

# Week 8 Practical Session

David Barron

Hilary Term 2017

## Structural equation models

There are two commonly used packages for doing structural equation modelling in R: `sem` and `lavaan`. I use the latter because I find the models easier to specify. It also includes some utilities to make creating covariance matrices a bit easier. First, enter it as a single string.

```
# input the correlations in lower diagonal form
houghtonLower.cor <- '
1.000
.668 1.000
.635 .599 1.000
.263 .261 .164 1.000
.290 .315 .247 .486 1.000
.207 .245 .231 .251 .449 1.000
-.206 -.182 -.195 -.309 -.266 -.142 1.000
-.280 -.241 -.238 -.344 -.305 -.230 .753 1.000
-.258 -.244 -.185 -.255 -.255 -.215 .554 .587 1.000
.080 .096 .094 -.017 .151 .141 -.074 -.111 .016 1.000
.061 .028 -.035 -.058 -.051 -.003 -.040 -.040 -.018 .284 1.000
.113 .174 .059 .063 .138 .044 -.119 -.073 -.084 .563 .379 1.000 '
```

Then use the function `getCov` to create a correlation matrix, and the function `cor2cov` to convert to a covariance matrix:

```
houghtonFull.cor <-
  getCov(houghtonLower.cor, names = c("wk1", "wk2", "wk3", "hap", "md1", "md2", "pr1", "pr2",
    "app", "bel", "st", "ima"))

houghtonFull.cov <-
  cor2cov(houghtonFull.cor, sds = c(0.939, 1.017, 0.937, 0.562, 0.760, 0.524, 0.585, 0.609,
    0.731, 0.711, 1.124, 1.001))

print(houghtonFull.cov, digits = 1)
```

	wk1	wk2	wk3	hap	md1	md2	pr1	pr2	app	bel	st
wk1	0.88	0.64	0.56	0.139	0.21	0.102	-0.11	-0.16	-0.177	0.053	0.064
wk2	0.64	1.03	0.57	0.149	0.24	0.131	-0.11	-0.15	-0.181	0.069	0.032
wk3	0.56	0.57	0.88	0.086	0.18	0.113	-0.11	-0.14	-0.127	0.063	-0.037
hap	0.14	0.15	0.09	0.316	0.21	0.074	-0.10	-0.12	-0.105	-0.007	-0.037
md1	0.21	0.24	0.18	0.208	0.58	0.179	-0.12	-0.14	-0.142	0.082	-0.044
md2	0.10	0.13	0.11	0.074	0.18	0.275	-0.04	-0.07	-0.082	0.053	-0.002
pr1	-0.11	-0.11	-0.11	-0.102	-0.12	-0.044	0.34	0.27	0.237	-0.031	-0.026
pr2	-0.16	-0.15	-0.14	-0.118	-0.14	-0.073	0.27	0.37	0.261	-0.048	-0.027
app	-0.18	-0.18	-0.13	-0.105	-0.14	-0.082	0.24	0.26	0.534	0.008	-0.015
bel	0.05	0.07	0.06	-0.007	0.08	0.053	-0.03	-0.05	0.008	0.506	0.227
st	0.06	0.03	-0.04	-0.037	-0.04	-0.002	-0.03	-0.03	-0.015	0.227	1.263
ima	0.11	0.18	0.06	0.035	0.10	0.023	-0.07	-0.04	-0.061	0.401	0.426
ima											
wk1	0.11										

```

wk2  0.18
wk3  0.06
hap  0.04
md1  0.10
md2  0.02
pr1 -0.07
pr2 -0.04
app -0.06
bel  0.40
st   0.43
ima  1.00

```

This example comes from a study of job satisfaction among 263 university employees. The hypothesis is that constructive thinking reduces dysfunctional thinking, which leads to an enhanced sense of well-being, which in turn results in greater job satisfaction. The four theoretical constructs are:

1. Constructive (opportunity oriented) thinking
2. Dysfunctional (obstacle oriented) thinking
3. Subjective well-being
4. Job satisfaction

The structural part of the model represents the hypotheses that:

1. Both dysfunctional thinking and subjective well-being have direct effects on job satisfaction
2. Dysfunctional thinking has a direct effect on subjective well-being
3. Constructive thinking has a direct effect on dysfunctional thinking

In the measurement part of the model, each construct has three indicators (see p. 221 of Kline).

```

# specify sr model
houghtonSR.model0 <- '
# measurement part

Construc =~ bel + st + ima
Dysfunc  =~ pr1 + pr2 + app
WellBe   =~ hap + md1 + md2
JobSat   =~ wk1 + wk2 + wk3

# structural part

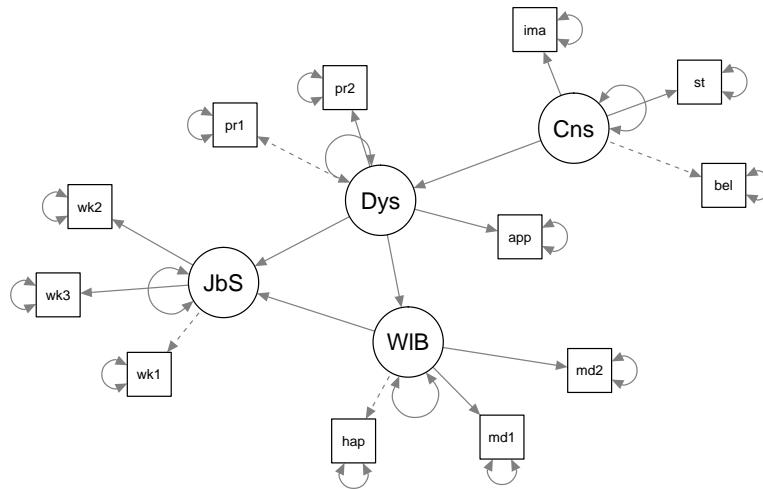
Dysfunc ~ Construc
WellBe  ~ Dysfunc
JobSat  ~ Dysfunc + WellBe '

# fit sr model to data
srmodel0 <- sem(houghtonSR.model0,
               sample.cov = houghtonFull.cov,
               sample.nobs = 263)

```

This is what the model looks like as a diagramme, followed by the results.

```
semPaths(srmodel0, layout = 'spring')
```



```
summary(srmodel0, fit.measures = TRUE)
```

lavaan (0.5-23.1097) converged normally after 43 iterations

Number of observations	263
Estimator	ML
Minimum Function Test Statistic	66.313
Degrees of freedom	50
P-value (Chi-square)	0.061

Model test baseline model:

Minimum Function Test Statistic	1087.490
Degrees of freedom	66
P-value	0.000

User model versus baseline model:

Comparative Fit Index (CFI)	0.984
Tucker-Lewis Index (TLI)	0.979

Loglikelihood and Information Criteria:

Loglikelihood user model (H0)	-3126.092
Loglikelihood unrestricted model (H1)	-3092.936
Number of free parameters	28
Akaike (AIC)	6308.185
Bayesian (BIC)	6408.205
Sample-size adjusted Bayesian (BIC)	6319.432

Root Mean Square Error of Approximation:

RMSEA		0.035
90 Percent Confidence Interval	0.000	0.056
P-value RMSEA <= 0.05		0.866

Standardized Root Mean Square Residual:

SRMR	0.045
------	-------

Parameter Estimates:

Information	Expected
Standard Errors	Standard

Latent Variables:

	Estimate	Std.Err	z-value	P(> z )
Construc =~				
bel	1.000			
st	1.060	0.178	5.941	0.000
ima	1.861	0.331	5.627	0.000
Dysfunc =~				
pr1	1.000			
pr2	1.126	0.080	14.108	0.000
app	0.991	0.089	11.184	0.000
WellBe =~				
hap	1.000			
md1	1.768	0.242	7.305	0.000
md2	0.812	0.125	6.484	0.000
JobSat =~				
wk1	1.000			
wk2	1.031	0.081	12.729	0.000
wk3	0.892	0.073	12.160	0.000

