# Capita Selecta AI - Probabilistic Programming Inference for SRL

Thierry Deruyttere (r<br/>0660485) & Armin Halilovic (r<br/>0679689) April 1, 2018

## Probabilistic Inference Using Weighted Model Counting

#### 1.1 PGM to CNF

#### 1.1.1 ENC 1

Our ENC1 encoding for the Cancer Bayesian network can be found in appendix 4.1.

#### 1.1.2 ENC 2

Our ENC2 encoding for the Cancer Bayesian network can be found in appendix 4.2.

#### 1.2 SRL to CNF

#### 1.2.1 Encoding of Monty Hall as CNF

An encoding of problog programs can be generated by our program as follows:

python3 scripts/inference.py —problog files/problog/monty\_hall.pl

The CNF will be shown using the program's predicates. A version of the CNF in dimacs format will be shown as well. See README.MD for more information.

```
Our CNF encoding for the given Monty Hall ProbLog program is:
         \land (open\_door(2) \lor prize(2) \lor prize(3) \lor \neg p\_open\_door(2)\_0)
         \land (open\_door(2) \lor prize(2) \lor \neg prize(3))
         \land (\neg open\_door(2) \lor \neg prize(2) \lor \neg prize(2))
         \land (\neg open\_door(2) \lor \neg prize(2) \lor prize(3))
         \land (\neg open\_door(2) \lor \neg prize(3) \lor \neg prize(2))
         \land (\neg open\_door(2) \lor \neg prize(3) \lor prize(3))
         \land (\neg open\_door(2) \lor p\_open\_door(2)\_0 \lor \neg prize(2))
         \land (\neg open\_door(2) \lor p\_open\_door(2) \_0 \lor prize(3))
         \land (open\_door(3) \lor prize(2) \lor prize(3) \lor \neg p\_open\_door(3)\_0)
         \land (open\_door(3) \lor prize(3) \lor \neg prize(2))
         \land (\neg open\_door(3) \lor \neg prize(2) \lor \neg prize(3))
         \land (\neg open\_door(3) \lor \neg prize(2) \lor prize(2))
         \land (\neg open\_door(3) \lor \neg prize(3) \lor \neg prize(3))
         \land (\neg open\_door(3) \lor \neg prize(3) \lor prize(2))
         \land (\neg open\_door(3) \lor p\_open\_door(3)\_0 \lor \neg prize(3))
         \land (\neg open\_door(3) \lor p\_open\_door(3)\_0 \lor prize(2))
         \land (win\_keep \lor \neg prize(1))
         \land (\neg win\_keep \lor prize(1))
         \land (win\_switch \lor \neg prize(2) \lor open\_door(2))
         \land (win\_switch \lor \neg prize(3) \lor open\_door(3))
         \land (\neg win\_switch \lor prize(2) \lor prize(3))
         \land (\neg win\_switch \lor prize(2) \lor \neg open\_door(3))
         \land (\neg win\_switch \lor \neg open\_door(2) \lor prize(3))
         \land (\neg win\_switch \lor \neg open\_door(2) \lor \neg open\_door(3))
         \land (\neg prize(1) \lor \neg prize(2))
         \land (\neg prize(1) \lor \neg prize(3))
         \land (\neg prize(2) \lor \neg prize(3))
         \land (prize(1) \lor prize(2) \lor prize(3))
           Weights:
           W(p\_open\_door(2)\_0) = 0.5
           W(p\_open\_door(3)\_0) = 0.5
           W(select\_door(1)) = 1.00
           W(prize(1)) = 0.33
           W(prize(2)) = 0.33
           W(prize(3)) = 0.33
           W(open\_door(2)) = 1.00
           W(open\_door(3)) = 1.00
           W(win\_keep) = 1.00
           W(win\_switch) = 1.00
```

#### 1.3 Weighted Model Counting

#### 1.3.1 Weighted model counters on above CNFs

We have selected MiniC2D and Cachet as weighted model counters. We have executed the model counters on DIMACS versions of the CNFs. The DIMACS files can be found under report/encodings. The output of the model counters can be found in the listings below.

#### MiniC2D

MiniC2D needs to be executed with the -W flag in order for it to do weighted model counting. The resulting probability can be read next to "Count".

