

Resampling
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Required for 231 Students

Homework 4

FSTAT 131/231

Resampling

For this assignment, we will continue working with part of a [Kaggle data set](#) that was the subject of a machine learning competition and is often used for practicing ML models. The goal is classification; specifically, to predict which passengers would survive the [Titanic shipwreck](#).

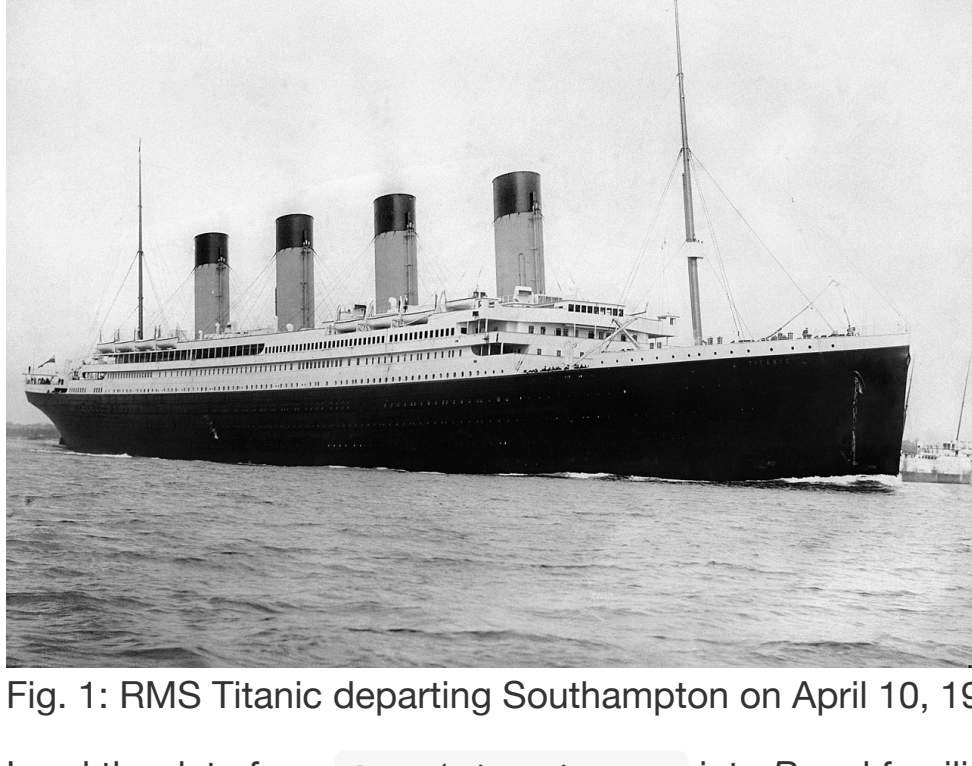


Fig. 1: RMS Titanic departing Southampton on April 10, 1912.

Load the data from `data/titanic.csv` into `R` and familiarize yourself with the variables it contains using the codebook (`data/titanic_codebook.txt`).

Notice that `survived` and `pclass` should be changed to factors. When changing `survived` to a factor, you may want to reorder the factor so that “yes” is the first level.

Make sure you load the `tidyverse` and `tidymodels`!

```
library(ggplot2)
library(tidyverse)
library(tidymodels)
library(corrplot)
library(ggthemes)
library(corr)
library(discrim)
# First, load packages ("pROC")
library(pROC)
library(klar)
tidymodels_prefer()
setwd("~/Users/abbayzope/Desktop/Fstat 131")
Titanic_data<-read.csv("titanic.csv")
Titanic_data$survived<- factor(Titanic_data$survived)
Titanic_data$pclass<- factor(Titanic_data$pclass)
Titanic_data %>%
  head()
```

```
##   passenger_id survived pclass
## 1             1       No      3
## 2             2       Yes      1
## 3             3       Yes      3
## 4             4       Yes      1
## 5             5       No      3
## 6             6       No      3

##              name sex age sib_sp parch
## 1 Braund, Mr. Owen Harris male 22 1 0
## 2 Cumings, Mrs. John Bradley (Florence Briggs Thayer) female 38 1 0
## 3 Heikkinen, Miss. Laina female 26 0 0
## 4 Futrelle, Mrs. Jacques Heath (Lily May Peel) female 35 1 0
## 5 Allen, Mr. William Henry male 35 0 0
## 6 Moran, Mr. James male NA 0 0

##   ticket fare cabin embarked
## 1 A/5 21171 7.2500 <NA> S
## 2 PC 17599 71.2833 C85 C
## 3 STON/O2. 3101282 7.9250 <NA> S
## 4 113803 53.1000 C123 S
## 5 373450 8.0500 <NA> S
## 6 330877 8.4583 <NA> Q
```

Remember that you'll need to set a seed at the beginning of the document to reproduce your results.

Create a recipe for this dataset **identical** to the recipe you used in Homework 3.

