## **Math Primer**

## **Taylor Series Expansion**

Expand a function as an infinite sum of its derivatives

$$f(x + \delta x) = f(x) + \frac{\partial f}{\partial x} \delta x + \frac{\partial^2 f}{\partial x^2} \frac{\delta x^2}{2!} + \dots + \frac{\partial^n f}{\partial x^n} \frac{\delta x^n}{n!}$$

So, now you can see that if delta\_x is really small, then the higher order terms are almost zero (i.e if dx is small to begin with, the delta\_x^2 is even smaller)

If  $\delta x$  is small:

$$f(x + \delta x) = f(x) + \frac{\partial f}{\partial x} \delta x + O(\delta x^2)$$
 Almost Zero

So you model  $f(x + delta_x)$  by  $f(x) + df/dx * delta_x$ . This is a linear approximation because the approximation is linear in dx. AKA First order Taylor approximation.

For a function of three variables with small  $\delta x$ ,  $\delta y$ ,  $\delta t$ :

$$f(x + \delta x, y + \delta y, t + \delta t) \approx f(x, y, t) + \frac{\partial f}{\partial x} \delta x + \frac{\partial f}{\partial y} \delta y + \frac{\partial f}{\partial t} \delta y$$

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