



LGS GROUP OF COLLEGES

A PROJECT OF LAHORE GRAMMAR SCHOOL

Sheet # _____

Name: M. Mujtaba Smtiaz Class: 12th Roll No. _____

Subject: Math Test No. _____ Date: _____

A	B	C	D	A	B	C	D	A	B	C	D	A	B	C	D	Marks Obtained	
1				6				11				16					
2				7				12				17					
3				8				13				18					
4				9				14				19					
5				10				15				20					

Q1: —

 {i}
 $y = \sqrt{x}$, when x changes from 4 to 4.41.

As 'x' changes from 4 to 4.41, so,

$$y + \delta y = \sqrt{x + \delta x}$$

so, $x = 4$ and $\delta x = 4.41 - 4 = 0.41$

$$y + \delta y = \sqrt{4 + 0.41}$$

$$\delta y = \sqrt{4 + 0.41} - \sqrt{x}$$

$$\therefore y = \sqrt{x}$$

$$\delta y = \sqrt{4.41} - \sqrt{4}$$

$$\delta y = 2.1 - 2$$

$$\delta y = 0.1$$

$$\delta y = 0.1$$

 {ii}

$$xy - \ln x = c$$

diff on b/s

$$d(xy) - d(\ln x) = d(c)$$

$$x dy + y dx - \frac{1}{x} dx = 0$$

Multiplying 'x' on b/s

$$x^2 dy + xy dx - dx = 0$$

so,

$$x^2 dy = dx - xy dx$$

$$x^2 dy = dx(1 - xy)$$

$$\frac{dy}{dx} = \frac{1 - xy}{x^2}$$



$$\frac{dy}{dx} = \frac{1-xy}{x^2}$$

{iii}

$$= \int \frac{(\sqrt{\theta}-1)^2}{\sqrt{\theta}} d\theta$$

$$= \int \frac{(\theta + 1 - 2\sqrt{\theta})}{\sqrt{\theta}} d\theta$$

$$= \int \left(\frac{\theta}{\sqrt{\theta}} + \frac{1}{\sqrt{\theta}} - \frac{2\sqrt{\theta}}{\sqrt{\theta}} \right) d\theta$$

$$= \int (\theta^{1/2} + \theta^{-1/2} - 2) d\theta$$

$$= \int \theta^{1/2} d\theta + \int \theta^{-1/2} d\theta - 2 \int d\theta$$

$$= \int \theta^{1/2} d\theta + \int \theta^{-1/2} d\theta - 2 \int d\theta$$

$$= \frac{\theta^{3/2}}{3/2} + \frac{\theta^{1/2}}{1/2} - 2\theta = \frac{2\theta^{3/2}}{3} + \frac{2\theta^{1/2}}{1} - 2\theta$$

$$= \frac{2\theta^{3/2}}{3} + 2\theta^{1/2} - 2\theta + C$$

Long Ques:-

(3)

$$= \int \frac{\cos 2x - 1}{1 + \cos 2x} dx = \int \frac{-(1 - \cos 2x)}{(1 + \cos 2x)} dx \quad \because 1 - \cos 2x = 2\sin^2 x$$

$$= - \int \frac{(1 - \cos 2x)}{(1 + \cos 2x)} dx = - \int \frac{(2\sin^2 x)}{2\cos^2 x} dx = - \int \tan^2 x dx$$

$$= - \int (\sec^2 x - 1) dx \quad \because \sec^2 x - \tan^2 x = 1$$

$$= - \int \sec^2 x - (-1) \int dx = -\tan x + 1x + C$$

$$= x - \tan x + C$$