

Lecture 10/06/23

CRA Due today!
Quiz 5 today!

Defn: let f be a function, ~~Does an inverse~~
~~function~~ f^{-1}

A function f^{-1} is called the inverse to f if

$$f^{-1}(f(x)) = x \quad f(f^{-1}(y)) = y$$

Think of f^{-1} as undoing f

$$f^{-1}(f(x)) = x$$

$$f(f^{-1}(y)) = y$$

#3 Book!

Warning! Not every function has an inverse!
~~How to find inv~~ Will see soon!

How to find Inverse functions

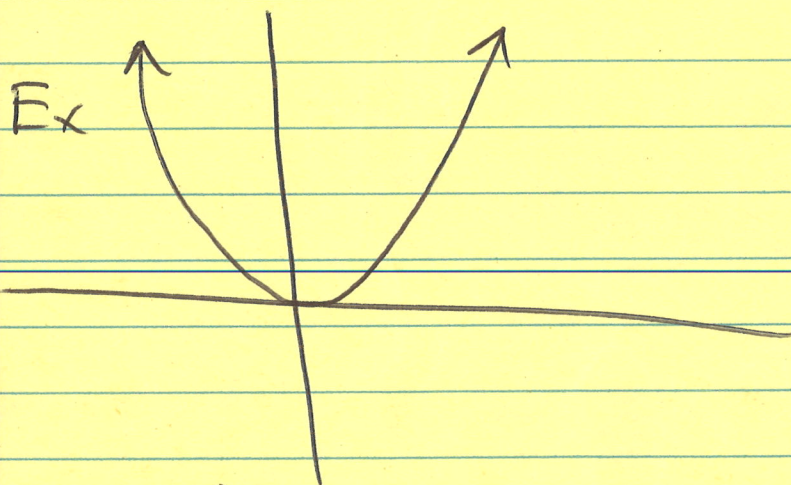
#4 ~~Board~~ Board
 $c + d$

① Swap $x - y$ ② Solve for y .

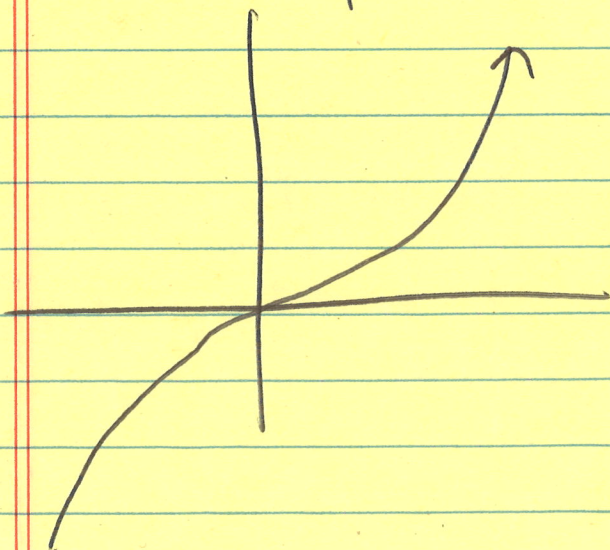
Defn We say a function $f(x)$ is invertible if it has an inverse function f^{-1} . This is the same thing as saying every output of f has a unique input

$\rightarrow =$

H.L.T. A function is invertible if and only if every horizontal line passes through the graph at most once.



Not invertible!



Invertible!

Domain + Range of inverses

$f(x)$

~~but~~

Domain ~~$f(x)$~~ = range $f^{-1}(y)$

Range $f(x)$ = domain ~~$f(x)$~~

Ind var x
Dep var y

$f^{-1}(y)$

Domain $f^{-1}(y)$ = Range $f(x)$

Range $f^{-1}(y)$ = domain ~~$f(x)$~~

Ind var y
Dep var x

#5 #6
└──────────┘
10 mm

#7
5

#8
└──────────┘
Together