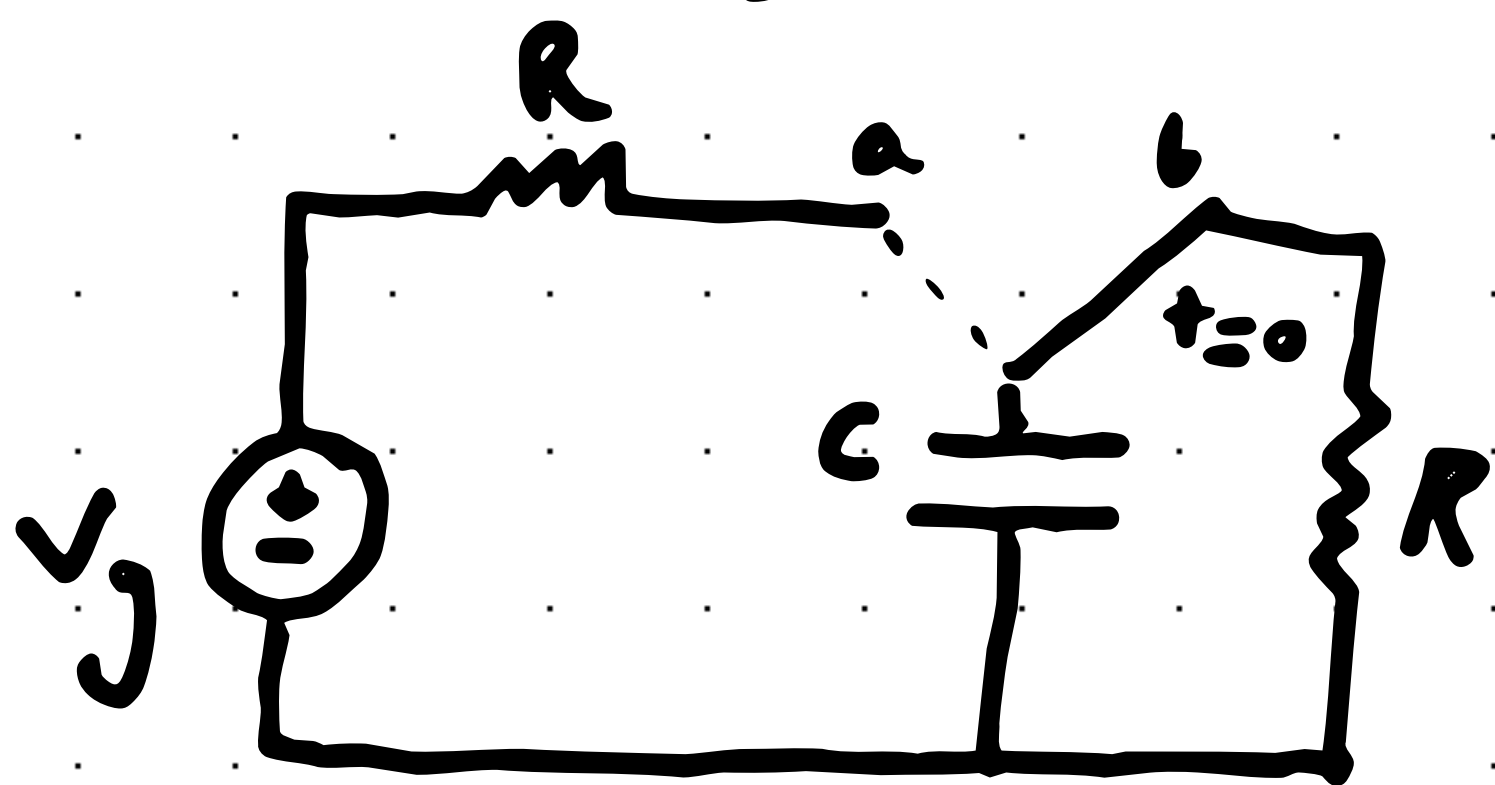


The Natural Response of an RC Circuit

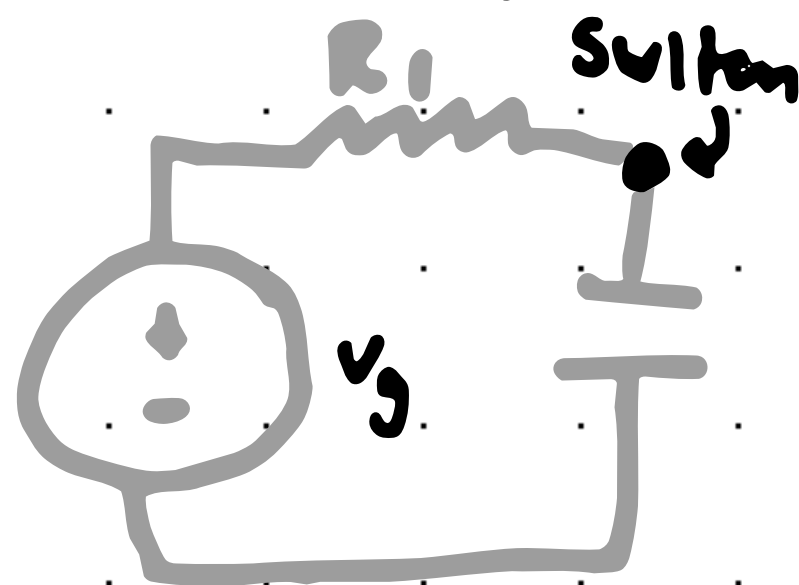
- Forced Response means source after closing the switch

- Natural Response means no source after closing the switch.



At $t=0$, the switch is moved to position B.

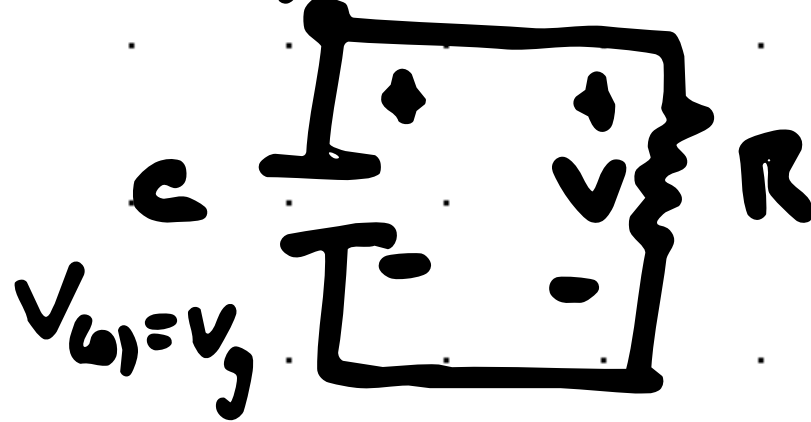
Before moving the switch



At $t=0$, the switch moved.

So the initial charge for the capacitor is V_g

After moving the switch

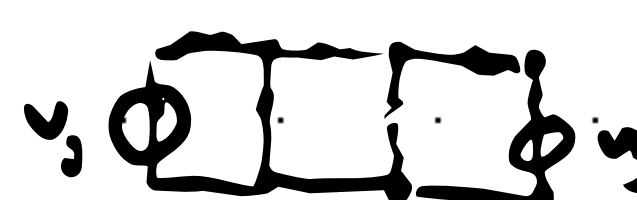


$$V_{(t)} = V_{(0)} e^{-\frac{t}{RC}}$$

$$\frac{V}{R} + C \frac{dV}{dt} = 0$$

same to above P.E

Lab Test Checklist

- 1) • Create circuit

 • Parallelized for blowing fuse
 • (parallel vs series for voltage)
 • Can sit anywhere

2) and 3)

Based on lab questions.

- R Time for example
- Superposition
- OP AMPS
- oscilloscope
- R_g and R_L

The voltage across the capacitor is not changing instantaneously, so $V_c(0^+) = V_c(0^-) = V_c(0)$

The current is changing across the

Assume

$$\tau = RC \quad \text{time constant}$$

$0_+ = \text{Immediately after closing switch}$

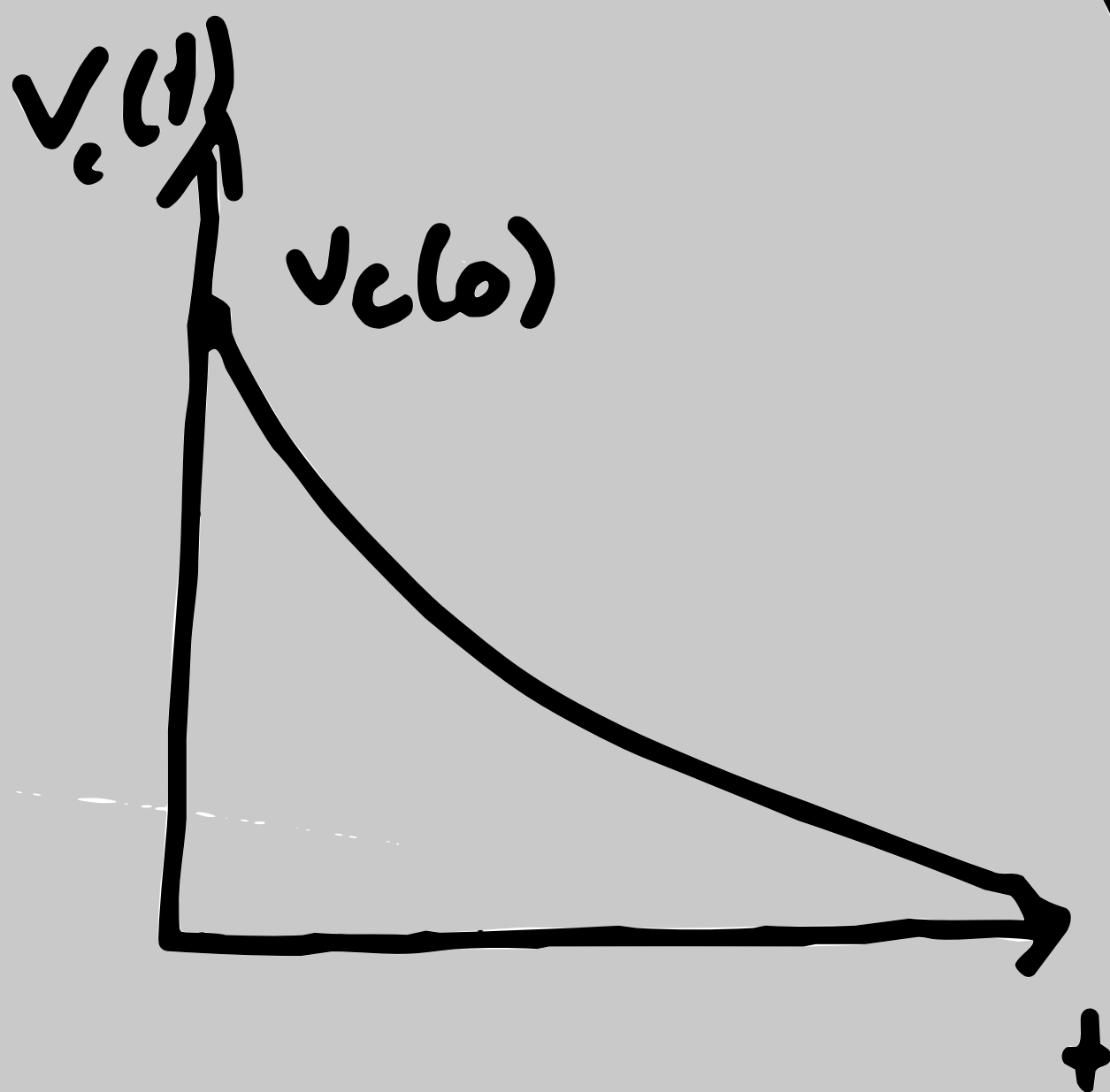
$0_- = \text{Immediately before closing switch}$

