

# Vehicle Dynamics Modelling and Simulation

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CHAPTER 10.1

# Liniowy model jednośladowy

Stała prędkość środka ciężkości

Ruch toczny pominięty

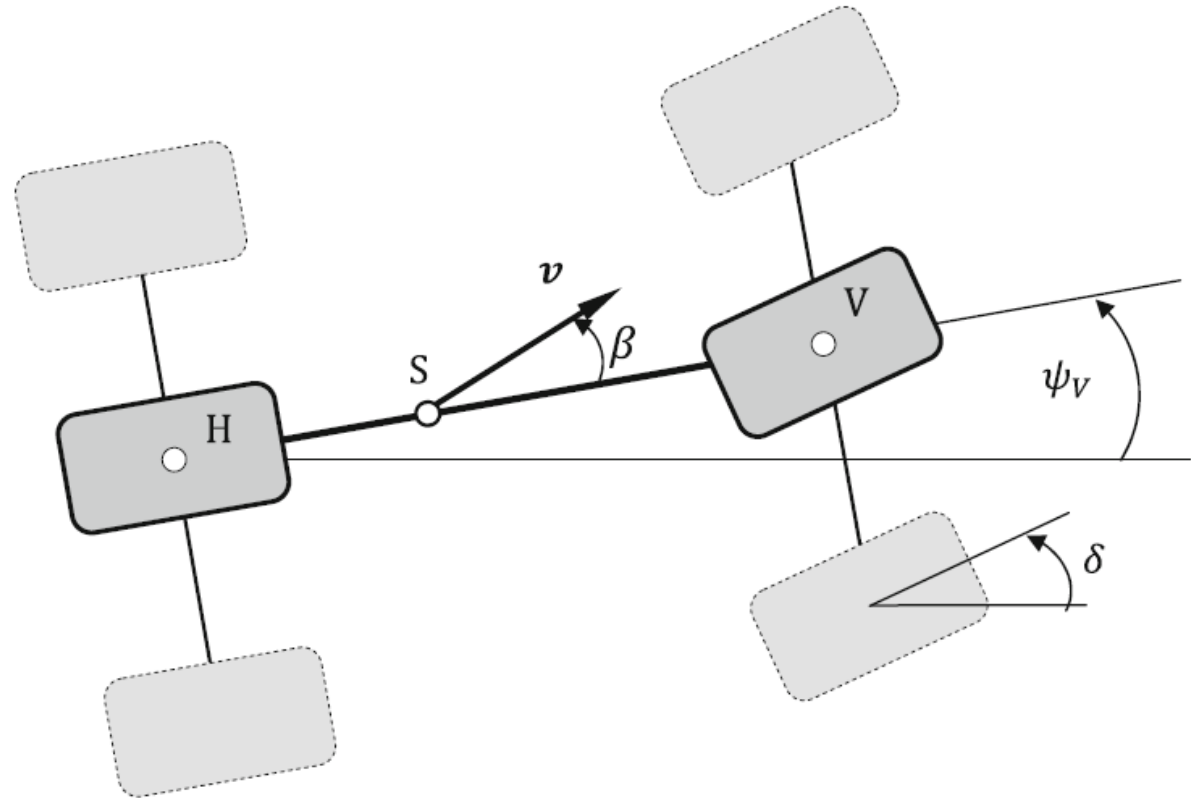
Masa w środku ciężkości

Przednie i tylne opony jako jedna opona na środku każdej z osi

Moment obrotowy wynikający z kąta poślizgu pominięty

Siły wzdłużne w oponach pominięte

$$a_y \leq 0,4g \approx 4 \frac{\text{m}}{\text{s}^2}$$



# Zależności

$$\tan \delta_A = \frac{l}{\sqrt{\rho_M^2 - l_h^2}}$$

$$\delta_A \approx \frac{l}{\rho_M}$$

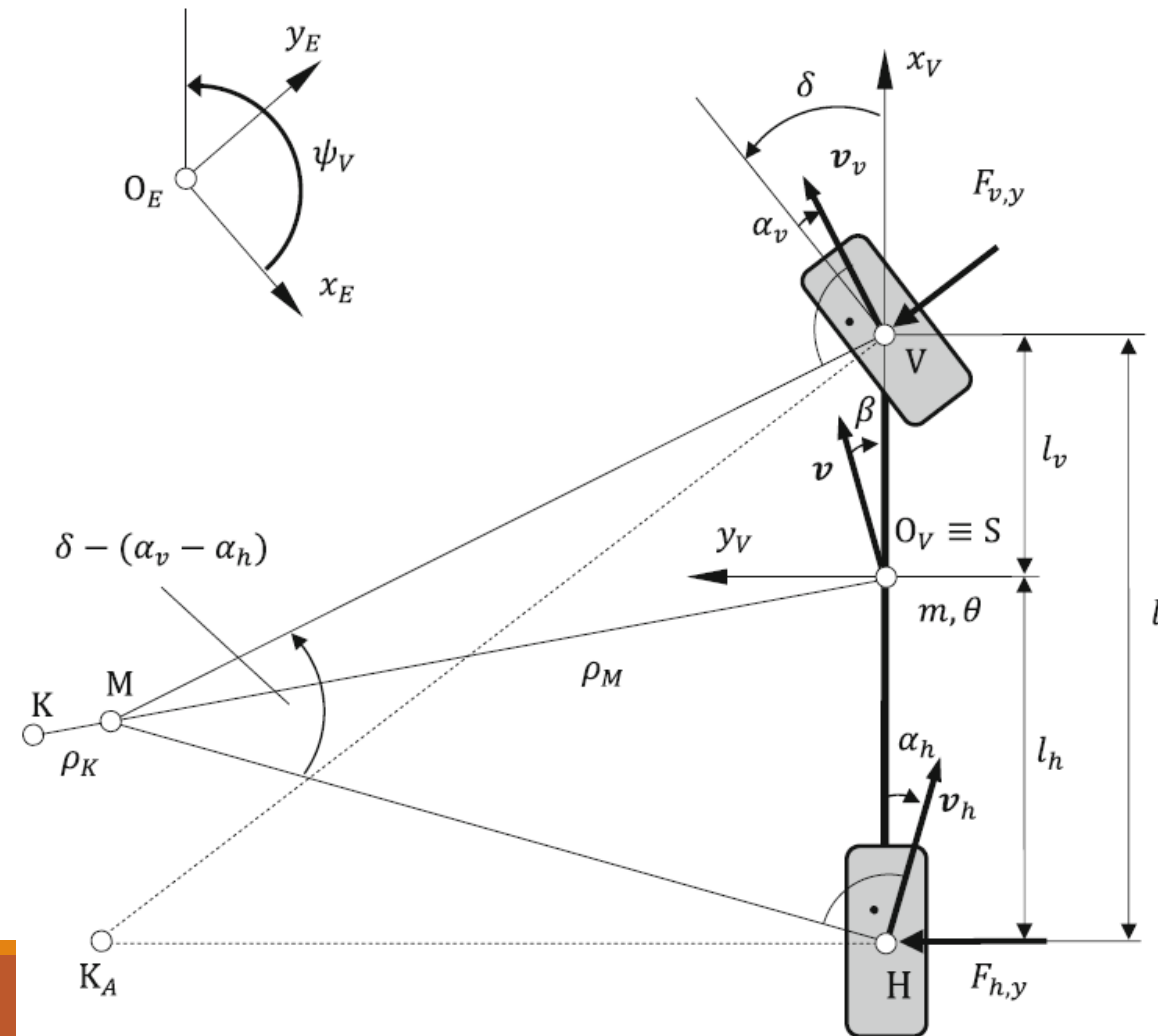
$$a_n = |\mathbf{a}_n| = v(\dot{\psi}_V + \dot{\beta})$$

$$\rho_K = \frac{v}{(\dot{\psi}_V + \dot{\beta})}$$

$$a_y = v(\dot{\psi}_V + \dot{\beta}) \cos \beta \approx v(\dot{\psi}_V + \dot{\beta}) = \frac{v^2}{\rho_K}$$

$$\alpha_v = \delta - \beta - l_v \frac{\dot{\psi}_v}{v}$$

$$\alpha_h \approx -\beta + l_h \frac{\dot{\psi}_V}{v}$$

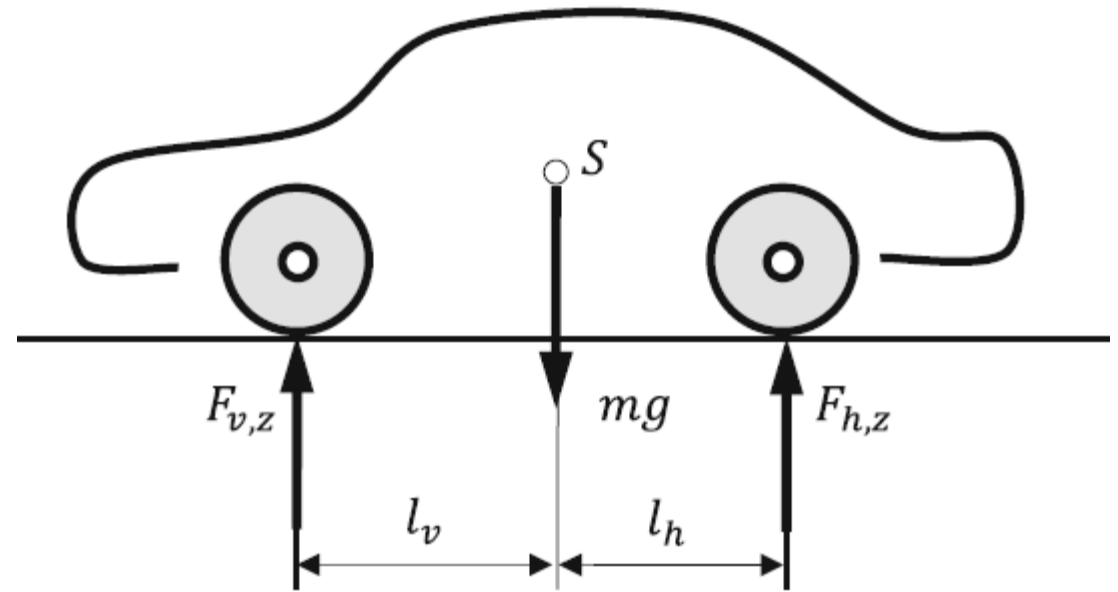


# Obciążenia opon

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$$F_{v,z} = mg \frac{l_h}{l} \quad \text{and} \quad F_{h,z} = mg \frac{l_v}{l}$$

$$F_{v,y} = c_{\alpha,v} \alpha_v \quad \text{and} \quad F_{h,y} = c_{\alpha,h} \alpha_h$$



# Równania ruchu modelu

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$$mv(\dot{\psi}_V + \dot{\beta})\cos\beta = \cos\delta F_{v,y} + F_{h,y}$$

$$\theta\ddot{\psi}_V = F_{v,y}\cos\delta l_v - F_{h,y}l_h$$

$$mv\dot{\beta} + (mv^2 + c_{\alpha,v}l_v - c_{\alpha,h}l_h)\frac{\dot{\psi}_V}{v} + (c_{\alpha,v} + c_{\alpha,h})\beta = c_{\alpha,v}\delta$$

$$\theta\ddot{\psi}_V + (c_{\alpha,v}l_v^2 + c_{\alpha,h}l_h^2)\frac{\dot{\psi}_V}{v} + (c_{\alpha,v}l_v - c_{\alpha,h}l_h)\beta = c_{\alpha,v}l_v\delta$$

# Pokonywanie zakrętów

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$$\delta = const, \dot{\delta} = 0$$

