

Physics (Assignment WK-5)

Question 1:

When an object rolls without slipping, its total mechanical energy is conserved. This includes both translational and rotational kinetic energy.

1. Initial Energy at Height

- The sphere starts from rest, so its initial kinetic energy is zero.
- Its potential energy is mgh , where m is the mass, g is acceleration due to gravity, and h is height.

2. Energy at Bottom

- At the bottom, the potential energy is zero.
- The kinetic energy is combination of translational kinetic energy ($\frac{1}{2}mv^2$) and rotational kinetic energy ($\frac{1}{2}I\omega^2$), where I is the moment of inertia and ω is angular velocity.

For a solid sphere, the moment of

Moment of Inertia I is $\frac{2}{5} mr^2$ and the relationship between ω the angular velocity, the moment of Inertia I is $\omega = \frac{v}{r}$

The total energy at the bottom is

$$\frac{1}{2} mv^2 + \left(\frac{2}{5} mr^2 \right) \left(\frac{v}{r} \right)^2$$

Simplifying the rotational kinetic energy

$$\text{term: } \frac{1}{2} \frac{2}{5} mr^2 \frac{v^2}{r^2} = \frac{1}{5} mv^2$$

So, the total kinetic energy at the bottom is:

$$\frac{1}{2} mv^2 + \frac{1}{5} mv^2 = \frac{7}{10} mv^2$$

Question 2.

For an object to be in a stable low earth orbit, this velocity can be calculated using the formula for orbital velocity:

$$\text{velocity} = \sqrt{\frac{GM}{r}}$$

Where:

- G is the gravitational constant.
 $6.674 \times 10^{-11} \text{ Nm}^2/\text{kg}^2$

- M is the mass of earth
approximately $5.972 \times 10^{24} \text{ kg}$.

- r is the distance from the centre of the earth to the object, which for a low earth orbit is roughly equal to the Earth radius plus the altitude of the orbital / ranging from about 200km to 2000km above the Earth's surface. However, to simplify we often use the Earth radius ($6.371 \times 10^6 \text{ m}$) for basic calculation. using the approximate values, we can calculate.

$$v_{\text{circular}} \approx \sqrt{\frac{(6.674 \times 10^{-11}) (5.972 \times 10^{24})}{6.371 \times 10^6}}$$

When you complete this, you find that $v_{\text{circular}} = 7000 \text{ m/s}$.

Since 7000 m/s is essentially 7.9 km/s .

Question.no.3

We can use the concept of apparent weight.

1. Understanding Weight in Physics

- The actual weight W of a person is the gravitational force acting on them, which is mg , where m is the mass of a person and g is the acceleration due to gravity.

2. Apparent weight in an Elevator

- When the elevator is at rest or moving at a constant velocity, the apparent weight is equal to actual weight
- When the elevator accelerates, the apparent weight is the normal

Force N exerted by the floor. This changes due to the acceleration of the elevator.

3. Elevator Accelerating Upward

• If the elevator accelerates upward with acceleration a , the apparent weight can be expressed using Newton's second law:

$$N = m(g + a)$$

• In this case, a is equal to g .
Therefore:

$$N = m(g + g) = 2mg$$

• Thus, the apparent weight N becomes $2W$, since $W = mg$ the person's weight

Thus, when in the elevator will be $2W$ when the elevator is accelerating upward with an acceleration equal to g .

Question no. 4

Given:

- Speed of the satellite, $v = 1.01 \text{ km/s}$
- Radius of the orbit, $r = 39,040 \text{ km}$

To find the time T it takes for the satellite to complete one revolution, we use the formula for the circumference of the orbit and the relationship between distance, speed and time.

$$C = 2\pi r$$

$$T = \frac{C}{v} = \frac{2\pi r}{v}$$

First let's calculate the circumference:

$$C = 2\pi \times 390,400 \text{ km} \approx 2,452,629 \text{ km}$$

Now, the time to complete one revolution:

$$T = \frac{2,452,629 \text{ km}}{1.01 \text{ km/s}}$$

$$T \approx 2,428,347 \text{ s}$$

To convert seconds into days:

$$T \approx \frac{2,428,347 \text{ s}}{86400} \approx 28.11 \text{ days}$$

Therefore, the satellite will complete one revolution approximately every 28.11 days.

Question no. 5

The formula for the orbital radius r of a geostationary satellite is given by:

$$r = \left(\frac{GMT^2}{4\pi^2} \right)^{1/3}$$

Where,

- G is the gravitational constant ($6.674 \times 10^{-11} \text{ m}^3/\text{kg s}^2$).
- M is the mass of earth $5.972 \times 10^{24} \text{ kg}$
- T is the orbital period (one sidereal day in seconds: 86164 s).

Given these values, we compute the orbital radius r :



$$r = \left(\frac{16.674 \times 10^{-11} \times 15.972 \times 10^{24} \times (86164)}{4\pi^2} \right)$$

Upon calculating this, we find:
 $r = 42,164 \text{ km.}$

This is the distance from the center of the Earth.

Question no. 6

Given:-

Diameter of beam = length of arc = $S = 2.50 \text{ m}$

Distance of moon from the earth = $r = 3.8 \times 10^8 \text{ m}$

Find:-

Divergence angle = $\theta = ?$

Calculation:-

$$\text{As } \therefore S = r\theta$$

$$\theta = \frac{S}{r}$$

Putting values, we get

$$\theta = \frac{2.50}{3.8 \times 10^8}$$

$$\theta = 6.6 \times 10^{-9} \text{ rad.}$$



Question no. 7

Given:-

Distance between Earth and the Moon = $r_0 = 3.85 \times 10^8 \text{ m}$

Radius of the moon = $r_s = 1.74 \times 10^6 \text{ m}$

Find:-

Ratio of spin and orbital angular = $\frac{L_s}{L_o} = ?$

Calculation:-

The spin angular momentum of the Moon about its own axis is

$$L_s = I_s \omega$$

$$L_s = \frac{2}{5} m r_s^2 \omega \dots (1)$$

The orbital angular momentum is given by

$$L_o = I_o \omega$$

$$L_o = m r_0^2 \omega \dots (2)$$

Dividing equation (1) by equation (2) we get

$$\frac{L_s}{L_o} = \frac{\frac{2}{5} m r_s^2 \omega}{m r_0^2 \omega}$$

$$\frac{L_s}{L_o} = \frac{2}{5} \frac{r_s^2}{r_0^2}$$

putting values, we get

$$\frac{L_s}{L_o} = \frac{2}{5} \frac{(1.74 \times 10^6)^2}{(3.85 \times 10^8)^2}$$

$$\frac{L_s}{L_o} = 8.2 \times 10^{-6}$$