

# SUBJECTIVE TYPE

## PART-I

### SHORT ANSWERS

#### Q.NO.1

#### SPEED OF SPHERE

Speed of sphere is  $\sqrt{\frac{10}{7}gh}$

proof

Linear Rotational kinetic energy =  $\frac{1}{2}mv^2$  — (i)

Rotational kinetic energy =  $\frac{1}{2}I\omega^2$  — (ii)

$\therefore I$  for sphere =  $\frac{2}{5}mR^2$

putting value of  $I$  in eq (ii)

$$\frac{1}{2} \left( \frac{2}{5}mR^2 \right) \omega^2$$

$$\frac{1}{5}mR^2\omega^2$$

$$\therefore v = R\omega$$

$$\therefore v^2 = R^2\omega^2$$

$$\frac{1}{5}mv^2$$

$$\begin{aligned} \text{Total kinetic energy} &= K.E_{\text{linear}} + K.E_{\text{rot}} \\ &= \frac{1}{2}mv^2 + \frac{1}{5}mv^2 \end{aligned}$$

$$= \frac{5mv^2 + 2mv^2}{10}$$



$$\frac{10mv^2}{10} = \frac{7mv^2}{10}$$

According to law of conservation of angular momentum

P.E at top = K.E at bottom

$$mgh = \frac{7mv^2}{10}$$

$$gh = \frac{7v^2}{10}$$

$$\frac{10gh}{7} = v^2$$

Taking square root on both sides

$$\sqrt{v^2} = \sqrt{\frac{10gh}{7}}$$

$$v = \sqrt{\frac{10gh}{7}}$$

Q.NO.2

## CRITICAL VELOCITY

The minimum velocity which is required to set a satellite in orbit is called critical velocity. Critical velocity is  $7.9 \text{ km/s}$

Proof

$$\therefore \text{orbital velocity} = \sqrt{\frac{GM}{r}}$$

$$\therefore \text{orbital velocity} = \sqrt{gR}$$

$$= \sqrt{(9.8)(6.4 \times 10^6)}$$

$$= \sqrt{9.8 \times 6.4 \times 10^6}$$

$$= 7.9 \text{ km/s}$$

Q.NO.3

## WEIGHT IN LIFT

Condition:

Body is moving upward  
 $a = g$ .

$T - W = \text{net force}$

$$T - W = ma$$

$$T - W = mg \quad \because g = a$$

$$T = W + mg \quad \because mg = W$$

$$T = W + W$$

$$T = 2W$$

hence, weight is  $2W$

Q.NO.6

## NUMERICAL

GIVEN:

Diameter = length of arc =  $2.50 \text{ m}$

angle =  $\theta = 6.6 \times 10^{-9} \text{ rad}$

To find:

Distance =  $r = ?$

Solution:

$$S = r\theta$$

$$\frac{S}{\theta} = r$$

$$\frac{2.50}{6.6 \times 10^{-9}} = r$$

$$r = 3.787 \times 10^8 \text{ m}$$

## NUMERICAL

GIVEN:

$$v = 100 \text{ km/s}$$

$$r = 390400 \text{ km}$$

TO FIND,

$$T = ?$$

Solution

$$T = \frac{2\pi r}{v}$$

$$T = \frac{2(3.14)(390400)}{(100)}$$

$$T = 2427437 \text{ sec}$$

converting sec into days

$$\frac{2427437}{60 \times 60 \times 24}$$

$$= 28 \text{ days}$$

Q.NO.3

~~GEOSTATIONARY SATE~~  
HEIGHT OF SATELLITE

$$r = \left[ \frac{GMT^2}{4\pi^2} \right]^{1/3}$$

$$\text{or } r = R + h$$

$$h = r - R$$

$$h = \left[ \frac{GMT^2}{4\pi^2} \right]^{1/3} - 6400$$

Putting the value we get  
64000



Q.NO.7

## NUMERICAL

GIVEN.

$$r = 3.85 \times 10^8 \text{ m}$$

$$R = 1.74 \times 10^6 \text{ m}$$

$$\frac{L_o}{L_s}$$

$$\therefore L_s = I \omega^2$$

$$\therefore I = \frac{2\pi m R^2}{5}$$

$$L_o = M r^2 \omega$$

$$\frac{L_o}{L_s} = \frac{2\pi M r^2 \omega}{5 M R^2 \omega}$$

$$\frac{L_o}{L_s} = \frac{2r^2}{5R^2}$$

$$\frac{L_o}{L_s} = \frac{2(3.85 \times 10^8)^2}{5(1.74 \times 10^6)^2}$$

$$\frac{L_o}{L_s} = \frac{2(1.48225 \times 10^{17})}{5(3.0276 \times 10^{12})}$$

$$\frac{L_o}{L_s} = \frac{2.9645 \times 10^{17}}{1.5138 \times 10^{13}}$$

$$\frac{L_o}{L_s} = 1.9583 \times 10^4$$