Week2 Report

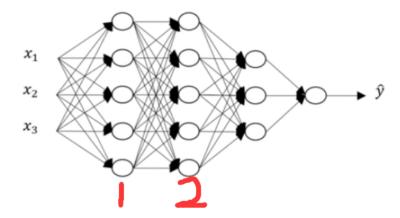
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Contents

	Forward Propagation in a deep Network	2
	1.1 Illustration	2
2	Building Blocks of deep neural Network 2.1	2 2
3	Program for week2	3
	3.1 Codes	
	3.2 Result	5

1 Forward Propagation in a deep Network



1.1 Illustration

For the first layer we calculate X=Z^[1]=W^[1]x + b^[1]

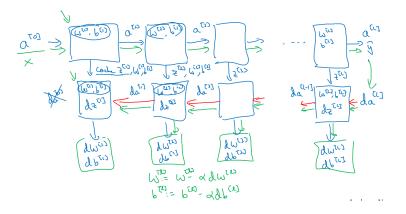
then the activation for this layer is $a^{[1]}=g^{[1]}(Z^{[1]})$

Then for the second layer we use $a^{[1]}$ as input, so we calculate:

 $Z^{[2]}=W^{[2]}a^{[1]}+b^{[2]}$

and so on Use the former activation as the input for the current parameter

2 Building Blocks of deep neural Network



2.1

As the case in the picture, we input the feature $a^{[0]}$, we can propagate forward and calculate the activation which will used as the input of next layer

For back propagating, use \hat{y} to compute for $da^([l])$ and then get $dw^([l])$ and $db^([l])$ and propagate back

3 Program for week2

Abstract

I've struggled to fix my python3 and piped the scipy,h5py,matplot.

It really challenging to practice. I didn't code it by myself, yet, I get through the meaning and learn the programmer of python.

3.1 Codes

```
import numpy as np
import matplotlib.pyplot as plt
import h5py
import scipy
from PIL import Image
from scipy import ndimage
from lr_utils import load_dataset
train_set_x_orig ,train_set_y ,test_set_x_orig ,test_set_y ,classes=load_dataset()
m_train=train_set_x_orig.shape[0]
m_test=test_set_x_orig.shape[0]
num_px=train_set_x_orig.shape[1]
train_set_x_flatten=train_set_x_orig.reshape(m_train,-1).T
test_set_x_flatten=test_set_x_orig.reshape(m_test,-1).T
train_set_x=train_set_x_flatten/255
test_set_x=test_set_x_flatten/255
def sigmoid(x):
    y=1/(1+(np.exp(-x)))
    return y
def initialize_with_zeros(dim):
    w=np.zeros([dim,1])
    b=0
    return w,b
def propagate(w,b,X,Y):
    m=X.shape[1]
    A = sigmoid(np.dot(w.T,X)+b)
    \verb|cost| = (-1/m) * \verb|np.sum| (\verb|np.mu| tiply (Y, \verb|np.log(A|)) + \verb|np.mu| tiply ((1-Y), \verb|np.log(1-A|))|
    dw = (1/m) * np. dot(X, (A-Y).T).T
    db=(1/m)*np.sum(A-Y)
    cost=np.squeeze(cost)
    grads = { 'dw' : dw, 'db' : db}
    return grads,cost
def optimize(w,b,X,Y,num_iterations,learning_rate,print_cost=False):
    costs=[]