Regressions:

	Estimate	Std.Err	z-value	P(> z )
Dysfunc ~				
Construc	-0.140	0.078	-1.804	0.071
WellBe ~				
Dysfunc	-0.332	0.062	-5.382	0.000
JobSat ~				
Dysfunc	-0.259	0.131	-1.983	0.047
WellBe	0.907	0.220	4.124	0.000

Variances:

	Estimate	Std.Err	z-value	P(> z )
.bel	0.289	0.043	6.669	0.000
.st	1.017	0.097	10.441	0.000
.ima	0.255	0.124	2.061	0.039
.pr1	0.105	0.016	6.702	0.000
.pr2	0.070	0.017	4.092	0.000
.app	0.300	0.029	10.176	0.000
.hap	0.198	0.022	8.912	0.000
.md1	0.212	0.044	4.764	0.000
.md2	0.197	0.020	9.871	0.000
.wk1	0.259	0.042	6.180	0.000

.wk2	0.372	0.050	7.454	0.000
.wk3	0.382	0.044	8.647	0.000
Construc	0.215	0.050	4.263	0.000
.Dysfunc	0.232	0.031	7.600	0.000
.WellBe	0.090	0.020	4.459	0.000
.JobSat	0.471	0.067	7.036	0.000

The implication is that constructive thinking reduces dysfunctional thinking, dysfunctional teaching reduces subjective well-being and job satisfaction, and subjective well-being increases job satisfaction.

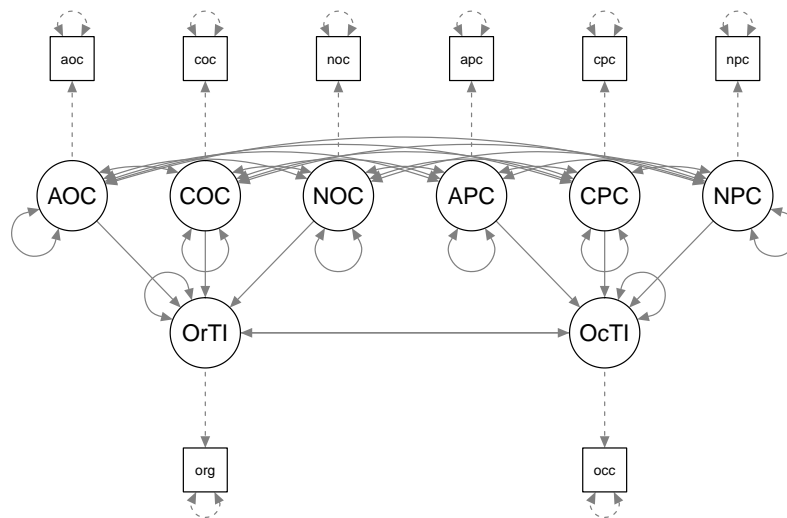
## Single indicator, non-recursive model

This example involves a study of 177 nurses intended to investigate occupational commitment (ie, to the nursing profession), organizational commitment (ie, to the hospital that currently employs them) and turnover intention. There are three types of organizational and occupational commitment: affective (emotional attachment), continuance (perceived cost of leaving) and normative (feeling of obligation to stay), and two types of turnover intention (occupational and organizational). The hypothesis is that the three types of occupational commitment influence occupational turnover intention, the three types of organizational commitment influence organizational turnover intention, and organizational and occupational turnover intention mutually influence each other.

Normally, with only one indicator per factor, we would not be able to estimate error variances, but the original authors also published score reliability coefficients, which we can use to calculate measurement error variance (see p. 222 of Kline).

