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PSTAT 131/231

Linear Regression

For this lab, we will be working with a data set from the UCI (University of California, Irvine) Machine Learning repository (see website here). The full data set consists of 4,177 observations of abalone in Tasmania. (Fun fact: Tasmania supplies about 25% of the yearly world abalone harvest.)



Fig 1. Inside of an abalone shell.

The age of an abalone is typically determined by cutting the shell open and counting the number of rings with a microscope. The purpose of this data set is to determine whether abalone age (number of rings + 1.5) can be accurately predicted using other, easier-to-obtain information about the abalone.

The full abalone data set is located in the \data subdirectory. Read it into R using read_csv(). Take a moment to read through the codebook (abalone codebook.txt) and familiarize yourself with the variable definitions. Make sure you load the tidyverse and tidymodels!

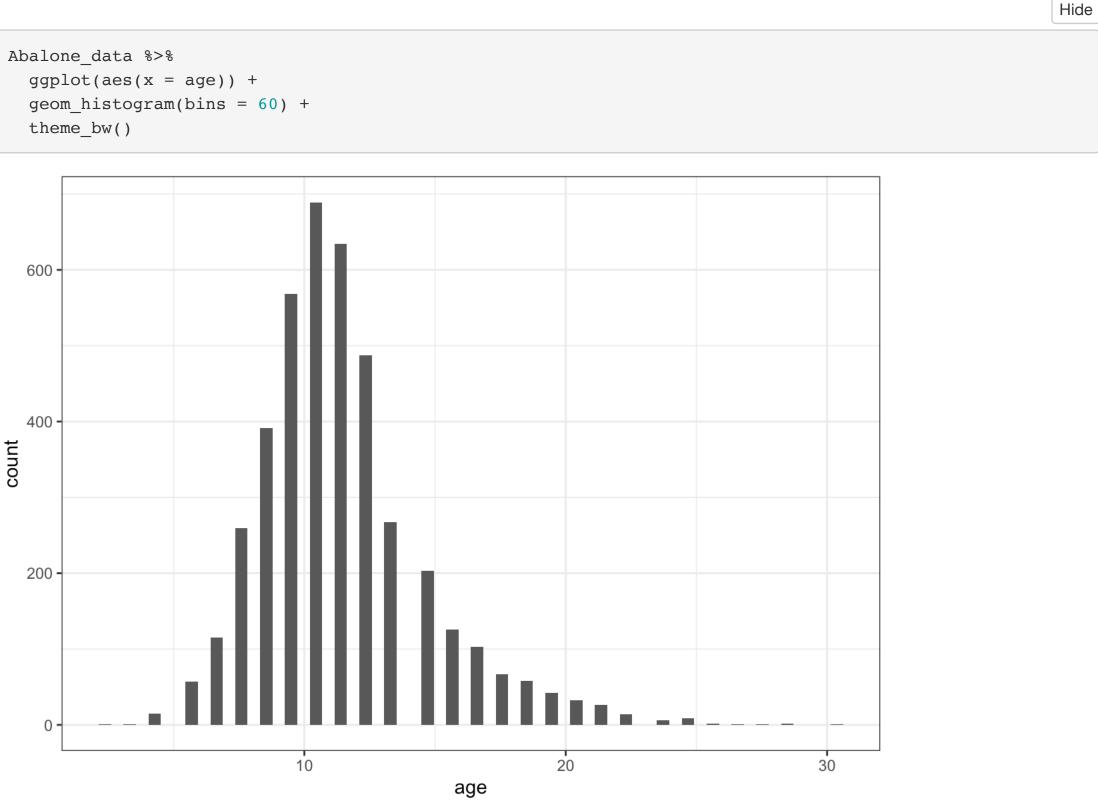
```
library(ggplot2)
library(tidyverse)
library(tidymodels)
library(corrplot)
library(ggthemes)
tidymodels_prefer()
Abalone_data=read.csv("abalone.csv")
Abalone_data %>%
 head()
     type longest_shell diameter height whole_weight shucked_weight viscera_weight
## 1
                  0.455
                                              0.5140
                                                             0.2245
                                                                            0.1010
                          0.365 0.095
                  0.350
                                              0.2255
                                                             0.0995
                                                                            0.0485
                          0.265 0.090
                  0.530
                          0.420 0.135
                                              0.6770
                                                             0.2565
                                                                            0.1415
                  0.440
                                              0.5160
                                                             0.2155
                                                                            0.1140
                          0.365 0.125
## 5
                  0.330
                          0.255 0.080
                                              0.2050
                                                             0.0895
                                                                            0.0395
    shell_weight rings
## 1
           0.150
                    15
## 2
           0.070
                     7
## 3
           0.210
## 4
           0.155
                    10
## 5
           0.055
## 6
           0.120
                      8
```

Question 1

Your goal is to predict abalone age, which is calculated as the number of rings plus 1.5. Notice there currently is no age variable in the data set. Add age to the data set.

```
Hide
Abalone_data$age <- Abalone_data$rings + 1.5
Abalone_data %>%
 head()
    type longest_shell diameter height whole_weight shucked_weight viscera_weight
                          0.365 0.095
## 1
                 0.455
                                              0.5140
                                                             0.2245
                                                                            0.1010
                 0.350
                          0.265 0.090
                                             0.2255
                                                             0.0995
                                                                            0.0485
## 2
                 0.530
                          0.420 0.135
                                             0.6770
                                                             0.2565
                                                                            0.1415
## 3
                                             0.5160
                                                             0.2155
                                                                            0.1140
## 4
                 0.440
                          0.365 0.125
## 5
                 0.330
                          0.255 0.080
                                             0.2050
                                                             0.0895
                                                                            0.0395
                 0.425
                                                             0.1410
                                                                            0.0775
## 6
                          0.300 0.095
                                             0.3515
    shell_weight rings age
## 1
           0.150
                    15 16.5
## 2
           0.070
                     7 8.5
## 3
           0.210
                     9 10.5
## 4
           0.155
                    10 11.5
## 5
           0.055
                     7 8.5
## 6
           0.120
                      8 9.5
```

Assess and describe the distribution of age.