Listing 1.1: MiniC2D on ENC1 encoding of Cancer network

```
Constructing CNF... DONE
CNF stats:
  Vars=30 / Clauses=74
  CNF Time
                  0.000\,\mathrm{s}
Constructing vtree (from primal graph)... DONE
Vtree stats:
  Vtree widths: con \le 5, c_con = 48 v_con = 5
  Vtree Time
                  0.001\,\mathrm{s}
Counting... DONE
  Learned clauses
                            0
Cache stats:
                  75.0\%
  hit rate
  lookups
                  16
  ent count
                  4
  ent memory
                  0.2 KB
  ht memory
                  152.6 MB
  clists
                  1.0 ave, 1 max
                  3.0b ave, 3.0b max, 3.0b min
  kevs
Count stats:
  Count Time
                  0.000 \, s
  \operatorname{Count}
                  0.999999999999999
Total Time: 0.012s
```

Listing 1.2: MiniC2D on ENC2 encoding of Cancer network

```
Constructing CNF... DONE
CNF stats:
  Vars=20 / Clauses=30
  CNF Time
                   0.000 \, \mathrm{s}
Constructing vtree (from primal graph)... DONE
Vtree stats:
  Vtree widths: con \le 6, c_con = 16 v_con = 6
  Vtree Time
                   0.000\,\mathrm{s}
Counting... DONE
  Learned clauses
                            0
Cache stats:
```

```
lookups
                  ^{26}
  ent count
                  20
  ent memory
                  1.0 KB
  ht memory
                  152.6 MB
                  1.0 ave, 1 max
  clists
                  1.8b ave, 3.0b max, 1.0b min
  keys
Count stats:
  Count Time
                  0.000\,\mathrm{s}
  Count
                  1.00000000000000000
Total Time: 0.012s
          Listing 1.3: MiniC2D on CNF encoding of Monty Hall
Constructing CNF... DONE
CNF stats:
  Vars=10 / Clauses=26
  CNF Time
                  0.000\,\mathrm{s}
Constructing vtree (from primal graph)... DONE
Vtree stats:
  Vtree widths: con \le 4, c_con = 22 v_con = 4
  Vtree Time
                  0.000\,\mathrm{s}
Counting ... DONE
  Learned clauses
                           0
Cache stats:
  hit rate
                  20.0\%
  lookups
  ent count
                  4
  ent memory
                  0.2~\mathrm{KB}
                  152.6 MB
  ht memory
  clists
                  1.0 ave, 1 max
                  3.2b ave, 4.0b max, 3.0b min
  keys
Count stats:
  Count Time
                  0.000\,\mathrm{s}
                  1.000000000000000000
  Count
Total Time: 0.011s
```

23.1%

hit rate

#### Cachet

For Cachet, there is no need to use extra parameters to get a probability. It is reported next to "Satisfying probability".

Listing 1.4: Cachet on ENC1 encoding of Cancer network

Number of total components	11
Number of split components	2
Number of non-split components	5
Number of SAT residual formula	12
Number of trivial components	0
Number of changed components	0
Number of adjusted components	0

First component split level	1
Number of Decisions Max Decision Level Number of Variables Original Num Clauses Original Num Literals Added Conflict Clauses Added Conflict Literals Deleted Unrelevant clauses Deleted Unrelevant literals Number of Implications Total Run Time Satisfying probability	$ \begin{array}{c} 11 \\ 5 \\ 30 \\ 74 \\ 172 \\ 0 \\ 0 \\ 0 \\ 0 \\ 124 \\ 0.0163 \\ 8.72319e-08 \end{array} $
Number of solutions	93.6645
Listing 1.5: Cachet on ENC2 encoding of C Number of total components	11
Number of split components Number of non-split components Number of SAT residual formula Number of trivial components Number of changed components Number of adjusted components First component split level	2 5 12 0 0 0 1
Number of Decisions Max Decision Level Number of Variables Original Num Clauses Original Num Literals Added Conflict Clauses Added Conflict Literals Deleted Unrelevant clauses Deleted Unrelevant literals Number of Implications Total Run Time	11 5 20 30 84 0 0 0 0 72 0.017372
Satisfying probability Number of solutions	$^{1}_{1.04858\mathrm{e}+06}$
Listing 1.6: Cachet on WCNF encoding of Number of total components Number of split components Number of non-split components Number of SAT residual formula Number of trivial components Number of changed components	of Monty Hall 4 1 2 5 0 0

Number of adjusted components	0
First component split level	2
Number of Decisions	4
Max Decision Level	4
Number of Variables	10
Original Num Clauses	26
Original Num Literals	73
Added Conflict Clauses	0
Added Conflict Literals	0
Deleted Unrelevant clauses	0
Deleted Unrelevant literals	0
Number of Implications	26
Total Run Time	0.016062
Satisfying probability	0.444444
Number of solutions	455.111

For ENC1, we see that with Cachet reports a satisfying probability of almost 0. Similarly, for Monty Hall, we see that we get a probability of 0.4. This is due to the fact that with ENC1, the weights of negated literals are 1, but Cachet expects that weight(x) + weight(-x) = 1. In the Monty Hall encoding, we also have weights of negated literals equalling 1, which gives the same problem as with ENC1.