Question 1

Split the data, stratifying on the outcome variable, `survived`. You should choose the proportions to split the data into. Verify that the training and testing data sets have the appropriate number of observations.

```
set.seed(3435)

titanic_split <- initial_split(Titanic_data, prop = 0.80,
                               strata = survived)
titanic_train <- training(titanic_split)
titanic_test <- testing(titanic_split)

titanic_train %>%
  head()
```

```
##   passenger_id survived pclass              name sex age
## 1             1       No      3 Braund, Mr. Owen Harris male 22
## 5             5       No      3 Allen, Mr. William Henry male 35
## 7             7       No      1 McCarthy, Mr. Timothy J male 54
## 8             8       No      3 Palsson, Master. Gosta Leonard male 2
## 14            14       No      3 Andersson, Mr. Anders Johan male 39
## 15            15       No      3 Vestrom, Miss. Hulda Amanda Adolfina female 14
##   sib_sp parch ticket fare cabin embarked
## 1      1      0 A/5 21171 7.2500 <NA> S
## 5      0      0 373450 8.0500 <NA> S
## 7      0      0 17463 51.8625 E46 S
## 8      3      1 349909 21.0750 <NA> S
## 14     1      5 347082 31.2750 <NA> S
## 15     0      0 350406 7.8542 <NA> S
```

```
dim(titanic_train)
```

```
## [1] 712 12
```

```
dim(titanic_test)
```

```
## [1] 179 12
```

```
titanic_recipe <- recipe(survived ~ pclass + sex + age + sib_sp + parch
                          + fare, data = titanic_train) %>%
  step_dummy(all_nominal_predictors()) %>%
  step_impute_linear(age, impute_with = imp_vars(all_predictors())) %>%
  step_interact(terms = ~ sex:fare) %>%
  step_interact(terms = ~ age:fare)
```

Question 2

Fold the **training** data. Use *k*-fold cross-validation, with *k* = 10.

```
titanic_folds <- vfold_cv(titanic_train, v = 10)

titanic_folds
```

```
## # 10-fold cross-validation
## # A tibble: 10 × 2
##   splits id
##   <list> <chr>
## 1 <split [640/72]> Fold01
## 2 <split [640/72]> Fold02
## 3 <split [641/71]> Fold03
## 4 <split [641/71]> Fold04
## 5 <split [641/71]> Fold05
## 6 <split [641/71]> Fold06
## 7 <split [641/71]> Fold07
## 8 <split [641/71]> Fold08
## 9 <split [641/71]> Fold09
## 10 <split [641/71]> Fold10
```

```
degree_grid <- grid_regular(degree(range = c(1, 10)), levels = 10)
degree_grid
```

```
## # A tibble: 10 × 1
##   degree
##   <dbl>
## 1      1
## 2      2
## 3      3
## 4      4
## 5      5
## 6      6
## 7      7
## 8      8
## 9      9
## 10     10
```

Question 3

In your own words, explain what we are doing in Question 2. What is *k*-fold cross-validation? Why should we use it, rather than simply fitting and testing models on the entire training set? If we **did** use the entire training set, what resampling method would that be?

K-fold cross validation is an alternative attempt to evaluate a model on some data. When performing k-fold cross validation, we are essentially dividing our data into folds and ensuring that each fold is used as a testing set at some point. K-fold cross validation ensures every observation from the original dataset has the chance of appearing in the training and test set. This is the key advantage that k-fold cross validation has over the validation set approach which we have been using up until now.

Question 4

Set up workflows for 3 models:

1. A logistic regression with the `glm` engine;
2. A linear discriminant analysis with the `MASS` engine;
3. A quadratic discriminant analysis with the `MASS` engine.

```
log_reg <- logistic_reg() %>%
  set_engine("glm") %>%
  set_mode("classification")

log_wf <- workflow() %>%
  add_model(log_reg) %>%
  add_recipe(titanic_recipe)
```

```
lda_mod <- discrim_linear() %>%
  set_mode("classification") %>%
  set_engine("MASS")

lda_wf <- workflow() %>%
  add_model(lda_mod) %>%
  add_recipe(titanic_recipe)
```

```
qda_mod <- discrim_quad() %>%
  set_mode("classification") %>%
  set_engine("MASS")

qda_wf <- workflow() %>%
  add_model(qda_mod) %>%
  add_recipe(titanic_recipe)
```

How many models, total, across all folds, will you be fitting to the data? To answer, think about how many folds there are, and how many models you'll fit to each fold.

We will be fitting thirty models to the data across all folds.

