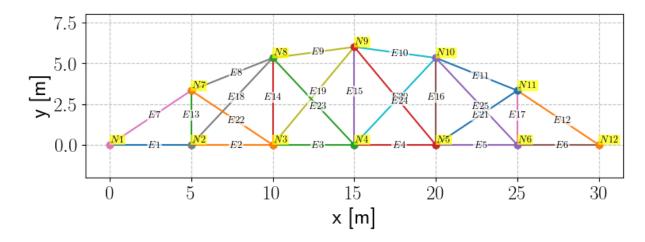
Linear elastic static and modal analysis of a bridge

This example is the python version of the fenicsx tutorial by Jeremy Bleyer https://bleyerj.github.io/comet-fenicsx/tours/beams/linear_truss/linear_truss.html

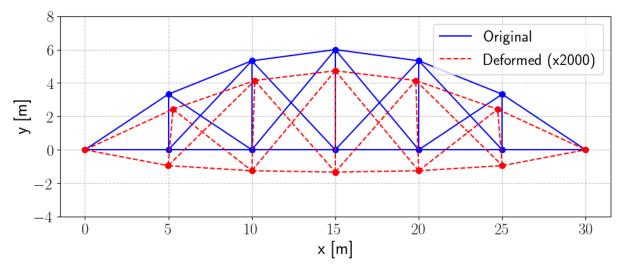
In this way you can compare a native python implementation with the fenicsx one.

```
In [1]: # As usual we start by generating the coordinates and mesh
        import numpy as np
        from src.postprocessing.plot mesh import plot truss structure 2d
        import matplotlib.pyplot as plt
        # Define parameters
        E = 200e3 \# [Pa]
        A = 1 # [m^2]
        EA = E * A
        l = 5.0
        h1 = 3.33
        h2 = 5.33
        h3 = 6.0
        # Node coordinates
        bottom indices = np.arange(1, 6)
        top indices = np.arange(6, 11)
        # Create coordinates matrix
        n nodes = 12
        coordinates = np.zeros((n nodes, 2))
        # Assign coordinates
        # Left (first node) and right (last) points
        left id = 0
        right id = 11
        coordinates[left id] = [0.0, 0.0]
        coordinates[right id] = [6*1, 0.0]
        # Bottom points
        for i in bottom indices:
            coordinates[i] = [i*l, 0.0]
        # Top points
        for i, coord id in enumerate(top indices):
            h i = [h1, h2, h3, h2, h1][i]
            coordinates[coord id] = [(i+1)*l, h i]
        # Create connectivity table
```

```
num bottom lines = 6 # left + 5 bottom points + right = 7 points, 6 l
                            # left + 5 top points + right = 7 points, 6 line
num top lines = 6
num vertical lines = 5
num diagonal lines = 4 * 2 # 4 left diagonals + 4 right diagonals
n elements = num bottom lines + num top lines + num vertical lines + num dia
connectivity table = np.zeros((n elements, 2), dtype=int)
element id = 0
# Bottom lines
for i in range(num bottom lines):
   if i == 0:
       # First bottom line connects left to first bottom point
        connectivity table[element id] = [left id, bottom indices[0]]
   elif i == num bottom lines - 1:
       # Last bottom line connects last bottom point to right
        connectivity table[element id] = [bottom indices[-1], right id]
   else:
        # Middle bottom lines connect adjacent bottom points
        connectivity table[element id] = [bottom indices[i-1], bottom indice
   element id +=1
# Top lines
for i in range(num top lines):
   if i == 0:
       # First top line connects left to first top point
        connectivity table[element id] = [0, top indices[0]]
   elif i == num top lines - 1:
       # Last top line connects last top point to right
        connectivity table[element id] = [top indices[-1], right id]
   else:
        # Middle top lines connect adjacent top points
        connectivity table[element id] = [top indices[i-1], top indices[i]]
   element id +=1
# Vertical lines
for i in range(num vertical lines):
   connectivity table[element id] = [bottom indices[i], top indices[i]]
   element id +=1
# Right diagonal lines (bottom to top)
for i in range(num vertical lines - 1):
    connectivity table[element id] = [bottom indices[i], top indices[i+1]]
   element id +=1
# Left diagonal lines (top to bottom)
for i in range(num vertical lines - 1):
   connectivity table[element id] = [top indices[i], bottom indices[i+1]]
   element id += 1
# plt.plot(coordinates[:, 0], coordinates[:, 1], 'o')
ax = plot truss structure 2d(coordinates, connectivity table,
                        xlabel='x [m]',
                        ylabel='y [m]',
                        ylim=[-2, 8])
```



```
In [3]: from src.fem.assemble matrices import assemble stiffness truss 2d
        from src.fem.solve system import solve system homogeneous bcs
        n dofs = n nodes*2
        f = np.zeros(n dofs)
        # Set vertical force on the vertical dofs of the bottom nodes
        for i in bottom indices:
            f[i*2+1] = -1
        dofs bcs = [2*left id, 2*left id+1, 2*right id, 2*right id+1]
        K = assemble stiffness truss 2d(coordinates, connectivity table, EA)
        q all, reactions = solve system homogeneous bcs(K, f, dofs bcs)
        # print(f"Displacement at these nodes [m]:\n {q all}\n")
        # print(f"Reactions at bcs in [N]:\n {reactions}\n")
        fig, ax = plt.subplots(figsize=(10, 8))
        ax = plot truss structure 2d(coordinates, connectivity table, ax=ax,
                show element labels=False,
                show_node_labels=False,
                color='blue',
                linestyle='o-',
                label='Original',
                xlabel='x [m]',
                ylabel='y [m]',
                ylim=[-4, 8])
        scale = 2000
        deformed coordinates = coordinates + scale * q all.reshape(-1, 2)
        ax = plot truss structure 2d(deformed coordinates, connectivity table, ax=ax
                linestyle='o--',
                show element labels=False,
                show node labels=False,
                label=f'Deformed (x{scale})')
        plt.tight layout()
        plt.show()
```



In []: