

CS512 Assignment 4: Report

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Abstract

Implementation of epipolar line construction using weak calibration and 8 point algorithm

Problem statement

- Two views of the same object is seen
- Point on one view is related to the other view
- The search space for the corresponding points on the views is limited to a line

Proposed solution

Over view:

- Read two images from command line
- load them and display next to each other
- user clicks on corresponding points in the image through mouse
- normalizing each point
- Fundamental matrix of normalized points
- Ensure rank 2 matrix
- Fundamental matrix calculation
- Epipolar line calculation and drawing
- Epipole calculation

Normalizing points

- Each point in each image is taken individually and normalized using M

$$q_i = \begin{bmatrix} \frac{1}{\sigma} & & \\ & \frac{1}{\sigma} & \\ & & 1 \end{bmatrix} \begin{bmatrix} 1 & -x_c & -x_c y_c \\ 0 & 1 & -y_c \\ 0 & 0 & 1 \end{bmatrix} p_i$$

M

$$q_i = M p_i$$
$$q'_i = M' p'_i$$

- Mean and sigma are calculated for the points in each image and used as seen in above image to normalize points

Computation of fundamental matrix

- Fundamental matrix for normalized points is found by taking svd on a system of equations matrix developed as shown in the below image

- Right null space of A is the fundamental matrix
- Fundamental matrix is ensured to be Rank 2 by making the last element of D to zero and the matrices are recombined to form A
- Svd is performed on this again whose right null space represents the 2rank fundamental matrix of normalized points

Computing Fundamental matrix of original points

- Using the relation shown below we compute the fundamental matrix from Fprime which is fundamental matrix of normalized points

Epipolar line is construction

- Left epipolar line and right epipolar line are computed as r and l
- $l = F p_l$
 - where p_l is the point selected in left image
- $r = F^{\text{transpose}} * p_r$
 - where p_r is the point selected in the right image

Current Implementation

- Input
 - Two views of the same object is taken
- User selects points on the image (8)
- Epipolar lines are bit off where it should be displayed

Future Enhancements

- Improving the implementation to better accuracy

Manual

Structure of manual:

- Type of input description
- Command line arguments
- Input description
- Output

1. Input provided as two images **rock-l.tif rock-r.tif**

command line arguments : <leftimage> <rightimage>

2. Manual selection of points

Select corresponding points on the left and right image displayed by double clicking on the images

3. Press any key to move forward

4. Images are redisplayed for user point selection for epipolar line construction

5. On selection epipolar line will be displayed depending on the image on which points were selected

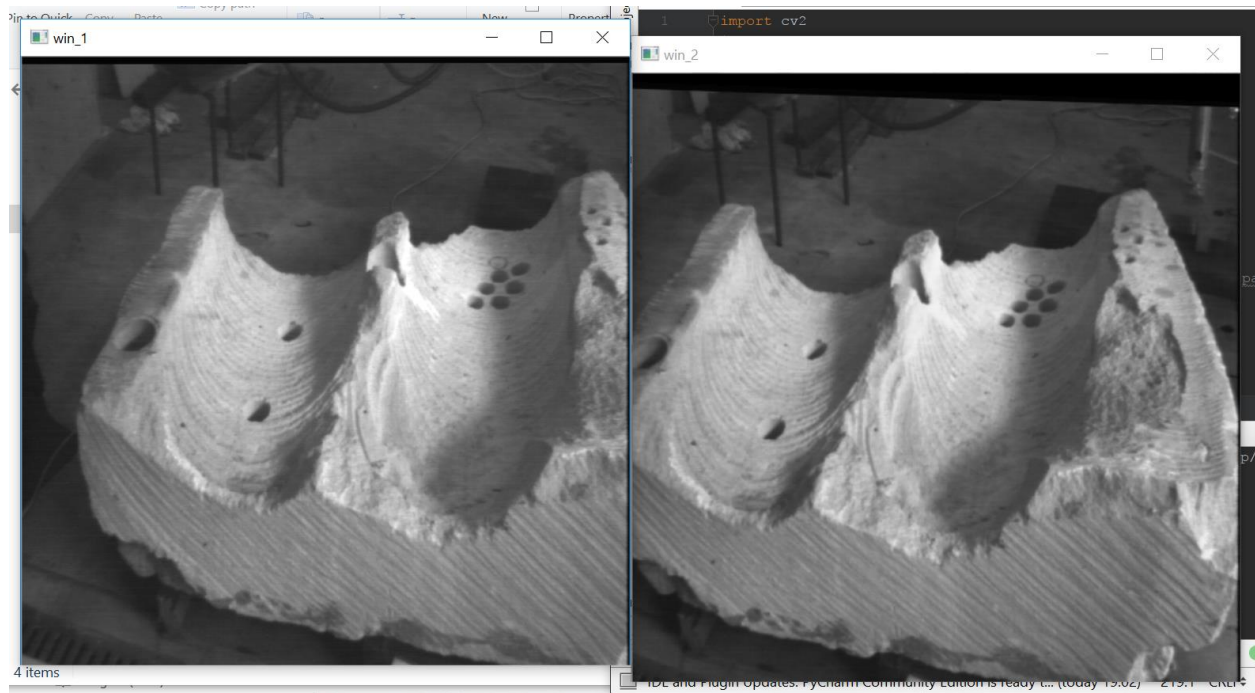
NOTE: user can select point on either left or right image