#### 1.3.2 Difference between the selected WMCs

#### MiniC2D Vs Cachet

MiniC2D and Cachet are both weighted model counters but how they do this is quite different. MiniC2D is a top down compiler that compiles CNFs into a SDD which results in a faster system but it also uses less space while Cachet is an algorithm that uses formula caching together with clause learning and component analysis. MiniC2D needs vtrees to be able to compile the CNFs into an SDD. TThey, however, both use things from the SAT literature. They both use clause learning and component caching as to be able to reuse components that later appear again in the search. Cachet on the other hand also uses some other things from SAT literature like an explicit on the fly calculation of connected components. This is different in MiniC2D as it uses a vtree to identify disconnected CNF components. [?] [?]

#### 1.3.3 Overview of computational requirements

All the tests can be found in the test folder. We used our scripts to create the dimac files. The input files for our enc1 and enc2 converter ard ".dsc" files which can be found at http://www.bnlearn.com/bnrepository/discrete-small.html#cancer.

#### Test 1: Cancer network

Table 1.1: My caption

	ENC1				ENC2		
	Prob   Memory   Runtime			e Prob Memory Runti			
Minic2d	1.0	0.2 KB	0.155s	1.0	1.0 KB	0.000s	
Cachet	val1	val2	a	b	val3	val4	

Test 2: asia network

Table 1.2: My caption

	ENC1			ption	ENC2	
	Prob   Memory   Runtime			Prob	Runtime	
Minic2d	1.0	0.9 KB	0.145s	1.0	2.0 KB	0.139s
Cachet	val1	val2	a	b	val3	val4

Test 3: sachs network

Table 1.3: My caption

	ENC1			ENC2		
	Prob Memory Runtime			Prob	Memory	Runtime
Minic2d	0.99707	14.3 KB	0.184s	1.0	14.5 KB	0.154s
Cachet	val1	val2	a	b	val3	val4

Test 4: earthquake network

Table 1.4: My caption

	ENC1				$\mathrm{ENC}2$		
	Prob	Memory	Runtime	Prob	Memory	Runtime	
Minic2d	1.0	0.6 KB	0.137s	1.0	1.0 KB	0.153s	
Cachet	val1	val2	a	b	val3	val4	

Test 5: survey network

Table 1.5: My caption

	ENC1				$\mathrm{ENC}2$		
	Prob Memory Runtime			Prob Memory Runt			
Minic2d	1.0	1.6 KB	0.125s	1.0	2.0 KB	0.125s	
Cachet	val1	val2	a	b	val3	val4	

#### Test 6: alarm network

Table 1.6: My caption

	ENC1			ENC2		
	Prob Memory Runtime			Prob	Memory	Runtime
Minic2d	1.0	959.7KB KB	0.268s	1.0	139KB	0.095s
Cachet	val1	val2	a	b	val3	val4

Test 6: andes network

Table 1.7: My caption

	ENC1				ENC2			
	Prob   Memory   Runtime			Prob   Memory   Runtime   Prob   M			Memory	Runtime
Minic2d	1.0	2.7GB	122.78s	1.0	139.8MB	6.086s		
Cachet	val1	val2	a	b	val3	val4		

### 1.4 Knowledge compilation

Vtree with the most compact circuit

During our tests

#### Pattern for a good vtree

As a vtree is a binary tree, which means that a good vtree is compact. We want thus a vtree that is shallow.

## Build an Inference Engine

#### 2.0.1 Implementation

We have implemented the pipeline using python. Information about it can be found in README.MD.

#### 2.0.2 Pipeline with previous tasks

#### Cancer Bayesian network

- Probability:
- Total runtime:
- Runtime of the separate parts:
- Number of variables in CNF:
- Number of lines in CNF:
- Depth of vtree:
- Number of edges and nodes in the circuit:

#### Monty Hall

- Probability:
- Total runtime:
- Runtime of the separate parts:
- Number of variables in CNF:
- Number of lines in CNF:
- Depth of vtree:
- Number of edges and nodes in the circuit:

### 2.0.3 Pipeline on Bayesian learning example

#### DAS NEN DIKKE VETTE TODO

- Probability:
- Total runtime:
- Runtime of the separate parts:
- Number of variables in CNF:
- Number of lines in CNF:
- Depth of vtree:
- Number of edges and nodes in the circuit:

#### 2.0.4 Pipeline on alarm Bayesian network

GOD DAMN IT STOM VAK HOE MOETEN WIJ DIT IN 50 UUR DOEN? PROCESS WORDT GEWOON GEKILLED OMDAT DIE CNF GIGANTISCH GROOT WORDT.

- Probability:
- Total runtime:
- Runtime of the separate parts:
- Number of variables in CNF:
- Number of lines in CNF:
- Depth of vtree:
- Number of edges and nodes in the circuit:

## Parameter Learning

learning

### Appendix

### 4.1 ENC1

#### Indicator clauses:

```
 \begin{array}{l} \left( \neg \ \lambda_{PollutionLow} \lor \neg \ \lambda_{PollutionHigh} \right) \land \left( \lambda_{PollutionLow} \lor \lambda_{PollutionHigh} \right) \land \left( \neg \ \lambda_{SmokerTrue} \lor \neg \ \lambda_{SmokerFalse} \right) \land \left( \lambda_{SmokerTrue} \lor \lambda_{SmokerFalse} \right) \land \left( \neg \ \lambda_{CancerTrue} \lor \neg \ \lambda_{CancerFalse} \right) \land \left( \neg \ \lambda_{XrayPositive} \lor \neg \ \lambda_{XrayNegative} \right) \land \left( \lambda_{XrayPositive} \lor \lambda_{XrayNegative} \right) \land \left( \neg \ \lambda_{DyspnoeaTrue} \lor \neg \ \lambda_{DyspnoeaFalse} \right) \land \left( \lambda_{DyspnoeaTrue} \lor \lambda_{DyspnoeaFalse} \right) \end{aligned}
```

