Modus Ponens	$p \longrightarrow q$ p $\therefore q$		Elimination	a. $p \lor q$ $\sim q$ $\therefore p$	b. $p \lor q$ $\sim p$ $\therefore q$
Modus Tollens	$ \begin{array}{c} p \to q \\ \sim q \\ \therefore \sim p \end{array} $		Transitivity	$p \rightarrow q$ $q \rightarrow r$ $\therefore p \rightarrow r$	
Generalization	a. <i>p</i> ∴ <i>p</i> ∨ <i>q</i>	b. q $\therefore p \lor q$	Proof by Division into Cases	$p \lor q$ $p \to r$ $q \to r$	
Specialization	a. $p \wedge q$ $\therefore p$	b. $p \wedge q$ $\therefore q$		∴ r	
Conjunction	p q $\therefore p \wedge q$		Contradiction Rule	$\sim p \to \mathbf{c}$ $\therefore p$	0.2

Theorem 2.1.1 Logical Equivalences

Given any statement variables p, q, and r, a tautology \mathbf{t} and a contradiction \mathbf{c} , the following logical equivalences hold.

nod.						
1.	Commutative laws:	$p \wedge q \equiv q \wedge p$	$p \vee q \equiv q \vee p$			
2.	Associative laws:	$(p \wedge q) \wedge r \equiv p \wedge (q \wedge r)$	$(p\vee q)\vee r\equiv p\vee (q\vee r)$			
3.	Distributive laws:	$p \wedge (q \vee r) \equiv (p \wedge q) \vee (p \wedge r)$	$p\vee (q\wedge r)\equiv (p\vee q)\wedge (p\vee r)$			
4.	Identity laws:	$p \wedge \mathbf{t} \equiv p$	$p \vee \mathbf{c} \equiv p$			
5.	Negation laws:	$p \vee \sim p \equiv \mathbf{t}$	$p \wedge \sim p \equiv \mathbf{c}$			
6.	Double negative law:	$\sim (\sim p) \equiv p$				
7.	Idempotent laws:	$p \wedge p \equiv p$	$p \lor p \equiv p$			
8.	Universal bound laws:	$p \vee \mathbf{t} \equiv \mathbf{t}$	$p \wedge \mathbf{c} \equiv \mathbf{c}$			
9.	De Morgan's laws:	$\sim (p \land q) \equiv \sim p \lor \sim q$	$\sim (p \lor q) \equiv \sim p \land \sim q$			
10.	Absorption laws:	$p \lor (p \land q) \equiv p$	$p \wedge (p \vee q) \equiv p$			
11.	Negations of t and c:	$\sim t \equiv c$	~c ≡ t			

Rule of Inference	Name	
$\therefore \frac{\forall x P(x)}{P(c)}$	Universal instantiation	
$P(c) \text{ for an arbitrary } c$ $\therefore \forall x P(x)$	Universal generalization	
$\therefore \frac{\exists x P(x)}{P(c) \text{ for some element } c}$	Existential instantiation	