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AN Other

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Contents

1 Introduction

A file system has named files so we introduce file name and file content types.

$$[Name, File]$$

$$Path == \text{seq } Name$$

$\frac{FS}{fs : Path \rightarrow File}$

$\frac{\begin{array}{l} CreateFile \\ \Delta FS \\ p? : Path \\ f? : File \end{array}}{p? \notin \text{dom } fs \\ fs' = fs \cup \{p? \mapsto f?\}}$
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$\frac{\begin{array}{l} DeleteFile \\ \Delta FS \\ p? : Path \end{array}}{p? \in \text{dom } fs \\ fs' = \{p?\} \triangleleft fs}$
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2 Z Notation

Numbers:

\mathbb{N} Natural numbers $\{0, 1, \dots\}$

Propositional logic and the schema calculus:

$\dots \wedge \dots$	And	$\langle \dots \rangle$	Free type injection
$\dots \vee \dots$	Or	$[\dots]$	Given sets
$\dots \Rightarrow \dots$	Implies	$', ?, !, 0 \dots 9$	Schema decorations
$\forall \dots \mid \dots \bullet \dots$	For all	$\dots \vdash \dots$	theorem
$\exists \dots \mid \dots \bullet \dots$	There exists	$\theta \dots$	Binding formation
$\dots \setminus \dots$	Hiding	$\lambda \dots$	Function definition
$\dots \hat{=} \dots$	Schema definition	$\mu \dots$	Mu-expression
$\dots == \dots$	Abbreviation	$\Delta \dots$	State change
$\dots ::= \dots \mid \dots$	Free type definition	$\Xi \dots$	Invariant state change

Sets and sequences:

$\{\dots\}$	Set	$\dots \setminus \dots$	Set difference
$\{\dots \mid \dots \bullet \dots\}$	Set comprehension	$\bigcup \dots$	Distributed union
$\mathbb{P} \dots$	Set of subsets of	$\# \dots$	Cardinality
\emptyset	Empty set	$\dots \subseteq \dots$	Subset
$\dots \times \dots$	Cartesian product	$\dots \subset \dots$	Proper subset
$\dots \in \dots$	Set membership	$\dots \text{ partition } \dots$	Set partition
$\dots \notin \dots$	Set non-membership	seq	Sequences
$\dots \cup \dots$	Union	$\langle \dots \rangle$	Sequence
$\dots \cap \dots$	Intersection	$\text{disjoint } \dots$	Disjoint sequence of sets

Functions and relations:

$\dots \leftrightarrow \dots$	Relation	\dots^*	Reflexive-transitive closure
$\dots \Rightarrow \dots$	Partial function	$\dots (\dots)$	Relational image
$\dots \rightarrow \dots$	Total function	$\dots \oplus \dots$	Functional overriding
$\dots \mapsto \dots$	Partial injection	$\dots \triangleleft \dots$	Domain restriction
$\dots \mapsto \dots$	Injection	$\dots \triangleright \dots$	Range restriction
$\text{dom } \dots$	Domain	$\dots \triangleleft \dots$	Domain subtraction
$\text{ran } \dots$	Range	$\dots \triangleright \dots$	Range subtraction
$\dots \mapsto \dots$	maplet		
$\dots \sim \dots$	Relational inverse		

Axiomatic descriptions:

<i>Declarations</i>
<i>Predicates</i>

Schema definitions:

<i>SchemaName</i>
<i>Declaration</i>
<i>Predicates</i>