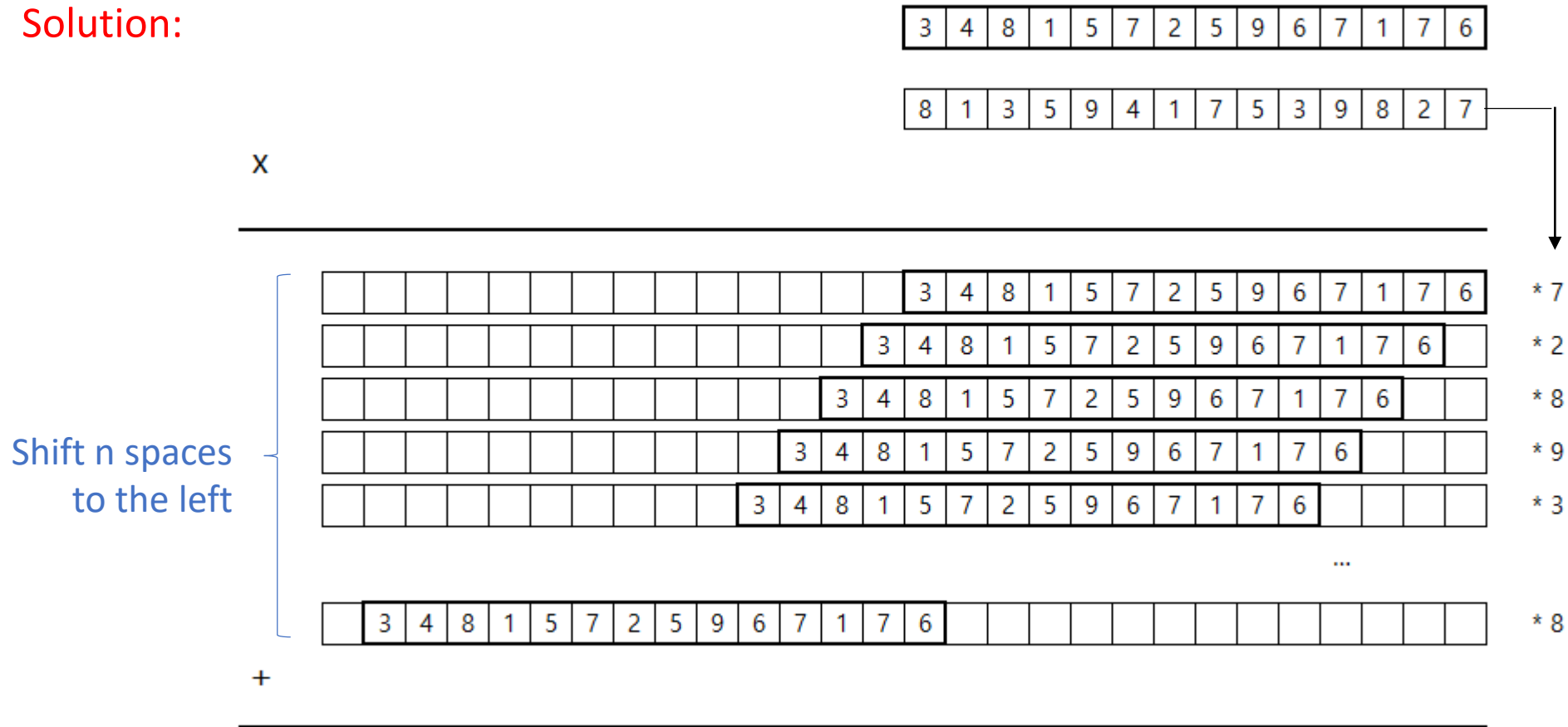
* 8000000000000000

+

Answer!

Big Integer (multiplication)

- Solution:



Answer!

Big Integer (multiplication)

Helpful to pre-define
big enough array length.

array length: a

3	4	8	1	5	7	2	5	9	6	7	1	7	6
---	---	---	---	---	---	---	---	---	---	---	---	---	---

array length: b

8	1	3	5	9	4	1	7	5	3	9	8	2	7
---	---	---	---	---	---	---	---	---	---	---	---	---	---

X

array length: $a+b$

array length: $a+b$

array length: $a+b$

array length: $a+b$

array length: $a+b$

array length: $a+b$

+

*7

* 2

* 8

* 9

* 3

* 8

Answer!