#### Parameter clauses:

```
(\neg \lambda_{PollutionLow} \lor \theta_{PollutionLow}) \land (\lambda_{PollutionLow} \lor \neg \theta_{PollutionLow}) \land (\neg
   \lambda_{PollutionHigh} \vee \theta_{PollutionHigh}) \wedge (\lambda_{PollutionHigh} \vee \neg \theta_{PollutionHigh}) \wedge (\neg \theta_{PollutionHigh})
        \lambda_{SmokerTrue} \vee \theta_{SmokerTrue}) \wedge (\lambda_{SmokerTrue} \vee \neg \theta_{SmokerTrue}) \wedge (\neg
       \lambda_{SmokerFalse} \vee \theta_{SmokerFalse}) \wedge (\lambda_{SmokerFalse} \vee \neg \theta_{SmokerFalse}) \wedge (\neg \theta_{SmokerFalse})
                       \lambda_{PollutionLow} \vee \neg \lambda_{SmokerTrue} \vee \neg \lambda_{CancerTrue} \vee 
                 \theta_{CancerTrue|PollutionLow,SmokerTrue}) \land (\lambda_{PollutionLow} \lor \neg
                 \theta_{CancerTrue|PollutionLow,SmokerTrue}) \land (\lambda_{SmokerTrue} \lor \neg
                  \theta_{CancerTrue|PollutionLow.SmokerTrue}) \wedge (\lambda_{CancerTrue} \vee \neg
 \theta_{CancerTrue|PollutionLow,SmokerTrue}) \land (\neg \lambda_{PollutionLow} \lor \neg \lambda_{SmokerTrue} \lor \neg
    \lambda_{CancerFalse} \lor \theta_{CancerFalse|PollutionLow,SmokerTrue}) \land (\lambda_{PollutionLow} \lor \neg)
                 \theta_{CancerFalse|PollutionLow,SmokerTrue}) \land (\lambda_{SmokerTrue} \lor \neg
                 \theta_{CancerFalse|PollutionLow,SmokerTrue}) \land (\lambda_{CancerFalse} \lor \lnot
\theta_{CancerFalse|PollutionLow,SmokerTrue}) \land (\neg \lambda_{PollutionLow} \lor \neg \lambda_{SmokerFalse} \lor \neg
     \lambda_{CancerTrue} \lor \theta_{CancerTrue|PollutionLow,SmokerFalse}) \land (\lambda_{PollutionLow} \lor \lnot)
                \theta_{CancerTrue|PollutionLow,SmokerFalse}) \land (\lambda_{SmokerFalse} \lor \neg
                 \theta_{CancerTrue|PollutionLow,SmokerFalse}) \land (\lambda_{CancerTrue} \lor \lnot)
\theta_{CancerTrue|PollutionLow,SmokerFalse}) \land (\neg \lambda_{PollutionLow} \lor \neg \lambda_{SmokerFalse} \lor \neg
    \lambda_{CancerFalse} \lor \theta_{CancerFalse|PollutionLow,SmokerFalse}) \land (\lambda_{PollutionLow} \lor \neg)
                \theta_{CancerFalse|PollutionLow,SmokerFalse}) \land (\lambda_{SmokerFalse} \lor \neg
                \theta_{CancerFalse|PollutionLow,SmokerFalse}) \land (\lambda_{CancerFalse} \lor \neg
\theta_{CancerFalse|PollutionLow,SmokerFalse}) \land (\neg \lambda_{PollutionHigh} \lor \neg \lambda_{SmokerTrue} \lor \neg
    \lambda_{CancerTrue} \lor \theta_{CancerTrue|PollutionHigh,SmokerTrue}) \land (\lambda_{PollutionHigh} \lor \lnot)
                 \theta_{CancerTrue|PollutionHigh,SmokerTrue}) \wedge (\lambda_{SmokerTrue} \vee \neg
                 \theta_{CancerTrue|PollutionHigh,SmokerTrue}) \wedge (\lambda_{CancerTrue} \vee \neg
\theta_{CancerTrue|PollutionHigh,SmokerTrue}) \land (\neg \lambda_{PollutionHigh} \lor \neg \lambda_{SmokerTrue} \lor \neg
   \lambda_{CancerFalse} \lor \theta_{CancerFalse|PollutionHigh,SmokerTrue}) \land (\lambda_{PollutionHigh} \lor \neg)
```

```
\theta_{CancerFalse|PollutionHigh,SmokerTrue}) \land (\lambda_{SmokerTrue} \lor \neg
                                                                               \theta_{CancerFalse|PollutionHigh,SmokerTrue}) \land (\lambda_{CancerFalse} \lor \neg
      	heta_{CancerFalse|PollutionHigh,SmokerTrue}) \land (\lnot \lambda_{PollutionHigh} \lor \lnot \lambda_{SmokerFalse} \lor
          \neg \lambda_{CancerTrue} \lor \theta_{CancerTrue|PollutionHigh,SmokerFalse}) \land (\lambda_{PollutionHigh} \lor \neg
                                                                            \theta_{CancerTrue|PollutionHigh,SmokerFalse}) \land (\lambda_{SmokerFalse} \lor \neg
                                                                                  \theta_{CancerTrue|PollutionHigh.SmokerFalse}) \land (\lambda_{CancerTrue} \lor \neg
      \theta_{CancerTrue|PollutionHigh,SmokerFalse}) \land (\neg \lambda_{PollutionHigh} \lor \neg \lambda_{SmokerFalse} \lor 
       \neg \lambda_{CancerFalse} \lor \theta_{CancerFalse|PollutionHigh,SmokerFalse}) \land (\lambda_{PollutionHigh} \lor \neg
                                                                            \theta_{CancerFalse|PollutionHigh,SmokerFalse}) \land (\lambda_{SmokerFalse} \lor \neg
                                                                            \theta_{CancerFalse|PollutionHigh,SmokerFalse}) \land (\lambda_{CancerFalse} \lor \neg)
          \theta_{CancerFalse|PollutionHigh,SmokerFalse}) \land (\neg \lambda_{CancerTrue} \lor \neg \lambda_{XrayPositive} \lor \neg \lambda_{
                         \theta_{XrayPositive|CancerTrue}) \wedge (\lambda_{CancerTrue} \vee \neg \theta_{XrayPositive|CancerTrue}) \wedge 
                                                 (\lambda_{XrayPositive} \lor \neg \theta_{XrayPositive|CancerTrue}) \land (\neg \lambda_{CancerTrue} \lor \neg
                                                               \lambda_{XrayNegative} \lor \theta_{XrayNegative|CancerTrue}) \land (\lambda_{CancerTrue} \lor \neg
\theta_{XrayNegative|CancerTrue}) \wedge (\lambda_{XrayNegative} \vee \neg \theta_{XrayNegative|CancerTrue}) \wedge (\neg
\lambda_{CancerFalse} \lor \lnot \lambda_{XrayPositive} \lor \theta_{XrayPositive|CancerFalse}) \land (\lambda_{CancerFalse} \lor \lnot
  \theta_{XrayPositive|CancerFalse}) \land (\lambda_{XrayPositive} \lor \neg \theta_{XrayPositive|CancerFalse}) \land (\neg \theta_{XrayPositive})
 \lambda_{CancerFalse} \lor \neg \lambda_{XrayNegative} \lor \theta_{XrayNegative|CancerFalse}) \land (\lambda_{CancerFalse} \lor \neg \lambda_{XrayNegative} \lor \neg
\neg \theta_{XrayNegative|CancerFalse}) \land (\lambda_{XrayNegative} \lor \neg \theta_{XrayNegative|CancerFalse}) \land (\lambda_{XrayNegative} \lor \neg \theta_{XrayNegative|CancerFalse}) \land (\lambda_{XrayNegative} \lor \neg \theta_{XrayNegative}) \land (\lambda_{XrayNega
  (\neg \lambda_{CancerTrue} \lor \neg \lambda_{DyspnoeaTrue} \lor \theta_{DyspnoeaTrue} | CancerTrue) \land (\lambda_{CancerTrue})
 \vee \neg \theta_{DyspnoeaTrue|CancerTrue}) \wedge (\lambda_{DyspnoeaTrue} \vee \neg \theta_{DyspnoeaTrue|CancerTrue})
                                       \wedge \left( \neg \ \lambda_{CancerTrue} \lor \neg \ \lambda_{DyspnoeaFalse} \lor \ \theta_{DyspnoeaFalse|CancerTrue} \right) \land \\
                                             (\lambda_{CancerTrue} \vee \neg \ \theta_{DyspnoeaFalse|CancerTrue}) \wedge (\lambda_{DyspnoeaFalse} \vee \neg
                                                 \theta_{DyspnoeaFalse|CancerTrue}) \wedge (\neg \lambda_{CancerFalse} \vee \neg \lambda_{DyspnoeaTrue} \vee 
          \theta_{DyspnoeaTrue|CancerFalse}) \wedge (\lambda_{CancerFalse} \vee \neg \theta_{DyspnoeaTrue|CancerFalse}) \wedge (\lambda_{CancerFalse}) \wedge
                                      (\lambda_{DyspnoeaTrue} \lor \neg \theta_{DyspnoeaTrue|CancerFalse}) \land (\neg \lambda_{CancerFalse} \lor \neg
                                                      \lambda_{DyspnoeaFalse} \lor \theta_{DyspnoeaFalse|CancerFalse}) \land (\lambda_{CancerFalse} \lor \lnot)
       \theta_{DyspnoeaFalse|CancerFalse}) \wedge (\lambda_{DyspnoeaFalse} \vee \neg \theta_{DyspnoeaFalse|CancerFalse})
Weights:
```