A diagramme of the model is shown below:

	aoc	coc	noc	apc	cpc	npc	orgti	occti
aoc	1.0816	-0.1019	0.6658	0.5341	0.0649	0.544	-0.7717	-0.7800
coc	-0.1019	0.9604	0.0951	0.0629	0.4434	0.128	-0.0549	-0.0294
noc	0.6658	0.0951	0.9409	0.4359	0.1135	0.465	-0.7876	-0.5820
apc	0.5341	0.0629	0.4359	1.1449	0.1836	0.805	-0.5093	-1.0111
cpc	0.0649	0.4434	0.1135	0.1836	0.6084	0.289	-0.1420	-0.3276
npc	0.5441	0.1282	0.4652	0.8047	0.2891	1.188	-0.5188	-0.9483
orgti	-0.7717	-0.0549	-0.7876	-0.5093	-0.1420	-0.519	1.9600	1.1760
occti	-0.7800	-0.0294	-0.5820	-1.0112	-0.3276	-0.948	1.1760	2.2500



## Results

lavaan (0.5-23.1097) converged normally after 54 iterations

Number of observations	177
Estimator	ML
Minimum Function Test Statistic	9.420
Degrees of freedom	4
P-value (Chi-square)	0.051

Model test baseline model:

Minimum Function Test Statistic	627.135
Degrees of freedom	28
P-value	0.000

User model versus baseline model:

Comparative Fit Index (CFI)	0.991
Tucker-Lewis Index (TLI)	0.937

Loglikelihood and Information Criteria:

Loglikelihood user model (H0)	-1808.897
Loglikelihood unrestricted model (H1)	-1804.187
Number of free parameters	32
Akaike (AIC)	3681.794
Bayesian (BIC)	3783.431
Sample-size adjusted Bayesian (BIC)	3682.093

Root Mean Square Error of Approximation:

RMSEA		0.087
90 Percent Confidence Interval	0.000	0.161
P-value RMSEA <= 0.05		0.159

Standardized Root Mean Square Residual:

SRMR	0.018
------	-------

Parameter Estimates:

Information	Expected
Standard Errors	Standard

Latent Variables:

	Estimate	Std.Err	z-value	P(> z )
AOC =~				
aoc	1.000			
COC =~				
coc	1.000			
NOC =~				
noc	1.000			
APC =~				
apc	1.000			
CPC =~				
cpc	1.000			
NPC =~				
npc	1.000			
OrgTI =~				
orgti	1.000			
OccTI =~				
occti	1.000			

Regressions:

	Estimate	Std.Err	z-value	P(> z )
OrgTI ~				
AOC	0.052	0.376	0.137	0.891
COC	0.044	0.171	0.255	0.799
NOC	-1.162	0.403	-2.882	0.004
OccTI ~				
APC	-0.658	0.184	-3.574	0.000
CPC	-0.102	0.156	-0.649	0.516
NPC	-0.291	0.204	-1.424	0.154
OrgTI ~				
OccTI	0.031	0.141	0.222	0.824
OccTI ~				
OrgTI	0.224	0.119	1.876	0.061

Covariances:

	Estimate	Std.Err	z-value	P(> z )
.OrgTI ~~				
.OccTI	0.274	0.173	1.591	0.112
AOC ~~				
COC	-0.101	0.077	-1.322	0.186

NOC	0.661	0.090	7.319	0.000
APC	0.540	0.092	5.845	0.000
CPC	0.066	0.061	1.084	0.279
NPC	0.546	0.094	5.804	0.000
COC ~~				
NOC	0.092	0.071	1.292	0.196
APC	0.052	0.078	0.663	0.507
CPC	0.439	0.066	6.647	0.000
NPC	0.122	0.080	1.520	0.129
NOC ~~				
APC	0.432	0.084	5.144	0.000
CPC	0.115	0.057	2.027	0.043
NPC	0.458	0.086	5.349	0.000
APC ~~				
CPC	0.187	0.064	2.924	0.003
NPC	0.799	0.106	7.550	0.000
CPC ~~				
NPC	0.290	0.067	4.309	0.000

Variances:

	Estimate	Std.Err	z-value	P(> z )
.aoc	0.195			
.coc	0.288			
.noc	0.245			
.apc	0.160			
.cpc	0.176			
.npc	0.190			
.orgti	0.274			
.occti	0.270			
AOC	0.881	0.114	7.704	0.000
COC	0.667	0.102	6.570	0.000
NOC	0.693	0.100	6.960	0.000
APC	0.977	0.121	8.082	0.000
CPC	0.430	0.064	6.672	0.000
NPC	0.990	0.125	7.892	0.000
.OrgTI	0.753	0.189	3.989	0.000
.OccTI	0.669	0.127	5.271	0.000

	aoc	coc	noc	apc	cpc	npc	orgti	occti
aoc	NA							
coc	NA	NA						
noc	NA	0.514	NA					
apc	NA	2.027	0.293	0.159				
cpc	NA	1.858	-0.429	NA	NA			
npc	NA	1.221	0.403	0.301	NA	0.238		
orgti	-1.113	1.565	0.485	-0.166	-0.798	0.382	NA	
occti	-1.811	2.665	1.876	0.151	-2.064	2.212	NA	0.000

	lhs	op	rhs	mi	epc	sepc.lv	sepc.all	sepc.nox
124	apc	~~	npc	8.54	0.904	0.904	0.780	0.780
59	COC	==	cpc	8.36	9.495	7.755	9.957	9.957
60	COC	==	npc	8.36	3.316	2.709	2.494	2.494
58	COC	==	apc	8.36	1.467	1.198	1.123	1.123
149	OccTI	~	COC	8.36	0.965	0.562	0.562	0.562
62	COC	==	occti	8.36	0.965	0.788	0.527	0.527



61	COC =~ orgti	8.36	-4.306	-3.517	-2.519	-2.519
144	NPC ~~ OccTI	7.99	0.621	0.445	0.445	0.445
22	npc ~~ npc	7.99	2.136	2.136	1.810	1.810
131	npc ~~ occti	7.66	0.603	0.603	0.371	0.371

The largest standardized residual concerns the relationship between occupational turnover intention and continuance organizational commitment. This also has one of the largest modification indices, so try adding that to the model.

```
# respecified model with single indicators
chang.model2 <- '
```

```
#latent variables
```

```
AOC =~ aoc
```

```
COC =~ coc
```

```
NOC =~ noc
```

```
APC =~ apc
```

```
CPC =~ cpc
```

```
NPC =~ npc
```

```
OrgTI =~ orgti
```

```
OccTI =~ occti
```

```
#regressions
```

```
OrgTI ~ AOC + COC + NOC
```

```
OccTI ~ APC + CPC + NPC + COC
```

```
OrgTI ~ OccTI
```

```
OccTI ~ OrgTI
```

```
#fix error variances
```

```
aoc ~~ .1947*aoc
```

```
coc ~~ .2881*coc
```

```
noc ~~ .2446*noc
```

```
apc ~~ .1603*apc
```

```
cpc ~~ .1764*cpc
```

```
npc ~~ .1901*np
```

```
orgti ~~ .2744*orgti
```

```
occti ~~ .2700*occti
```

```
#correlated disturbances
```

```
OrgTI ~~ OccTI '
```

```
# fit respecified model to data
```

```
model2 <- sem(chang.model2,
  sample.cov = changFull.cov,
  sample.nobs = 177)
```

Compare model fits:

```
anova(model1, model2)
```

Chi Square Difference Test

	Df	AIC	BIC	Chisq	Chisq diff	Df diff	Pr(>Chisq)
model2	3	3675	3780	0.81			
model1	4	3682	3783	9.42	8.61	1	0.0033

```
summary(model2, fit.measure = TRUE)
```

lavaan (0.5-23.1097) converged normally after 63 iterations

Number of observations	177
Estimator	ML
Minimum Function Test Statistic	0.809
Degrees of freedom	3
P-value (Chi-square)	0.847

Model test baseline model:

Minimum Function Test Statistic	627.135
Degrees of freedom	28
P-value	0.000

User model versus baseline model:

Comparative Fit Index (CFI)	1.000
Tucker-Lewis Index (TLI)	1.034

Loglikelihood and Information Criteria:

Loglikelihood user model (H0)	-1804.592
Loglikelihood unrestricted model (H1)	-1804.187
Number of free parameters	33
Akaike (AIC)	3675.184
Bayesian (BIC)	3779.997
Sample-size adjusted Bayesian (BIC)	3675.492

Root Mean Square Error of Approximation:

RMSEA	0.000
90 Percent Confidence Interval	0.000 0.070
P-value RMSEA <= 0.05	0.913

Standardized Root Mean Square Residual:

SRMR	0.005
------	-------

Parameter Estimates:

Information	Expected
Standard Errors	Standard

Latent Variables:

	Estimate	Std.Err	z-value	P(> z )
AOC =~				
aoc	1.000			
COC =~				
coc	1.000			
NOC =~				

noc	1.000
APC =~	
apc	1.000
CPC =~	
cpc	1.000
NPC =~	
npc	1.000
OrgTI =~	
orgti	1.000
OccTI =~	
occti	1.000

Regressions:

	Estimate	Std.Err	z-value	P(> z )
OrgTI ~				
AOC	-0.062	0.413	-0.149	0.882
COC	0.030	0.174	0.170	0.865
NOC	-1.033	0.408	-2.534	0.011
OccTI ~				
APC	-0.754	0.231	-3.259	0.001
CPC	-1.441	0.647	-2.226	0.026
NPC	0.094	0.309	0.306	0.760
COC	0.996	0.454	2.195	0.028
OrgTI ~				
OccTI	0.037	0.147	0.250	0.803
OccTI ~				
OrgTI	0.287	0.145	1.982	0.047

Covariances:

	Estimate	Std.Err	z-value	P(> z )
.OrgTI ~~				
.OccTI	0.226	0.178	1.272	0.203
AOC ~~				
COC	-0.104	0.076	-1.362	0.173
NOC	0.661	0.090	7.315	0.000
APC	0.532	0.092	5.768	0.000
CPC	0.067	0.061	1.103	0.270
NPC	0.541	0.094	5.754	0.000
COC ~~				
NOC	0.092	0.071	1.295	0.195
APC	0.063	0.078	0.808	0.419
CPC	0.443	0.066	6.733	0.000
NPC	0.127	0.080	1.587	0.112
NOC ~~				
APC	0.431	0.084	5.136	0.000
CPC	0.116	0.057	2.039	0.041
NPC	0.458	0.086	5.334	0.000
APC ~~				
CPC	0.182	0.064	2.856	0.004
NPC	0.800	0.106	7.556	0.000
CPC ~~				
NPC	0.288	0.067	4.289	0.000

Variances:

	Estimate	Std.Err	z-value	P(> z )
.aoc	0.195			
.coc	0.288			
.noc	0.245			
.apc	0.160			
.cpc	0.176			
.npc	0.190			
.orgti	0.274			
.occti	0.270			
AOC	0.881	0.114	7.704	0.000
COC	0.664	0.101	6.581	0.000
NOC	0.695	0.100	6.963	0.000
APC	0.978	0.121	8.083	0.000
CPC	0.427	0.064	6.670	0.000
NPC	0.991	0.126	7.894	0.000
.OrgTI	0.767	0.192	4.007	0.000
.OccTI	0.461	0.157	2.933	0.003