Question 5

Fit each of the models created in Question 4 to the folded data.

```
tune_res_logistic <- log_wf %>%
  fit_resamples(titanic_folds)

#tune_res_logistic <- tune_grid(
#  object = log_wf,
#  resamples = titanic_folds,
#  grid = degree_grid
#)

tune_res_lda <- lda_wf %>%
  fit_resamples(titanic_folds)

#tune_res_lda <- tune_grid(
#  object = lda_wf,
#  resamples = titanic_folds,
#  grid = degree_grid
#)

tune_res_qda <- qda_wf %>%
  fit_resamples(titanic_folds)

#tune_res_qda <- tune_grid(
#  object = qda_wf,
#  resamples = titanic_folds,
#  grid = degree_grid
#)
```

IMPORTANT: Some models may take a while to run – anywhere from 3 to 10 minutes. You should NOT re-run these models each time you knit. Instead, run them once, using an *R* script, and store your results; look into the use of *loading* and *saving*. You should still include the code to run them when you knit, but set `eval = FALSE` in the code chunks.

Question 6

Use `collect_metrics()` to print the mean and standard errors of the performance metric *accuracy* across all folds for each of the four models.

```
collect_metrics(tune_res_logistic)
```

```
## # A tibble: 2 × 6
##   .metric .estimator mean n std_err .config
##   <chr> <chr> <dbl> <int> <dbl> <chr>
## 1 accuracy binary 0.811 10 0.0155 Preprocessor1_Model11
## 2 roc_auc binary 0.849 10 0.0123 Preprocessor1_Model11
```

```
collect_metrics(tune_res_lda)
```

```
## # A tibble: 2 × 6
##   .metric .estimator mean n std_err .config
##   <chr> <chr> <dbl> <int> <dbl> <chr>
## 1 accuracy binary 0.794 10 0.0174 Preprocessor1_Model11
## 2 roc_auc binary 0.849 10 0.0142 Preprocessor1_Model11
```

```
collect_metrics(tune_res_qda)
```

```
## # A tibble: 2 × 6
##   .metric .estimator mean n std_err .config
##   <chr> <chr> <dbl> <int> <dbl> <chr>
## 1 accuracy binary 0.791 10 0.0174 Preprocessor1_Model11
## 2 roc_auc binary 0.841 10 0.0107 Preprocessor1_Model11
```

Decide which of the 3 fitted models has performed the best. Explain why. (Note: You should consider both the mean accuracy and its standard error).

The Logistic regression model is the best performing model as it has the highest mean and the lowest standard error.

Question 7

Now that you've chosen a model, fit your chosen model to the entire training dataset (not to the folds).

```
new_log_reg <- logistic_reg() %>%
  set_engine("glm") %>%
  set_mode("classification")

new_log_wf <- workflow() %>%
  add_model(new_log_reg) %>%
  add_recipe(titanic_recipe)

new_log_fit <- fit(new_log_wf, titanic_test)
```

Question 8

Finally, with your fitted model, use `predict()`, `bind_cols()`, and `accuracy()` to assess your model's performance on the testing data!

Compare your model's testing accuracy to its average accuracy across folds. Describe what you see.

```
log_modelpredict <- predict(new_log_fit, new_data = titanic_test, type = "prob")
log_modelaccuracy<- accuracy(new_log_fit, new_data = titanic_train) %>%
  accuracy(truth = survived, estimate = .pred_class)
bind_cols(log_modelpredict, log_modelaccuracy)
```

```
## # A tibble: 179 × 5
##   .pred.No .pred.Yes .metric .estimator .estimate
##   <dbl> <dbl> <chr> <chr> <dbl>
## 1 0.932 0.0682 accuracy binary 0.789
## 2 0.267 0.733 accuracy binary 0.789
## 3 0.150 0.850 accuracy binary 0.789
## 4 0.860 0.120 accuracy binary 0.789
## 5 0.273 0.727 accuracy binary 0.789
## 6 0.964 0.0357 accuracy binary 0.789
## 7 0.888 0.112 accuracy binary 0.789
## 8 0.500 0.500 accuracy binary 0.789
## 9 0.054 0.946 accuracy binary 0.789
## 10 0.282 0.718 accuracy binary 0.789
## # = with 169 more rows
```

```
#log_modelaccuracy
#log_modelpredict
```

We see a slight reduction on the model's testing accuracy in relation to its average accuracy across folds as the accuracy rate decreased from 80.4% to 78.9%. However, this is to be expected as most models generally perform slightly worse on testing data. Overall, while the logistic regression model is the most accurate model at our disposal, it still leaves a lot to be desired as approximately 20% of all predictions are incorrect.

Required for 231 Students

Consider the following intercept-only model, with $e \sim N(0, \sigma^2)$:

$$Y = \beta + e$$

where β is the parameter that we want to estimate. Suppose that we have n observations of the response, i.e. y_1, \dots, y_n , with uncorrelated errors.

Question 9

Derive the least-squares estimate of β .

Question 10

Suppose that we perform leave-one-out cross-validation (LOOCV). Recall that, in LOOCV, we divide the data into n folds. What is the covariance between $\hat{\beta}^{(1)}$ or the least-squares estimator of β that we obtain by taking the first fold as a training set, and $\hat{\beta}^{(2)}$, the least-squares estimator of β that we obtain by taking the second fold as a training set?