 $W(\lambda_{PollutionLow}) = 1.00$  $W(\neg \lambda_{PollutionLow}) = 1.00$  $W(\lambda_{PollutionHigh}) = 1.00$  $W(\neg \lambda_{PollutionHigh}) = 1.00$  $W(\lambda_{SmokerTrue}) = 1.00$  $W(\neg \lambda_{SmokerTrue}) = 1.00$  $W(\lambda_{SmokerFalse}) = 1.00$  $W(\neg \lambda_{SmokerFalse}) = 1.00$  $W(\lambda_{CancerTrue}) = 1.00$  $W(\neg \lambda_{CancerTrue}) = 1.00$  $W(\lambda_{CancerFalse}) = 1.00$  $W(\neg \lambda_{CancerFalse}) = 1.00$  $W(\lambda_{XrayPositive}) = 1.00$  $W(\neg \lambda_{XrayPositive}) = 1.00$  $W(\lambda_{XrayNegative}) = 1.00$  $W(\neg \lambda_{XrayNegative}) = 1.00$  $W(\lambda_{DyspnoeaTrue}) = 1.00$  $W(\neg \lambda_{DyspnoeaTrue}) = 1.00$  $W(\lambda_{DyspnoeaFalse}) = 1.00$  $W(\neg \lambda_{DyspnoeaFalse}) = 1.00$ 

```
W(\theta_{PollutionLow}) = 0.90
W(\neg \theta_{PollutionLow}) = 1.00
W(\theta_{PollutionHigh}) = 0.10
W(\neg \theta_{PollutionHigh}) = 1.00
W(\theta_{SmokerTrue}) = 0.30
W(\neg \theta_{SmokerTrue}) = 1.00
W(\theta_{SmokerFalse}) = 0.70
W(\neg \theta_{SmokerFalse}) = 1.00
W(\theta_{CancerTrue|PollutionLow,SmokerTrue}) = 0.03
W(\neg \theta_{CancerTrue|PollutionLow,SmokerTrue}) = 1.00
W(\theta_{CancerFalse|PollutionLow,SmokerTrue}) = 0.97
W(\neg \theta_{CancerFalse|PollutionLow,SmokerTrue}) = 1.00
W(\theta_{CancerTrue|PollutionLow,SmokerFalse}) = 0.00
W(\neg \theta_{CancerTrue|PollutionLow,SmokerFalse}) = 1.00
W(\theta_{CancerFalse|PollutionLow,SmokerFalse}) = 1.00
W(\neg \theta_{CancerFalse|PollutionLow,SmokerFalse}) = 1.00
W(\theta_{CancerTrue|PollutionHigh,SmokerTrue}) = 0.05
W(\neg \theta_{CancerTrue|PollutionHigh,SmokerTrue}) = 1.00
W(\theta_{CancerFalse|PollutionHigh,SmokerTrue}) = 0.95
W(\neg \theta_{CancerFalse|PollutionHigh,SmokerTrue}) = 1.00
W(\theta_{CancerTrue|PollutionHigh,SmokerFalse}) = 0.02
W(\neg \theta_{CancerTrue|PollutionHigh,SmokerFalse}) = 1.00
W(\theta_{CancerFalse|PollutionHigh,SmokerFalse}) = 0.98
W(\neg \theta_{CancerFalse|PollutionHigh,SmokerFalse}) = 1.00
W(\theta_{XrayPositive|CancerTrue}) = 0.90
W(\neg \theta_{XrayPositive|CancerTrue}) = 1.00
W(\theta_{XrayNegative|CancerTrue}) = 0.10
W(\neg \theta_{XrayNegative|CancerTrue}) = 1.00
W(\theta_{XrayPositive|CancerFalse}) = 0.20
W(\neg \theta_{XrayPositive|CancerFalse}) = 1.00
W(\theta_{XrayNegative|CancerFalse}) = 0.80
W(\neg \theta_{XrayNegative|CancerFalse}) = 1.00
W(\theta_{DyspnoeaTrue|CancerTrue}) = 0.65
W(\neg \theta_{DyspnoeaTrue|CancerTrue}) = 1.00
W(\theta_{DyspnoeaFalse|CancerTrue}) = 0.35
W(\neg \theta_{DyspnoeaFalse|CancerTrue}) = 1.00
W(\theta_{DyspnoeaTrue|CancerFalse}) = 0.30
W(\neg \theta_{DyspnoeaTrue|CancerFalse}) = 1.00
W(\theta_{DyspnoeaFalse|CancerFalse}) = 0.70
W(\neg \theta_{DyspnoeaFalse|CancerFalse}) = 1.00
```