    for i in range(num_iterations):
        grads,cost=propagate(w,b,X,Y)
        dw=grads['dw']
        db=grads['db']
        w=w-learning_rate*dw.T
        b=b-learning_rate*db
        if i%100 ==0:
```

```
costs.append(cost)
        if print_cost and i%100 == 0:
           print('Cost after iteration %i: %f'%(i,cost))
        params = { 'w':w, 'b':b}
       grads={'dw':dw,'db':db}
   return params, grads, costs
def predict(w,b,X):
   m=X.shape[1]
   Y_prediction=np.zeros((1,m))
   w=w.reshape(X.shape[0],1)
   A=sigmoid(np.dot(w.T,X)+b)
   print(A)
   Y_prediction=np.around(A)
   print(Y_prediction)
   return Y_prediction
def model(X_train,Y_train,X_test,Y_test,num_iterations=2000,learning_rate=0.5,
                                        print_cost=False):
   w,b=initialize_with_zeros(X_train.shape[0])
   parameters,grads,costs=optimize(w,b,X_train,Y_train,num_iterations,
                                            learning_rate,print_cost);
   w=parameters['w']
   b=parameters['b']
   Y_prediction_test=predict(w,b,test_set_x)
   Y_prediction_train=predict(w,b,train_set_x)
   print("train accuracy: {} %".format(100 - np.mean(np.abs(Y_prediction_train -
                                            Y_train)) * 100))
   print("test accuracy: {} %".format(100 - np.mean(np.abs(Y_prediction_test -
                                            Y_test)) * 100))
   d = {"costs": costs,
         "Y_prediction_test": Y_prediction_test,
        "Y_prediction_train" : Y_prediction_train,
        "w" : w,
"b" : b,
        "learning_rate" : learning_rate,
         "num_iterations": num_iterations}
   return d
learning_rates = [0.01, 0.001, 0.0001]
models = {}
for i in learning_rates:
   print ("learning rate is: " + str(i))
   models[str(i)] = model(train_set_x, train_set_y, test_set_x, test_set_y,
                                            num_iterations = 1500, learning_rate
                                            = i, print_cost = False)
   print ('\n' + "----" + '\n'
                                           )
for i in learning_rates:
   plt.plot(np.squeeze(models[str(i)]["costs"]), label= str(models[str(i)]["
                                            learning_rate"]))
```

```
plt.ylabel('cost')
plt.xlabel('iterations')

legend = plt.legend(loc='upper center', shadow=True)
frame = legend.get_frame()
frame.set_facecolor('0.90')
plt.show()
```

