

Quiz 9

Deadline	Wednesday, 23 October 2019 at 4:00PM
Latest Submission	<i>no submission yet</i>
Maximum Mark	5

Question 1 (1 mark)

True or false:

The following approach establishes that $P(n)$ holds for all $n \in \mathbb{N}$:

- Show $P(0)$ holds
- Show if $P(n)$ holds for $n \geq 0$ then $P(2n)$ holds
- Show if $P(n)$ holds for $n \geq 0$ then $P(n-1)$ holds

(a) <input type="radio"/>	True
(b) <input type="radio"/>	False

Question 2 (1 mark)

True or false:

The following approach establishes that $P(n)$ holds for all $n \in \mathbb{N}$:

- Show $P(0)$ holds
- Show $P(1)$ holds
- Show that if $P(a)$ holds and $P(b)$ holds for $a, b \geq 0$ then $P(a+b)$ holds

(a) <input type="radio"/>	True
(b) <input type="radio"/>	False

Question 3 (1 mark)

True or false:

The following establishes that $P(w)$ holds for all $w \in \Sigma^*$

- Show $P(a)$ holds for all $a \in \Sigma$
- Show if $P(aw)$ holds then $P(w)$ holds for all $a \in \Sigma$ and all $w \in \Sigma^*$
- Show if $P(w)$ holds then $P(abw)$ holds for all $a, b \in \Sigma$ and all $w \in \Sigma^*$

(a) <input type="radio"/>	True
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(b) ☐

False

Question 4 (2 marks)

Recall the definition of a **well-formed formula** (over a set Prop):

- \top is a well-formed formula
- \perp is a well-formed formula
- p is a well-formed formula for all $p \in \text{Prop}$
- If ϕ is a well-formed formula, then $\neg\phi$ is a well-formed formula
- If ϕ and ψ are well formed formulas, then:
 - $\phi \vee \psi$ is a well-formed formula
 - $\phi \wedge \psi$ is a well-formed formula
 - $\phi \rightarrow \psi$ is a well-formed formula
 - $\phi \leftrightarrow \psi$ is a well-formed formula

Fill in the blanks to complete the following statement (you may wish to use copy-paste to get the correct symbols):

In order to show that $P(\phi)$ holds for all well-formed formulas ϕ , we show:

- $P(\top)$ holds
- $P(\perp)$ holds

Enter response

holds for all $p \in P$

- If $P(\phi)$ holds then $P(\neg\phi)$ holds
- If

Enter response

and

Enter response

hold then:

- $P(\phi \vee \psi)$ holds

Enter response

holds

Enter response

holds, and

Enter response

holds

✓ Submit