$$\dot{\psi}_V = const, \ddot{\psi}_V = 0$$

$$\beta = const, \dot{\beta} = 0$$

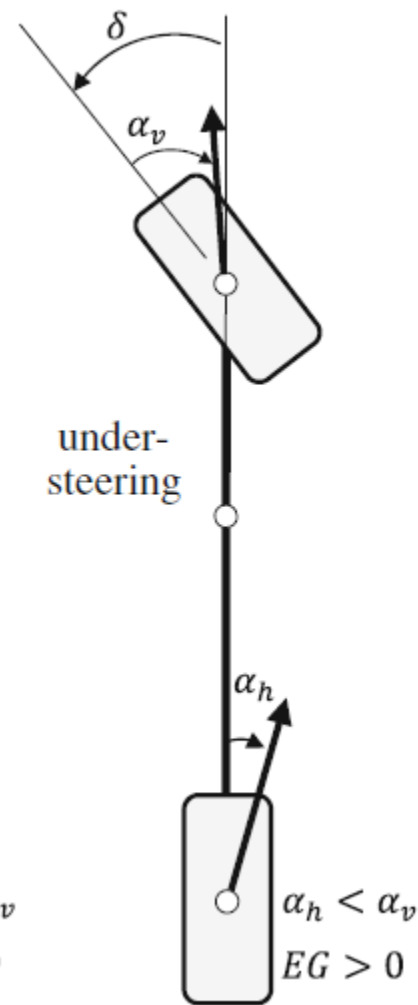
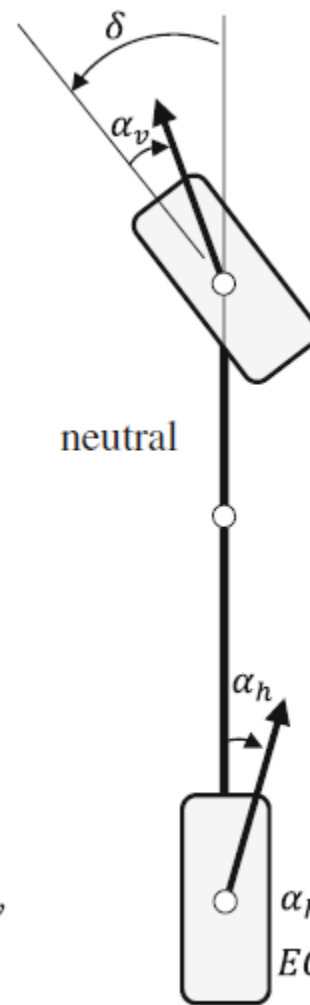
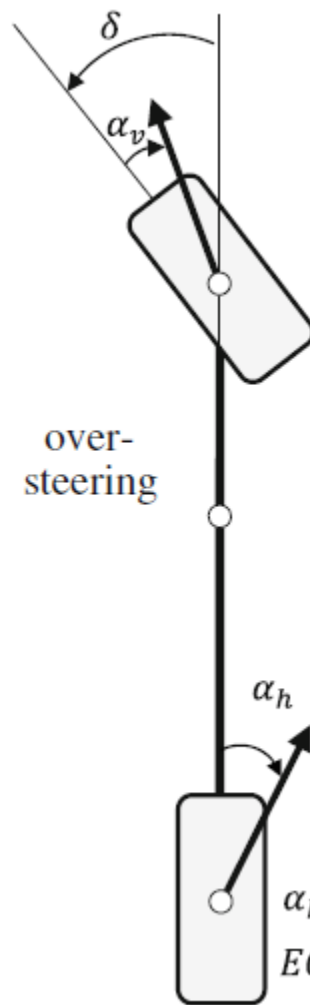
$$\rho_K = \frac{v}{\dot{\psi}_V + \dot{\beta}} = \frac{v}{\dot{\psi}_V} = \rho$$

# Sterowność

$$\beta = l_h \frac{\dot{\psi}_V}{v} - \alpha_h = \frac{l_h}{\rho} - \frac{m}{c_{\alpha,h}} \frac{l_v v^2}{l \rho}$$

$$\begin{aligned} \delta &= l_v \frac{\dot{\psi}_V}{v} + \alpha_v + \beta = \frac{l}{\rho} + \alpha_v - \alpha_h \\ &= \underbrace{\frac{l}{\rho}}_{\delta_A} + \underbrace{\frac{m}{l} \left( \frac{l_h c_{\alpha,h} - l_v c_{\alpha,v}}{c_{\alpha,v} c_{\alpha,h}} \right)}_{EG} \underbrace{\frac{v^2}{\rho}}_{a_y} = \delta_A + EG \cdot a_y \end{aligned}$$

$$EG \cdot a_y = \alpha_v - \alpha_h$$



# Zależności

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$$\dot{\psi}_V = \frac{v}{\rho} = \text{const}$$

$$F_{v,y} = m \frac{l_h v^2}{l \rho} \quad F_{h,y} = m \frac{l_v v^2}{l \rho}$$

$$\alpha_v = \frac{F_{v,y}}{c_v} = \frac{m}{c_{\alpha,v}} \frac{l_h v^2}{l \rho} \quad \alpha_h = \frac{F_{h,y}}{c_h} = \frac{m}{c_{\alpha,h}} \frac{l_v v^2}{l \rho}$$

$$v_{kr} = \sqrt{-\frac{l}{EG}}$$