3.2 Result

```
learning rate is: 0.01
[[0.97125943 0.9155338 0.92079132 0.96358044 0.78924234 0.60411297
  0.01179527 0.89814048 0.91522859 0.70264065 0.19380387 0.49537355
  0.7927164 \quad 0.85423431 \quad 0.00298587 \quad 0.96199699 \quad 0.01234735 \quad 0.9107653
  0.13661137 \ 0.01424336 \ 0.96894735 \ 0.1033746 \ 0.00579297 \ 0.86081326
  0.53811196 0.64950178 0.83272843 0.00426307 0.0131452 0.99947804
  0.11468372\ 0.82182442\ 0.69611733\ 0.4991522\ 0.67231401\ 0.01728165
   0.04136099 \ \ 0.80069693 \ \ 0.26832359 \ \ 0.03958566 \ \ 0.74731239 \ \ 0.32116434 
 0.71871197 \ 0.01205725 \ 0.96879962 \ 0.62310364 \ 0.17737126 \ 0.98960523
  0.74697265 0.07284605]]
1. 1. 1. 0. 0. 1. 0. 1. 1. 0. 1. 0. 0. 1. 0. 0. 1. 0. 1. 0. 1. 0. 1. 1. 0. 1.
[[1.47839653e-01 5.78008189e-02 9.42385025e-01 4.14849242e-05
  2.27209941e-02\ 7.29254667e-02\ 2.23704495e-02\ 9.49717864e-01
  5.41724297e-02 2.92729896e-02 6.82412299e-02 8.33370210e-01
  1.71420615 \text{e} - 01 \quad 9.66879883 \text{e} - 01 \quad 8.11537151 \text{e} - 01 \quad 2.44343486 \text{e} - 02
  7.87634096e-03 2.64027273e-02 5.60720048e-02 9.53130353e-01
  5.30865327e-03 3.11020747e-02 1.43606493e-01 1.92650472e-02
  9.30132798 {e}-01 \ 8.95291211 {e}-01 \ 2.72790551 {e}-02 \ 9.01480142 {e}-01
  2.73987903e-02 8.09041583e-01 6.64266070e-02 5.00479730e-02
  1.29245158e-01 1.40274640e-01 6.48179132e-02 1.35261337e-02
  4.77693626 \text{e} - 03 \quad 2.65922709 \text{e} - 02 \quad 8.89771230 \text{e} - 01 \quad 2.64826222 \text{e} - 01
  1.22921586 \text{e} - 02 \quad 6.03229153 \text{e} - 01 \quad 8.81822076 \text{e} - 01 \quad 1.35079743 \text{e} - 02
  2.49595286 \\ e^{-02} \quad 6.88961129 \\ e^{-02} \quad 5.86046929 \\ e^{-02} \quad 8.68932415 \\ e^{-01}
  5.14520332e-03 1.21099845e-02 8.23403970e-01 1.70985647e-01
  9.49977563e-02 3.04227660e-01 9.48091298e-01 8.09204742e-04
  9.66640038 \text{e} - 01 \quad 8.78319466 \text{e} - 01 \quad 3.17284881 \text{e} - 02 \quad 9.76165700 \text{e} - 01
  8.81584697e-01 8.48145722e-01 2.70795161e-02 2.28390395e-02
  1.05295676 \text{e}{-01} \quad 4.45165292 \text{e}{-02} \quad 1.22858876 \text{e}{-02} \quad 1.35813814 \text{e}{-01}
  8.25867437e-01 \ \ 9.21552659e-03 \ \ 2.49353831e-02 \ \ 9.88067070e-01
  5.78381495e-02 8.57292850e-02 4.10128551e-02 5.70507956e-01
  2.11603230e-04 1.52264723e-02 6.18390723e-02 1.39187810e-01
  6.68993749e-02 4.14281787e-04 1.23347661e-02 9.24789062e-01
  8.16880995e-01 9.29503653e-03 8.23770892e-02 2.75905820e-02
  8.52215781 e - 01 \ 2.36580783 e - 02 \ 1.75344552 e - 01 \ 6.15499363 e - 02
  6.58017001 \\ e^{-01} \ \ 9.54697511 \\ e^{-01} \ \ 9.62775471 \\ e^{-01} \ \ 1.05372217 \\ e^{-01}
  9.37239410e-02 9.29062266e-01 2.68654455e-02 1.44668290e-01