#### 4.2 ENC2

#### Indicator clauses

```
 (\neg \lambda_{PollutionLow} \lor \neg \lambda_{PollutionHigh}) \land (\lambda_{PollutionLow} \lor \lambda_{PollutionHigh}) \land (\neg \lambda_{SmokerTrue} \lor \neg \lambda_{SmokerFalse}) \land (\lambda_{SmokerTrue} \lor \lambda_{SmokerFalse}) \land (\neg \lambda_{Smo
```

```
\lambda_{CancerTrue} \vee \neg \lambda_{CancerFalse}) \wedge (\lambda_{CancerTrue} \vee \lambda_{CancerFalse}) \wedge (\neg \lambda_{XrayPositive} \vee \neg \lambda_{XrayNegative}) \wedge (\lambda_{XrayPositive} \vee \lambda_{XrayNegative}) \wedge (\neg \lambda_{DyspnoeaTrue} \vee \neg \lambda_{DyspnoeaFalse}) \wedge (\lambda_{DyspnoeaTrue} \vee \lambda_{DyspnoeaFalse})
```

#### Parameter clauses

```
(\neg \rho_{PollutionLow} \lor \lambda_{PollutionLow}) \land (\rho_{PollutionLow} \lor \lambda_{PollutionHigh}) \land (\neg
        \rho_{SmokerTrue} \lor \lambda_{SmokerTrue}) \land (\rho_{SmokerTrue} \lor \lambda_{SmokerFalse}) \land (\neg
  \lambda_{PollutionLow} \vee \neg \lambda_{SmokerTrue} \vee \neg \rho_{CancerTrue|PollutionLow,SmokerTrue} \vee 
                   \lambda_{CancerTrue}) \wedge (\neg \lambda_{PollutionLow} \vee \neg \lambda_{SmokerTrue} \vee 
\rho_{CancerTrue|PollutionLow,SmokerTrue} \lor \lambda_{CancerFalse}) \land (\lnot \lambda_{PollutionLow} \lor \lnot
 \lambda_{SmokerFalse} \lor \neg \rho_{CancerTrue|PollutionLow,SmokerFalse} \lor \lambda_{CancerTrue}) \land (\neg
   \lambda_{PollutionLow} \vee \neg \lambda_{SmokerFalse} \vee \rho_{CancerTrue|PollutionLow,SmokerFalse} \vee
                \lambda_{CancerFalse}) \wedge (\neg \lambda_{PollutionHigh} \vee \neg \lambda_{SmokerTrue} \vee \neg
\rho_{CancerTrue|PollutionHigh,SmokerTrue} \lor \lambda_{CancerTrue}) \land (\neg \lambda_{PollutionHigh} \lor \neg
  \lambda_{SmokerTrue} \lor \rho_{CancerTrue|PollutionHigh,SmokerTrue} \lor \lambda_{CancerFalse}) \land (\lnot
\lambda_{PollutionHigh} \lor \lnot \lambda_{SmokerFalse} \lor \lnot \rho_{CancerTrue|PollutionHigh,SmokerFalse} \lor
                  \lambda_{CancerTrue}) \wedge (\neg \lambda_{PollutionHigh} \vee \neg \lambda_{SmokerFalse} \vee \neg \lambda_{SmokerFalse})
\rho_{CancerTrue|PollutionHigh,SmokerFalse} \lor \lambda_{CancerFalse}) \land (\lnot \lambda_{CancerTrue} \lor \lnot 
            \rho_{XrayPositive|CancerTrue} \lor \lambda_{XrayPositive}) \land (\lnot \lambda_{CancerTrue} \lor )
         \rho_{XrayPositive|CancerTrue} \lor \lambda_{XrayNegative}) \land (\lnot \lambda_{CancerFalse} \lor \lnot
           \rho_{XrayPositive|CancerFalse} \vee \lambda_{XrayPositive}) \wedge (\neg \lambda_{CancerFalse} \vee
         \rho_{XrayPositive|CancerFalse} \vee \lambda_{XrayNegative}) \wedge (\neg \lambda_{CancerTrue} \vee \neg
          \rho_{DyspnoeaTrue|CancerTrue} \vee \lambda_{DyspnoeaTrue}) \wedge (\neg \lambda_{CancerTrue} \vee )
        \rho_{DyspnoeaTrue|CancerTrue} \lor \lambda_{DyspnoeaFalse}) \land (\lnot \lambda_{CancerFalse} \lor \lnot
         \rho_{DyspnoeaTrue|CancerFalse} \lor \lambda_{DyspnoeaTrue}) \land (\lnot \lambda_{CancerFalse} \lor )
                         \rho_{DyspnoeaTrue|CancerFalse} \vee \lambda_{DyspnoeaFalse})
```