Question 2

Age tends to be very right skewed as the vast majority of datapoints are around the age of 10. After you pass the age of 20, there is

Split the abalone data into a training set and a testing set. Use stratified sampling. You should decide on appropriate percentages for splitting the data.

hardly any data visible anymore.

Remember that you'll need to set a seed at the beginning of the document to reproduce your results.

set.seed(3435)

```
abalone_split <- initial_split(Abalone_data, prop = 0.80,</pre>
                                      strata = age)
 abalone_train <- training(abalone_split)</pre>
 abalone_test <- testing(abalone_split)</pre>
Question 3
Using the training data, create a recipe predicting the outcome variable, age, with all other predictor variables. Note that you
```

should not include rings to predict age. Explain why you shouldn't use rings to predict age. We should not use rings to predict age because rings was actually used to create our variable age in the very beginning.

Steps for your recipe:

1. dummy code any categorical predictors 2. create interactions between

type and shucked_weight, longest_shell and diameter, shucked_weight and shell_weight

3. center all predictors, and 4. scale all predictors.

```
cera_weight + shell_weight, data = abalone_train) %>%
   step_dummy(all_nominal_predictors()) %>%
   step_interact(terms = ~ type:shucked_weight) %>%
   step_interact(terms = ~ longest_shell:diameter) %>%
   step_interact(terms = ~ shucked_weight:shell_weight) %>%
   step_normalize(longest_shell, diameter, height, whole_weight, shucked_weight, viscera_weight, shell_w
 eight)
You'll need to investigate the tidymodels documentation to find the appropriate step functions to use.
Question 4
```

abalone_recipe <- recipe(age ~ longest_shell + diameter + height + whole_weight + shucked_weight + vis

Create and store a linear regression object using the "lm" engine.

lm model <- linear reg() %>%

set_engine("lm")

```
Question 5
Now:
  1. set up an empty workflow,
  2. add the model you created in Question 4, and
```

3. add the recipe that you created in Question 3.

lm wflow <- workflow() %>% add_model(lm_model) %>% add recipe(abalone recipe)

```
Hide
 lm_fit <- fit(lm_wflow, abalone_train)</pre>
Question 6
Use your fit() object to predict the age of a hypothetical female abalone with longest_shell = 0.50, diameter = 0.10, height = 0.30,
whole_weight = 4, shucked_weight = 1, viscera_weight = 2, shell_weight = 1.
                                                                                                                         Hide
```

```
hypo_female <- data.frame(longest_shell = .50, diameter = 0.10, height = 0.30, whole_weight = 4, shucke
d weight = 1, viscera weight = 2, shell weight = 1, type = F)
predict(lm_fit, new_data = hypo_female)
## # A tibble: 1 × 1
    .pred
```

<dbl> ## 1 24.6

#install.packages("yardstick")

standard

library(yardstick)

3 mae

Hints:

Question 7

Now you want to assess your model's performance. To do this, use the yardstick package: 1. Create a metric set that includes R^2 , RMSE (root mean squared error), and MAE (mean absolute error).

2. Use predict() and bind_cols() to create a tibble of your model's predicted values from the training data along with the

3. Finally, apply your metric set to the tibble, report the results, and interpret the R^2 value.

abalone_train_res <- predict(lm_fit, new_data = abalone_train %>% select(-age))

actual observed ages (these are needed to assess your model's performance).

```
abalone_train_res <- bind_cols(abalone_train_res, abalone_train %>% select(age))
abalone_metrics <- metric_set(rmse, rsq, mae)</pre>
abalone_metrics(abalone_train_res, truth = age,
                estimate = .pred)
     .metric .estimator .estimate
    <chr> <chr>
                            <dbl>
## 1 rmse
             standard
                            2.19
             standard
                            0.539
## 2 rsq
```

The R² value tells us the degree to which the variation of your output model can be explained by your input variables. Here, the

A tibble: 3 × 3

value is .539, which means that 53.9% of the variation in age can be explained through the regression model. Required for 231 Students

1.59

In lecture, we presented the general bias-variance tradeoff, which takes the form: $E[(y_0 - \hat{f}(x_0))^2] = Var(\hat{f}(x_0)) + [Bias(\hat{f}(x_0))]^2 + Var(\epsilon)$

```
where the underlying model Y = f(X) + \epsilon satisfies the following:
    • \epsilon is a zero-mean random noise term and X is non-random (all randomness in Y comes from \epsilon);
```

• (x_0, y_0) represents a test observation, independent of the training set, drawn from the same model; • $\hat{f}(.)$ is the estimate of f obtained from the training set.

• reorganize terms in the expected test error by adding and subtracting $E[\hat{f}(x_0)]$

Question 8 Which term(s) in the bias-variance tradeoff above represent the reproducible error? Which term(s) represent the irreducible error?

Question 9 Using the bias-variance tradeoff above, demonstrate that the expected test error is always at least as large as the irreducible error.

Question 10

• use the definition of $Bias(\hat{f}(x_0)) = E[\hat{f}(x_0)] - f(x_0)$;

Prove the bias-variance tradeoff.