  9.15662945e-02 \ \ 2.89260931e-02 \ \ 8.02603133e-01 \ \ 6.11847788e-02
  9.87937141 \\ e^-01 \quad 5.84677167 \\ e^-02 \quad 9.87171184 \\ e^-01 \quad 8.37167548 \\ e^-01
  8.94717386e-01 8.58260204e-01 9.36232298e-01 9.33067878e-01
  8.77279898e-03 5.88387682e-02 5.09517612e-02 2.40626782e-02
  3.87480260e-02 9.35343373e-01 2.35202640e-03 8.83972092e-02
  4.49639007 e^{-03} \quad 6.64404296 e^{-01} \quad 1.76677024 e^{-02} \quad 2.75426444 e^{-05}
  8.71728805 \text{e} - 01 \quad 2.43292079 \text{e} - 03 \quad 8.92351131 \text{e} - 01 \quad 9.50411302 \text{e} - 02
  9.66495010 \text{e}-01 \quad 9.27285472 \text{e}-01 \quad 2.66413779 \text{e}-01 \quad 8.70883113 \text{e}-02
  5.40743543e-02 \ 9.75155427e-01 \ 8.02323751e-01 \ 6.92965781e-01
  9.06287458e-01 \ \ 9.39900204e-01 \ \ 1.64790717e-03 \ \ 1.91364331e-02
```

```
1.66925680e-02 1.46846280e-02 9.39237710e-01 2.57925925e-03
  8.19134438e-01 8.54311895e-01 9.10765300e-01 1.20452015e-01
  9.10603560e-01 9.11977137e-01 3.72174950e-01 6.13527932e-02
  1.30882744 e^{-0.2} \ 9.55225821 e^{-0.1} \ 4.30680817 e^{-0.2} \ 1.37970158 e^{-0.1} \\
  9.60868956e-01 8.67705031e-03 5.95741914e-03 2.19466775e-02
  1.78308410e-03 2.57658926e-02 8.63787547e-01 3.44218953e-02
  9.34152347e-01 9.35483280e-03 9.90908018e-01 1.17832721e-02
  2.67756873e-02 7.74546159e-01 8.43831858e-01 9.38847463e-01
  1.48599255e-01 4.17198955e-03 9.81043189e-01 8.22764984e-01
  1.92120395 \text{e} - 02 \quad 8.58870443 \text{e} - 01 \quad 5.37478572 \text{e} - 02 \quad 7.84878423 \text{e} - 01
  3.56080495 e^{-02} \ 2.80545015 e^{-02} \ 1.09777937 e^{-02} \ 1.30396160 e^{-02}
  3.81067987e - 04 \ 8.51025983e - 01 \ 2.44476493e - 02 \ 4.57657710e - 02
  8.81871553 e^{-01} \quad 1.06481929 e^{-02} \quad 2.84032918 e^{-02} \quad 1.96773462 e^{-02}
  8.54577180e-01 3.01055582e-02 1.33843958e-03 7.04152763e-02
  3.08344786e-01 9.25167630e-01 4.53183034e-02 9.31980530e-03
  8.69872444e-01 4.61339722e-03 4.86286964e-03 7.32772400e-03
  1.26009269e-01 1.46124056e-01 4.51019669e-02 1.45139959e-01
  1.45971589e-01]]
1. \ \ 1. \ \ 0. \ \ 1. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 1. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 1.
  0. \ \ 0. \ \ 1. \ \ 0. \ \ 0. \ \ 1. \ \ 0. \ \ 1. \ \ 1. \ \ 1. \ \ 1. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 1. \ \ 0. \ \ 0. \ \ 1.
  0. \ \ 0. \ \ 0. \ \ 1. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 1. \ \ 1. \ \ 0. \ \ 0. \ \ 0. \ \ 1. \ \ 1. \ \ 1. \ \ 0.
  0.\ 1.\ 0.\ 0.\ 1.\ 0.\ 1.\ 0.\ 1.\ 1.\ 0.\ 0.\ 1.\ 1.\ 1.\ 1.\ 1.\ 1.\ 0.\ 0.\ 0.\ 1.\ 0.
  1. 0. 0. 0. 0. 1. 0. 0. 1. 0. 0. 0. 0. 0. 0. 0. 0.]]
train accuracy: 99.52153110047847 %
test accuracy: 68.0 %
learning rate is: 0.001