### Weights

 $W(\lambda_{PollutionLow}) = 1.00$  $W(\neg \lambda_{PollutionLow}) = 1.00$  $W(\lambda_{PollutionHigh}) = 1.00$  $W(\neg \lambda_{PollutionHigh}) = 1.00$  $W(\lambda_{SmokerTrue}) = 1.00$  $W(\neg \lambda_{SmokerTrue}) = 1.00$  $W(\lambda_{SmokerFalse}) = 1.00$  $W(\neg \lambda_{SmokerFalse}) = 1.00$  $W(\lambda_{CancerTrue}) = 1.00$  $W(\neg \lambda_{CancerTrue}) = 1.00$  $W(\lambda_{CancerFalse}) = 1.00$  $W(\neg \lambda_{CancerFalse}) = 1.00$  $W(\lambda_{XrayPositive}) = 1.00$  $W(\neg \lambda_{XrayPositive}) = 1.00$  $W(\lambda_{XrayNegative}) = 1.00$  $W(\neg \lambda_{XrayNegative}) = 1.00$  $W(\lambda_{DyspnoeaTrue}) = 1.00$  $W(\neg \lambda_{DyspnoeaTrue}) = 1.00$  $W(\lambda_{DyspnoeaFalse}) = 1.00$  $W(\neg \lambda_{DyspnoeaFalse}) = 1.00$  $W(\rho_{PollutionLow}) = 0.90$  $W(\neg \rho_{PollutionLow}) = 0.10$ 

```
\begin{split} &W(\rho_{SmokerTrue}) = 0.30 \\ &W(\neg \rho_{SmokerTrue}) = 0.70 \\ &W(\rho_{CancerTrue}|PollutionLow,SmokerTrue) = 0.03 \\ &W(\neg \rho_{CancerTrue}|PollutionLow,SmokerTrue) = 0.97 \\ &W(\rho_{CancerTrue}|PollutionLow,SmokerFalse) = 0.00 \\ &W(\neg \rho_{CancerTrue}|PollutionLow,SmokerFalse) = 1.00 \\ &W(\rho_{CancerTrue}|PollutionHigh,SmokerTrue) = 0.05 \\ &W(\neg \rho_{CancerTrue}|PollutionHigh,SmokerTrue) = 0.95 \\ &W(\neg \rho_{CancerTrue}|PollutionHigh,SmokerFalse) = 0.02 \\ &W(\neg \rho_{CancerTrue}|PollutionHigh,SmokerFalse) = 0.02 \\ &W(\neg \rho_{CancerTrue}|PollutionHigh,SmokerFalse) = 0.98 \\ &W(\rho_{XrayPositive}|CancerTrue) = 0.10 \\ &W(\rho_{XrayPositive}|CancerFalse) = 0.20 \\ &W(\neg \rho_{XrayPositive}|CancerFalse) = 0.80 \\ &W(\rho_{DyspnoeaTrue}|CancerTrue) = 0.65 \\ \end{split}
```

 $W(\neg \rho_{DyspnoeaTrue|CancerTrue}) = 0.35$   $W(\rho_{DyspnoeaTrue|CancerFalse}) = 0.30$   $W(\neg \rho_{DyspnoeaTrue|CancerFalse}) = 0.70$