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EE 381 – Probability and Statistics with Applications to Computing

Lab 3 - Project on Binomial and Poisson Distributions

1) Experimental Bernoulli Trials

a) **INTRODUCTION:**

- i) The experiment follows tossing 3 dices 1000 times and recording whenever 3 sixes in a roll. Then create a probability mass function plot.

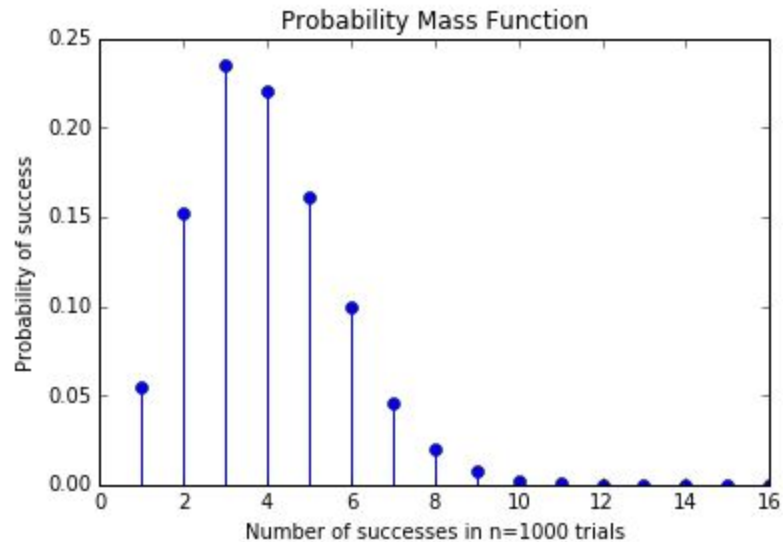
b) **METHODOLOGY:**

- i) Create several for loops to simulate a toss then doing it multiple times. If we toss 3 sixes we record that success by first checking if the dice roll equals to 6. Once we got the successes we store that on a list and send it to the plotting function.

c) **RESULTS AND CONCLUSIONS:**

- i) From running the program we get the following Distribution chart:

```
In [28]: runfile('/home/beryl/Downloads/untitled0.py', w
```



2) Calculation using the Binomial Distribution

a) INTRODUCTION:

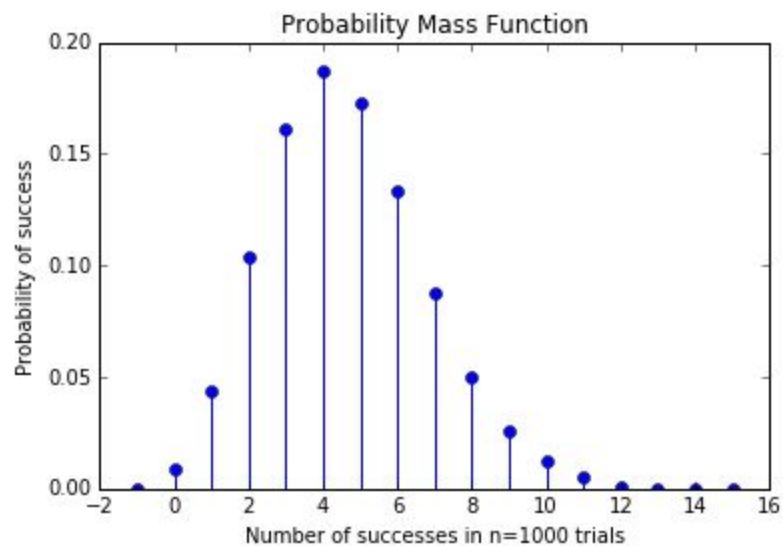
- i) The problem is the same as the previous one however we now use the Binomial distribution to calculate the probability of success of getting 3 sixes in one roll.

b) METHODOLOGY:

- i) We start by having the probability of getting 3 dices to each be 6 in a roll is $1/216$. With that we can calculate the Binomial Distribution by getting the values of p , q , and c . Once we have that we can get the calculation and print to a graph.

c) RESULTS AND CONCLUSIONS:

```
In [15]: runfile('/home/beryl/Downloads/untitled0.py', v
```



Compared to #1, 4 seem to be higher successes

3) Approximation of Binomial by Poisson Distribution

a) INTRODUCTION:

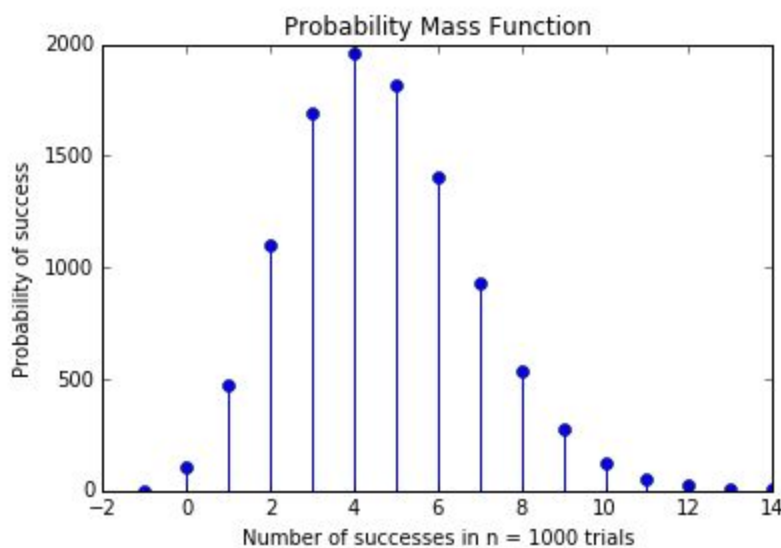
- i) Same as the previous problem, however we use the Poisson Distribution to approximate the previous answer.

b) METHODOLOGY:

- i) We solve this problem by first declaring all known variables for the Poisson Distribution. We then go and do multiple runs on the equation saving the results to a list which we then print in a distribution.

c) RESULTS AND CONCLUSIONS:

In [24]: `runfile('/home/beryl/Downloads/untitled0.py', wc`



It gave the same result as 3 which means the Poisson gave a pretty good approximation to the binomial

4) Appendix

a) Code for #1

```

1 # -*- coding: utf-8 -*-
2
3 # Name: Roberto Sanchez
4 # Assignment #3 Part 1
5 # October 14, 2017
6
7 import numpy as np
8 import random
9 import matplotlib.pyplot as plt
10 # Number of rounds ie: number of experiments run in this case 10,000
11 def Experiment(rounds):
12     #Tracks all the success per trial
13     ListOfSuccesses = []
14     # run experiment in number of rounds
15     for y in range(rounds):
16         #runs one trial, tosses 3 dices and see if its 3 sixes
17         TrialSuccessful = 0
18         # This is for one trial, repeated 1000 times
19         for x in range(1000):
20             #tracks if we have a six in a row when tossing 3 dies
21             GotaSix = 0
22             #Tossing 3 Dies
23             for z in range(3):
24                 # Is the value 6?
25                 if random.randint(1,7) == 6:
26                     #track it
27                     GotaSix += 1
28             #After tossing 3 dies, did we get 3 sixes?
29             if GotaSix == 3:
30                 #Track it
31                 TrialSuccessful += 1;
32             #After one trial, store value in list
33             ListOfSuccesses.append(TrialSuccessful)
34             #print("Success in Trial ",y," : ",TrialSuccessful)
35     # This prints out the graph
36     b = range(0,17)
37     h1, bin_edges = np.histogram(ListOfSuccesses, bins = b)
38     b1 = bin_edges[1:17]
39     # stem(x,y) coordinates
40     plt.stem(b1, h1/rounds)
41     plt.title("Probability Mass Function")
42     plt.ylabel("Probability of success")
43     plt.xlabel("Number of successes in n=1000 trials")
44
45 Experiment(10000)
46

```

b) Code for #2

```

1
2 import scipy as sp
3 import numpy as np
4 import matplotlib.pyplot as plt
5 def CalcBinomial(rounds):
6     calc = []
7     probability = 1/216.
8     #does the binomial calculation
9     for x in range(0,17):
10         c = sp.misc.comb(rounds,x)
11         p = np.power(probability, x)
12         q = np.power(1-probability, rounds-x)
13         for i in range((int)(c * p * q * rounds)):
14             calc.append(x)
15 #This prints out graph
16     b = range(-1,17)
17     h1, bin_edges = np.histogram(calc, b)
18     b1 = bin_edges[0:17]
19
20     plt.stem(b1, h1/rounds)
21     plt.title("Probability Mass Function")
22     plt.ylabel("Probability of success")
23     plt.xlabel("Number of successes in n=1000 trials")
24
25 CalcBinomial(1000)

```

c) Code for #3

```

1 import numpy as np
2 import matplotlib.pyplot as plt
3 def CalcPoisson(rounds):
4     probability = 1/216
5     lamda = probability * rounds
6     PoissonNum = []
7     e = 2.718281
8
9     for x in range(17):
10         lamda2 = np.power(lamda,x)
11         e2 = np.power(e,lamda)
12         factorial = np.math.factorial(x)
13         Poisson = (int)(lamda2*rounds/factorial*e2)
14         for i in range(Poisson):
15             PoissonNum.append(x)
16         #This prints the graph
17         b = range(-1,16)
18         h1, bin_edges = np.histogram(PoissonNum, bins = b)
19         b1 = bin_edges[0:16]
20
21         #plot
22         plt.stem(b1, h1/rounds)
23         plt.title("Probability Mass Function")
24         plt.ylabel("Probability of success")
25         plt.xlabel("Number of successes in n = 1000 trials")
26
27         #show graph
28         plt.show()
29 CalcPoisson(1000)

```