 \lceil \lceil 0.744\bar{5}8179 \ \ 0.63302701 \ \ 0.70621076 \ \ 0.7037801 \ \ \ 0.5322598 \ \ \ 0.43784581 
   \hbox{0.1843739} \quad \hbox{0.71778574} \quad \hbox{0.73717649} \quad \hbox{0.59122536} \quad \hbox{0.39837511} \quad \hbox{0.44491784} 
  0.63244572 \ 0.53976962 \ 0.09938522 \ 0.7227688 \ 0.12316033 \ 0.58301417
  0.28145733 \ \ 0.16609522 \ \ 0.61461919 \ \ 0.14166416 \ \ 0.0865388 \ \ \ 0.4251847
  0.67719513 0.61251308 0.46730808 0.11854922 0.21041046 0.8906756
   \tt 0.42313203 \ 0.56013238 \ 0.60322016 \ 0.37148913 \ 0.57460259 \ 0.11968291 
  0.24088599 0.65905854 0.4782032 0.14862075 0.4992436 0.61682528
  0.4795275 \quad 0.16260336 \ 0.70722369 \ 0.23929218 \ 0.36719514 \ 0.87223907
  0.45484261 0.19029187]]
0. 0.11
[[0.34403391 0.18575705 0.63392388 0.00949352 0.185803
                                                              0.30979007
  0.13544854 \ 0.75931407 \ 0.18856286 \ 0.16653711 \ 0.47903517 \ 0.55094252
   \tt 0.39894694 \ 0.67613631 \ 0.32941411 \ 0.15120523 \ 0.1515817 \ 0.10868391 
  0.21533234\ 0.78261458\ 0.09236643\ 0.13102179\ 0.30209379\ 0.22018859
  0.60467471 \ \ 0.63089631 \ \ 0.13786841 \ \ 0.52162666 \ \ 0.2229145 \ \ \ 0.41807311
   0.20928386 \ \ 0.22354737 \ \ 0.51863273 \ \ 0.37446655 \ \ 0.12619979 \ \ 0.24763606 
  0.08217106 \ 0.20570627 \ 0.61668309 \ 0.47341694 \ 0.07578526 \ 0.20272218
  0.63694514 \ 0.17332725 \ 0.12774778 \ 0.38987251 \ 0.25716102 \ 0.57589232
  0.03660729 0.23627192 0.5058546 0.44851881 0.26882028 0.54506441
   \tt 0.63427748 \ 0.07593065 \ 0.79389128 \ 0.55848777 \ 0.20399827 \ 0.82950311 
   \tt 0.67551516 \ 0.49340246 \ 0.12825017 \ 0.19483707 \ 0.30405843 \ 0.25239064 
 0.23849329 \ 0.28306742 \ 0.39562206 \ 0.1338017 \ \ 0.20953382 \ 0.84559705
  0.25983452 \ 0.43347997 \ 0.25869745 \ 0.5275365 \ 0.01851016 \ 0.18226072
   \tt 0.11686925 \ 0.24360522 \ 0.11457144 \ 0.09711829 \ 0.11403479 \ 0.64158072 
   \mathtt{0.56492264} \ \ \mathtt{0.14249209} \ \ \mathtt{0.26621215} \ \ \mathtt{0.23562087} \ \ \mathtt{0.63347539} \ \ \mathtt{0.19718838} 
  0.41665293 \ 0.2560914 \ 0.20511226 \ 0.75854285 \ 0.62700096 \ 0.22437352
  0.24158168 0.58986637 0.18250551 0.31168748 0.40230892 0.18766222
```

```
 \tt 0.37363736 \ 0.24954905 \ 0.81540625 \ 0.33905562 \ 0.85287524 \ 0.46460165 
  \tt 0.64873862 \ 0.49476607 \ 0.58689285 \ 0.73160658 \ 0.15974705 \ 0.28192355 
 0.21969254 0.17213348 0.24140747 0.59506433 0.09843999 0.4664941
  \tt 0.11789794 \ 0.41615495 \ 0.28828188 \ 0.01549565 \ 0.57657208 \ 0.03491378 
 0.56433333 0.52342054 0.58263447 0.828261
                                            0.33112864 0.30054751
 0.13866344 0.7796039 0.49905825 0.23849455 0.65130553 0.54865883
  0.07475945 \ \ 0.15289783 \ \ 0.17277205 \ \ 0.21093974 \ \ 0.77996081 \ \ 0.05731401 
  \tt 0.43542011 \ 0.62528802 \ 0.58301417 \ 0.39592429 \ 0.62711359 \ 0.62164606 
 0.52142034 \ 0.2237536 \ 0.11263677 \ 0.69875451 \ 0.13460421 \ 0.59843604
 0.53465382 0.37298272 0.67567251 0.08157721 0.80300364 0.36035876
 0.12411481 \ 0.3216639 \ 0.50044148 \ 0.71061923 \ 0.38536321 \ 0.15865892
 0.73153708 \ 0.60089581 \ 0.19123039 \ 0.60169201 \ 0.21145324 \ 0.35174627
 0.1036799 \quad 0.15432715 \quad 0.08266478 \quad 0.1765554 \quad 0.0315303 \quad 0.4005418
  \tt 0.12684962 \ 0.13818573 \ 0.69657105 \ 0.10353719 \ 0.15229696 \ 0.170385 
  \tt 0.39005657 \ 0.21251557 \ 0.03788715 \ 0.32853945 \ 0.47339083 \ 0.62631301 
 0.22739755 0.0902158 0.56782331 0.17507791 0.20252309 0.09500011
 0.34504767 0.39618939 0.25822558 0.24550552 0.30677401]]
1. \ \ 1. \ \ 0. \ \ 1. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 1. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 1.
 0. \ \ 0. \ \ 0. \ \ 1. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 1. \ \ 1. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 1. \ \ 1. \ \ 0.
 0.\ \ 0.\ \ 0.\ \ 1.\ \ 0.\ \ 1.\ \ 1.\ \ 1.\ \ 1.\ \ 1.\ \ 0.\ \ 0.\ \ 1.\ \ 0.\ \ 0.\ \ 1.\ \ 1.\ \ 0.\ \ 0.\ \ 1.\ \ 0.
 0. \ \ 0. \ \ 1. \ \ 1. \ \ 0. \ \ 1. \ \ 1. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 1. \ \ 0. \ \ 0. \ \ 0.
 0. 0. 0. 0. 1. 0. 0. 1. 0. 0. 0. 0. 0. 0. 0. 0.]
train accuracy: 88.99521531100478 %
test accuracy: 64.0 %
learning rate is: 0.0001
0.28884626 0.46438078 0.45494399 0.45491705 0.36938309 0.41863679
 0.45816519 \ 0.5031755 \ 0.2842568 \ 0.45155065 \ 0.30672371 \ 0.37824086
 0.26505548 \ \ 0.27737934 \ \ 0.40677576 \ \ 0.28781555 \ \ 0.24304775 \ \ 0.38397796
 0.50642581 0.47047843 0.35358916 0.31561491 0.39430714 0.4603235
 0.37998879 \ 0.3764821 \ 0.32056264 \ 0.38693085 \ 0.40764828 \ 0.23150119
 0.311659
           0.44981144 0.43152263 0.26276732 0.37785575 0.48883282
  \tt 0.37790798 \ 0.30969512 \ 0.47842906 \ 0.32857529 \ 0.34457076 \ 0.60547775 
 0.40733226 0.28828383]]
0. 0.11
[[0.4225819    0.31692389    0.42964509    0.14896683    0.28783033    0.38652698
  \tt 0.29492571 \ 0.44991522 \ 0.31988018 \ 0.32391139 \ 0.39318147 \ 0.34804173 
  \tt 0.40099138 \ 0.31694856 \ 0.28102266 \ 0.3231201 \ 0.25486297 \ 0.18485428 
  \hbox{\tt 0.31900054 0.52941528 0.25568417 0.27297382 0.29762542 0.35834172 } 
 0.38912252 \ 0.4552143 \ 0.2555983 \ 0.34830216 \ 0.29078565 \ 0.27432926
  \tt 0.31094887 \ 0.44330557 \ 0.47172673 \ 0.39765449 \ 0.22386371 \ 0.46108148 
 0.27055987 \ \ 0.31333951 \ \ 0.49901097 \ \ 0.439851 \ \ \ \ 0.23953174 \ \ 0.29809115
 0.42197081 \ \ 0.28385499 \ \ 0.2465556 \ \ \ \ 0.40478121 \ \ 0.35487343 \ \ 0.45521241