## Homework

	EdAsp	OcAsp	VerbAch	QuantAch	FamInc	FaEd	MoEd	VerbAb	QuantAb
[1,]	1.024	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
[2,]	0.792	1.077	0.000	0.000	0.000	0.000	0.000	0.000	0.000
[3,]	1.027	0.919	1.844	0.000	0.000	0.000	0.000	0.000	0.000
[4,]	0.756	0.697	1.244	1.286	0.000	0.000	0.000	0.000	0.000
[5,]	0.567	0.537	0.876	0.632	0.852	0.000	0.000	0.000	0.000
[6,]	0.445	0.424	0.677	0.526	0.518	0.670	0.000	0.000	0.000
[7,]	0.434	0.389	0.635	0.498	0.475	0.545	0.716	0.000	0.000
[8,]	0.580	0.564	0.893	0.716	0.546	0.422	0.373	0.851	0.000
[9,]	0.491	0.499	0.888	0.646	0.508	0.389	0.339	0.629	0.871

The model is that a student's achievement (**Achieve**) depends on home and family characteristics (**Home**), the student's ability (**Ability**), and the student's aspiration (**Aspire**). These four latent variable have the following measures:

*Achieve*: Verbal achievement (VerbAch) and Quantitative achievement (QuantAch). *Home*: Family income (FamInc), Father's education (FaEd) and Mother's education (MoEd). *Ability*: Verbal ability (VerbAb) and Quantitative ability (QuantAb). *Aspire*: Educational aspiration (EdAsp) and Occupational aspiration (OcAsp)

The covariance matrix above is based on data from 200 students.

Aspiration is thought to be influenced by Ability and Home situation. Achievement is thought to be influenced by all three latent variables. Specify an appropriate structural equation model, obtain results and determine whether the fit of the model is adequate. If it is not, modify the model and re-fit.

Since we're not having another class, I've included the answers, but try to do it yourself first!

## First SEM

lavaan (0.5-23.1097) converged normally after 43 iterations

Number of observations	200
Estimator	ML

Minimum Function Test Statistic	57.454
Degrees of freedom	21
P-value (Chi-square)	0.000

Parameter Estimates:

Information	Expected
Standard Errors	Standard

Latent Variables:

	Estimate	Std.Err	z-value	P(> z )
Home =~				
FamInc	1.000			
FaEd	1.007	0.073	13.725	0.000
MoEd	0.964	0.076	12.707	0.000
Ability =~				
VerbAb	1.000			
QuantAb	0.949	0.068	14.017	0.000
Aspire =~				
EdAsp	1.000			
OcAsp	0.917	0.064	14.341	0.000
Achieve =~				
VerbAch	1.000			
QuantAch	0.759	0.042	18.206	0.000

Regressions:

	Estimate	Std.Err	z-value	P(> z )
Aspire ~				
Home	0.410	0.125	3.282	0.001
Ability	0.590	0.116	5.081	0.000
Achieve ~				
Home	0.242	0.128	1.901	0.057
Ability	0.751	0.142	5.298	0.000
Aspire	0.548	0.113	4.859	0.000

Covariances:

	Estimate	Std.Err	z-value	P(> z )
Home ~~				
Ability	0.429	0.062	6.877	0.000

Variances:

	Estimate	Std.Err	z-value	P(> z )
.FamInc	0.318	0.039	8.106	0.000
.FaEd	0.129	0.024	5.303	0.000
.MoEd	0.221	0.030	7.394	0.000
.VerbAb	0.187	0.035	5.328	0.000
.QuantAb	0.273	0.038	7.146	0.000
.EdAsp	0.159	0.041	3.854	0.000
.OcAsp	0.349	0.047	7.370	0.000
.VerbAch	0.204	0.051	4.026	0.000
.QuantAch	0.340	0.043	7.866	0.000
Home	0.530	0.082	6.469	0.000
Ability	0.660	0.088	7.518	0.000
.Aspire	0.333	0.058	5.781	0.000

```

        .Achieve          0.224    0.057    3.911    0.000
chisq    df pvalue  rmsea    cfi    srmr
57.454 21.000  0.000  0.093  0.974  0.048

      lhs op      rhs    mi    epc sepc.lv sepc.all sepc.nox
64   FaEd ~~      MoEd 40.38  0.204  0.204   0.296  0.296
49  Achieve =~   FamInc 35.95  0.413  0.527   0.572  0.572
35  Ability =~   FamInc 35.63  0.620  0.504   0.547  0.547
42  Aspire =~   FamInc 23.04  0.401  0.371   0.403  0.403
57  FamInc ~~      MoEd 10.55 -0.098 -0.098  -0.126 -0.126
50  Achieve =~   FaEd 10.04 -0.206 -0.263  -0.322 -0.322
37  Ability =~   MoEd  9.88 -0.298 -0.242  -0.287 -0.287
56  FamInc ~~      FaEd  7.93 -0.090 -0.090  -0.120 -0.120
80  VerbAb ~~ VerbAch 7.71 -0.086 -0.086  -0.069 -0.069
43  Aspire =~   FaEd  7.34 -0.203 -0.188  -0.230 -0.230

      FamInc FaEd    MoEd    VerbAb QuantAb EdAsp  OcAsp  VrbAch QntAch
FamInc    0.000
FaEd      NA  0.000
MoEd      NA  2.173  0.000
VerbAb    3.334 -1.064 -2.835  0.000
QuantAb   2.784 -1.537 -2.994  0.000    NA
EdAsp     2.726 -4.472 -1.170  0.749 -4.728    NA
OcAsp     2.582 -0.616 -1.125  1.610  0.182    NA    NA
VerbAch   3.468    NA -3.416    NA  1.186  0.875 -1.178  0.000
QuantAch  2.290 -0.979 -0.919  1.061 -0.637 -0.951 -0.384  0.000  0.000

```

There are a number of possible modifications that these results suggest. Examples include covariance between father's and mother's education (which seems very plausible). Let's try this out.

lavaan (0.5-23.1097) converged normally after 46 iterations

```

Number of observations                200

Estimator                            ML
Minimum Function Test Statistic      19.265
Degrees of freedom                    20
P-value (Chi-square)                 0.505

```

Parameter Estimates:

```

Information                          Expected
Standard Errors                      Standard

```

Latent Variables:

```

      Estimate Std.Err z-value P(>|z|)
Home =~
  FamInc      1.000
  FaEd        0.782   0.064  12.215   0.000
  MoEd        0.720   0.069  10.398   0.000
Ability =~
  VerbAb      1.000
  QuantAb     0.949   0.067  14.136   0.000
Aspire =~
  EdAsp       1.000

```

OcAsp	0.918	0.064	14.377	0.000
Achieve =~				
VerbAch	1.000			
QuantAch	0.753	0.041	18.180	0.000

Regressions:

	Estimate	Std.Err	z-value	P(> z )
Aspire ~				
Home	0.506	0.153	3.297	0.001
Ability	0.447	0.151	2.968	0.003
Achieve ~				
Home	0.302	0.161	1.879	0.060
Ability	0.685	0.160	4.277	0.000
Aspire	0.526	0.115	4.567	0.000

Covariances:

	Estimate	Std.Err	z-value	P(> z )
Home ~~				
Ability	0.535	0.070	7.656	0.000
.FaEd ~~				
.MoEd	0.172	0.032	5.290	0.000

Variances:

	Estimate	Std.Err	z-value	P(> z )
.FamInc	0.189	0.040	4.755	0.000
.FaEd	0.264	0.034	7.680	0.000
.MoEd	0.371	0.044	8.519	0.000
.VerbAb	0.187	0.035	5.420	0.000
.QuantAb	0.273	0.038	7.213	0.000
.EdAsp	0.160	0.041	3.894	0.000
.OcAsp	0.348	0.047	7.376	0.000
.VerbAch	0.192	0.050	3.817	0.000
.QuantAch	0.347	0.044	7.965	0.000
Home	0.658	0.090	7.337	0.000
Ability	0.659	0.088	7.533	0.000
.Aspire	0.317	0.056	5.621	0.000
.Achieve	0.227	0.057	3.984	0.000

chisq	pvalue	rmsea	cfi	srmr
19.265	0.505	0.000	1.000	0.015

That seems to do the trick. You can see that all the hypothesised structural relationships are statistically significant.