$$V_c(t) = V_c(0) e^{-\frac{t}{\tau}}$$

$$i(t) = \frac{v(t)}{R} = \frac{V_c(0)}{R} e^{-\frac{t}{\tau}}$$

$$P_c(t) = \frac{V_c(0)^2}{R} e^{-\frac{2t}{\tau}}$$

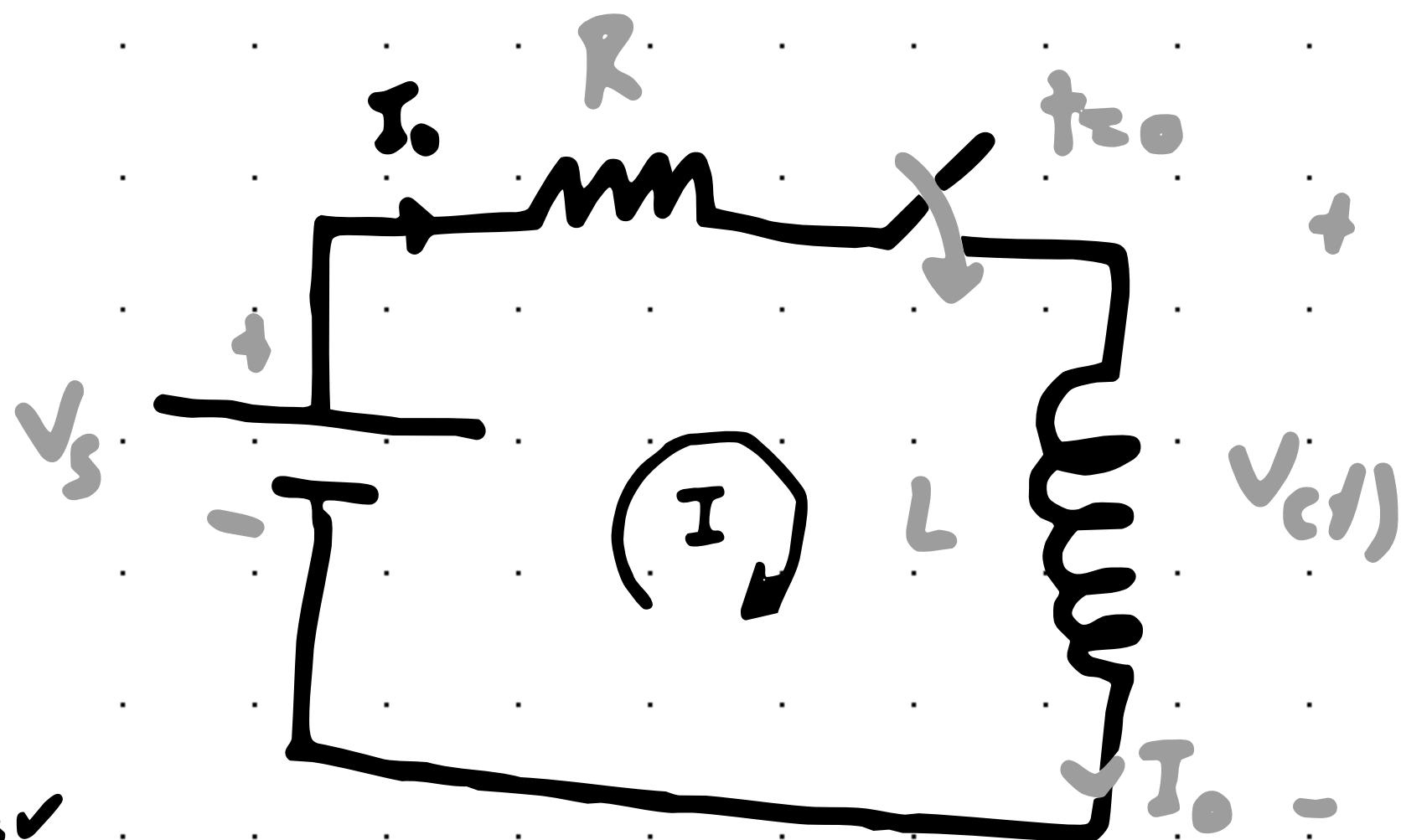
$$W_c(t) = \int_0^t P_c(t) dt = \frac{1}{2} C (V_c(0))^2 (1 - e^{-\frac{2t}{\tau}})$$



Step Response of RL

$$\sum_{\text{loop}} V = 0$$

$$V_s = IR + L \frac{di}{dt} \quad \leftarrow \text{First Order DE}$$



$$\frac{di}{dt} = \frac{-Ri + V_s}{L} = -\frac{R}{L} \left(i - \frac{V_s}{R} \right)$$

$$\int_{I_0}^{I(t)} \frac{di}{\left(i - \frac{V_s}{R} \right)} = -\int_{t_0}^t \frac{R}{L} dt \rightarrow \ln \left(i - \frac{V_s}{R} \right) \bigg|_{I_0}^{I(t)} = -\frac{R}{L} t \bigg|_{t_0}^t$$

$$\left(\frac{i(t) - \frac{V_s}{R}}{I_0 - \frac{V_s}{R}} \right) = e^{-\frac{R}{L}(t-t_0)}$$

For simplicity, if $t_0 = 0$ then $\sim e^{-\frac{R}{L}t}$

$$I(t) = \frac{V_s}{R} + \left(I_0 - \frac{V_s}{R} \right) e^{-\frac{R}{L}t}$$

↑

↑

Natural Response

* when the source, this equal zero.
So happens to be the natural response!
Eqn

General Eqn
for step and
natural.