  0.40460677 \ \ 0.24757226 \ \ 0.50122617 \ \ 0.38917296 \ \ 0.3687779 \ \ \ 0.50666786 
  \tt 0.52492017 \ 0.37864634 \ 0.24031899 \ 0.30627306 \ 0.35114005 \ 0.37398054 
 0.43104844 0.31851314 0.37029232 0.29232461 0.37616632 0.52373453
  \tt 0.32507684 \ 0.48381803 \ 0.39170698 \ 0.38646363 \ 0.17397111 \ 0.31623794 
  \hbox{\tt 0.38500817 0.46053573 0.23091555 0.47268593 0.43291929 0.26828088 } 
 0.30258929 0.4164904 0.24453098 0.27111067 0.39272427 0.3043153
```

```
0.27984468 \ 0.39085873 \ 0.52409691 \ 0.34966557 \ 0.55950717 \ 0.37739831
     \tt 0.43697184 \ 0.33557455 \ 0.38439647 \ 0.48607992 \ 0.30731772 \ 0.31028645 
    0.30037443\ 0.29400226\ 0.42714997\ 0.42909528\ 0.30432821\ 0.5227302
    0.32144602\ 0.4066469\ 0.43683178\ 0.17768611\ 0.4354696\ 0.18662466
     \tt 0.39558874 \ 0.48819809 \ 0.35425959 \ 0.57279833 \ 0.35098941 \ 0.33429763 
    0.31014998 0.49175402 0.44154511 0.31203466 0.38776576 0.38352489
    0.29611222\ 0.36104647\ 0.33824864\ 0.37198268\ 0.52831432\ 0.25732676
     \tt 0.36743298 \ 0.44902822 \ 0.37824086 \ 0.36790056 \ 0.41246464 \ 0.37833397 
    0.3418507 0.30119593 0.2592477 0.46753926 0.26777792 0.43134603
     \tt 0.32491304 \ 0.19700069 \ 0.25937972 \ 0.33143626 \ 0.19820128 \ 0.35468513 
     0.36334932 \ 0.51823778 \ 0.37235121 \ 0.27650473 \ 0.47271147 \ 0.44760504 
    0.33240186\ 0.29967323\ 0.41157608\ 0.47817969\ 0.39048545\ 0.28309008
    0.46350184 \ 0.41099669 \ 0.34508275 \ 0.4323286 \ 0.35065016 \ 0.33976266
    0.25459527 \ \ 0.29233107 \ \ 0.26976618 \ \ 0.30004182 \ \ 0.18212017 \ \ 0.34254174
    0.3783451 \quad 0.32762257 \quad 0.19831251 \quad 0.51451759 \quad 0.3792938 \quad 0.41417054
    0.34795587 0.25521854 0.42313521 0.32557428 0.38342989 0.21943589
    0.34909483 0.39399177 0.36128874 0.38042346 0.38929593]]
0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0.
    0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 1. \ \ 1. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 1.
    0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0.
    0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \  \, 0. \ \, 0. \  \, 0. \ \, 0. \ \, 0. \ \, 0. \ \, 0. \ \, 0. \ \, 0. \ \, 0. \ \, 0. \ \, 0. \ \, 0. \ \, 0. \ \, 0. \ \, 0. \ \, 0. \ \, 0. \ \, 0. \ \, 0. \ \, 0. \ \, 0. \ \, 0. \ \, 0. \ \, 0. \ \, 0. \ \, 0. \ \, 0. \ \, 0. \ \, 0. \ \, 0. \ \, 0. \ \, 0. \ \, 0. \ \, 0. \ \, 0. \ \, 0. \ \, 0. \ \, 0. \ \, 0. \ \, 0. \ \, 0. \ \, 0. \ \, 0. \ \, 0. \ \, 0. \ \, 0
    0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 1. \ \ 0. \ \ 0. \ \ 0.
    0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0. \ \ 0.
   train accuracy: 68.42105263157895 %
test accuracy: 36.0 %
```