Example Results for various input options

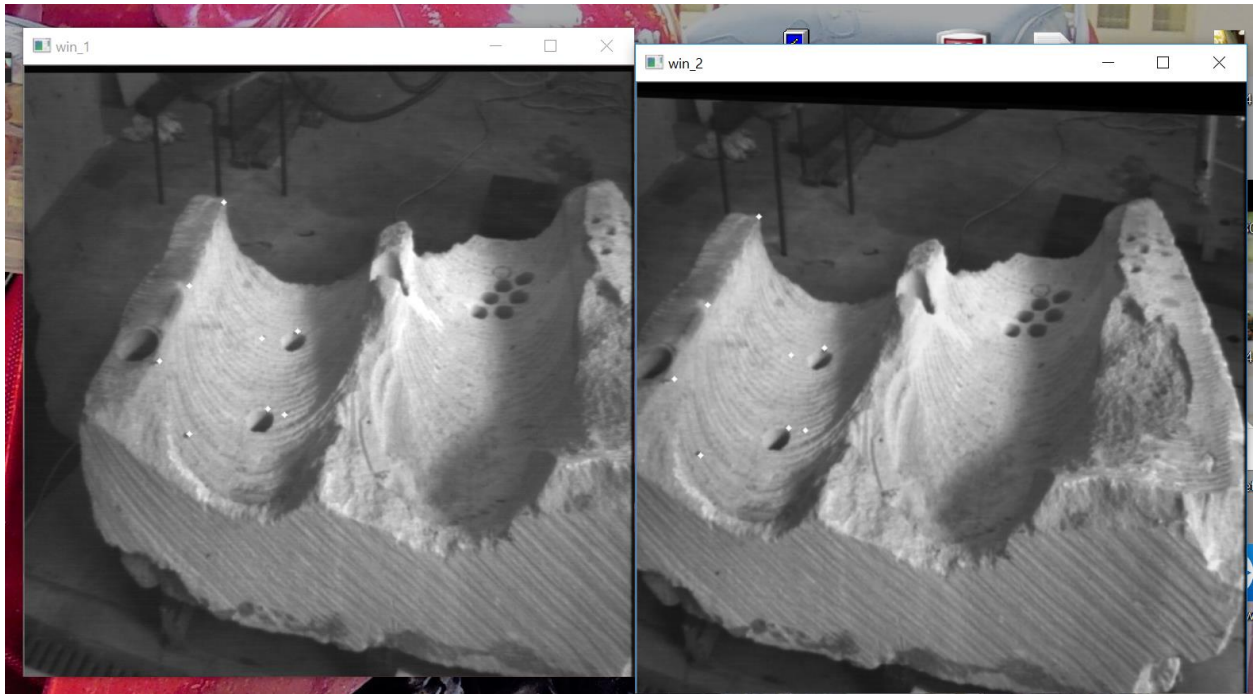
Instruction to start the program :

“Python Main.py rock-l.tif rock-r.tif”

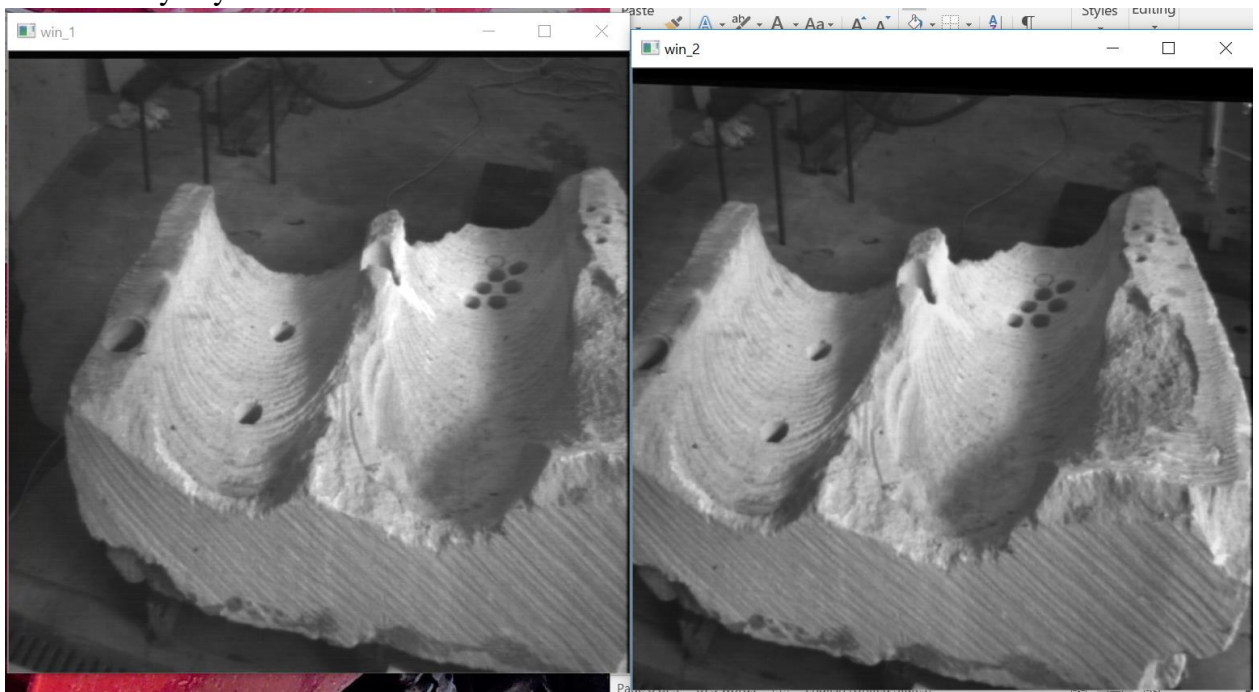
1. Input rock-l.tif rock-r.tif



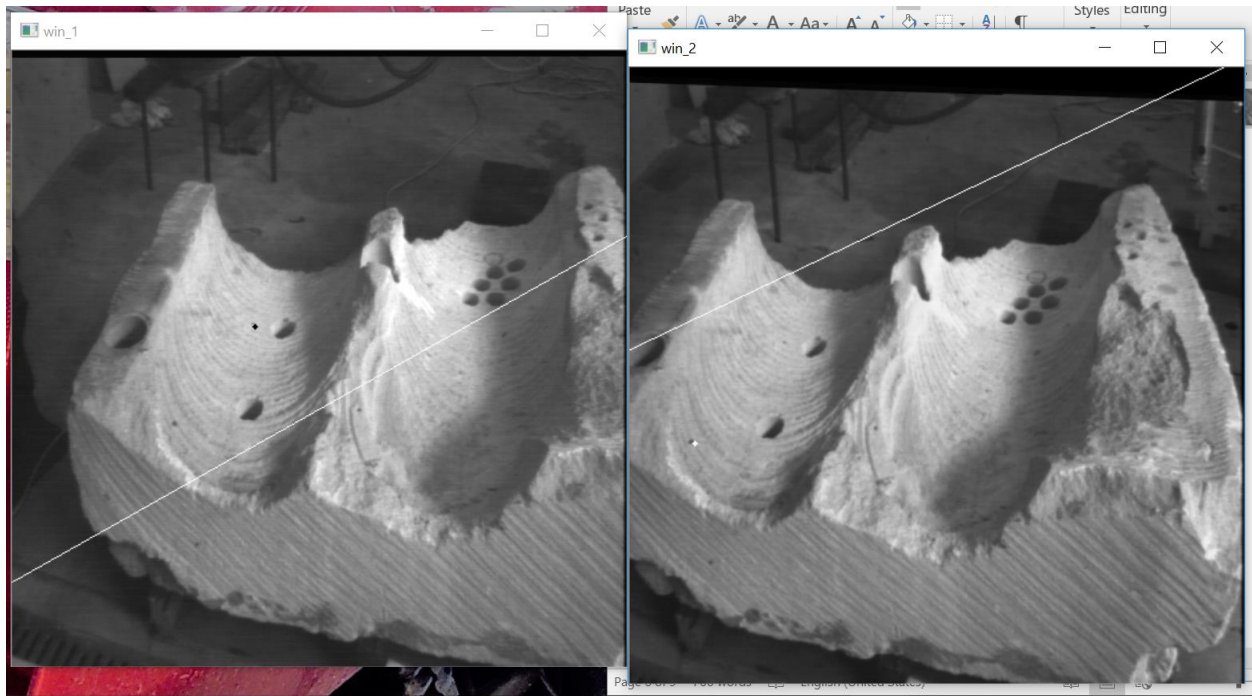
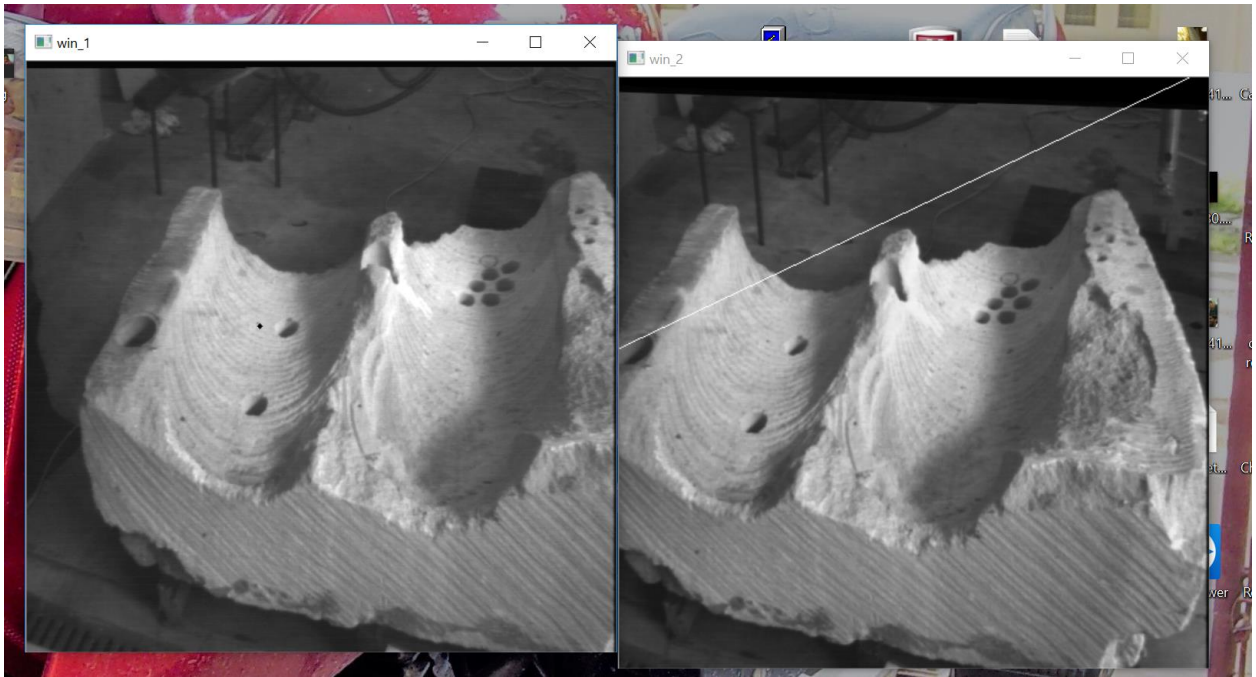
- Select the points by double clicking in the following pattern as follows:
(selection is highlight with white color)



- Press any key to move forward



- New images are shown to input points for computation of epipolar lines
- Double click on either of the image
- Following image shows epipolar line construction when a point (black) is selected on the left image



Line construction when points are selected on both the images(black on left, white on right)

- Corresponding epipoles are seen in the console

```
left epipole {} -0.000685444791082
right epipole [] -0.000102903692904
left epipole {} -0.000685444791082
right epipole [] -0.000102903692904
```