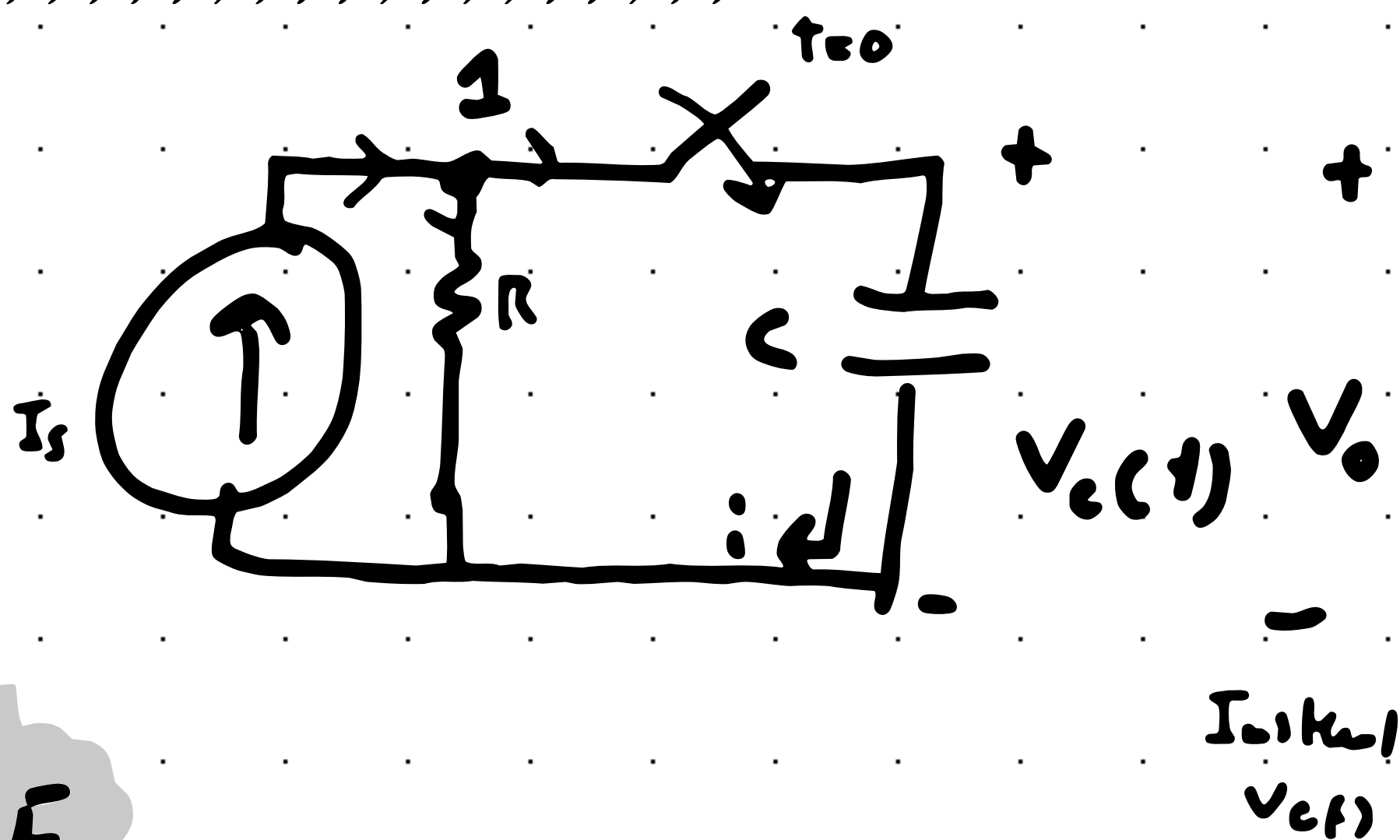
$$V(t) = L \frac{di}{dt} = L(-R)(I_0 - \frac{V_s}{R}) e^{-\frac{R}{L}t} +$$

$$= (V_s - I_0 R) e^{(-\frac{R}{L}t)} +$$

b) Step Response of RC Circuit

$$\sum I = 0$$

Node 1



$$I_s = \frac{V_o}{R} + C \frac{dV_c}{dt}$$

D.E

Initial $V_c(t)$

$$\frac{dV_c}{dt} + \frac{V_c}{R_c} = \frac{I_s}{C}$$

$$V_c(t) = I_s R + (V_o - I_s R) e^{-\frac{t}{R_c}} \quad t \geq 0$$

$$i_c(t) = (I_s - \frac{V_o}{R}) e^{-\frac{t}{R_c}} \quad t \geq 0^+$$

Now, we only ever derived these equations for one resistor, and inductor. What I'll do in tomorrow's notes, is show how to create an equivalent system....

