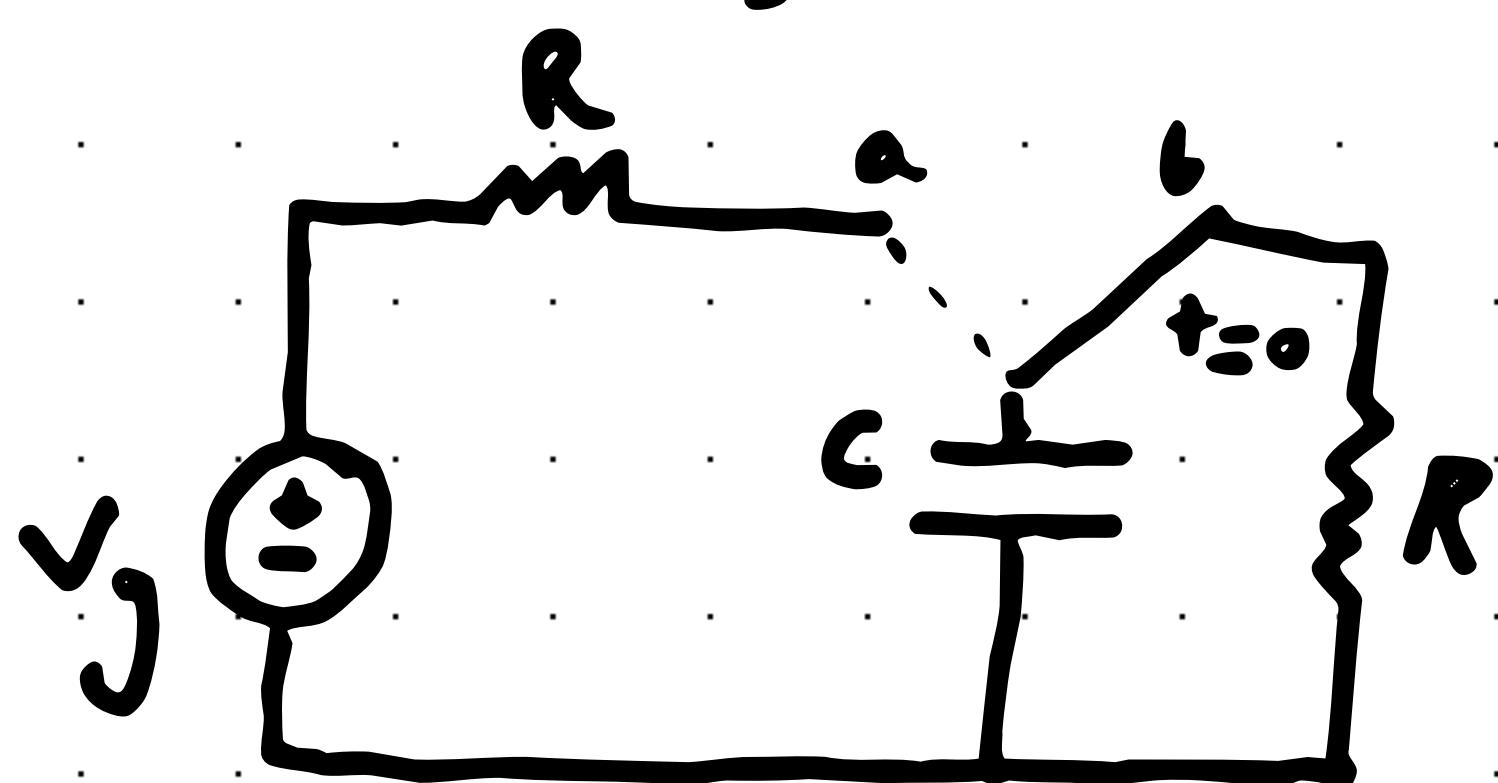


The Natural Response of an RC Circuit

- Forced Response Means Source after closing the switch
- Natural Response Means no source after closing the switch.

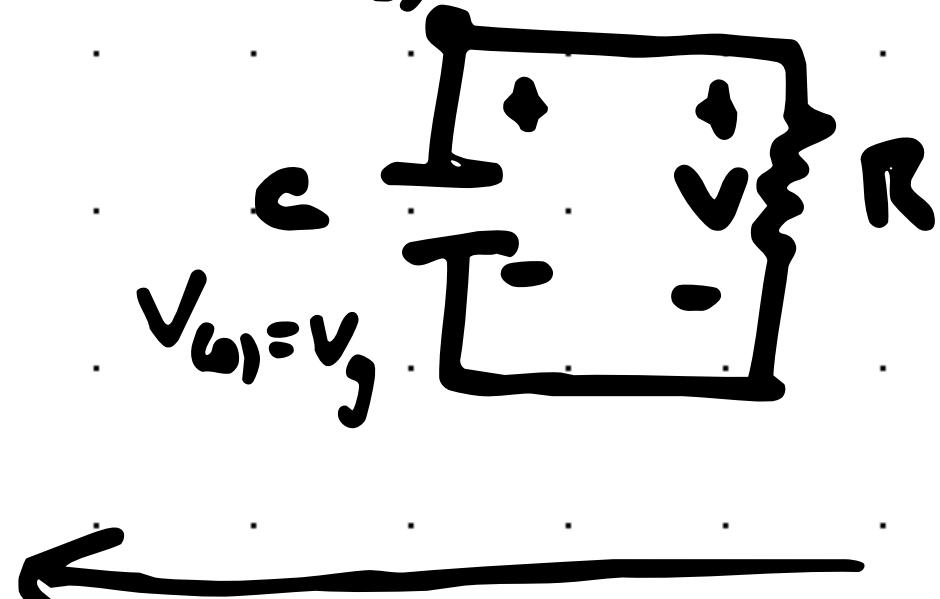


At $t=0$, the switch is moved to position B.

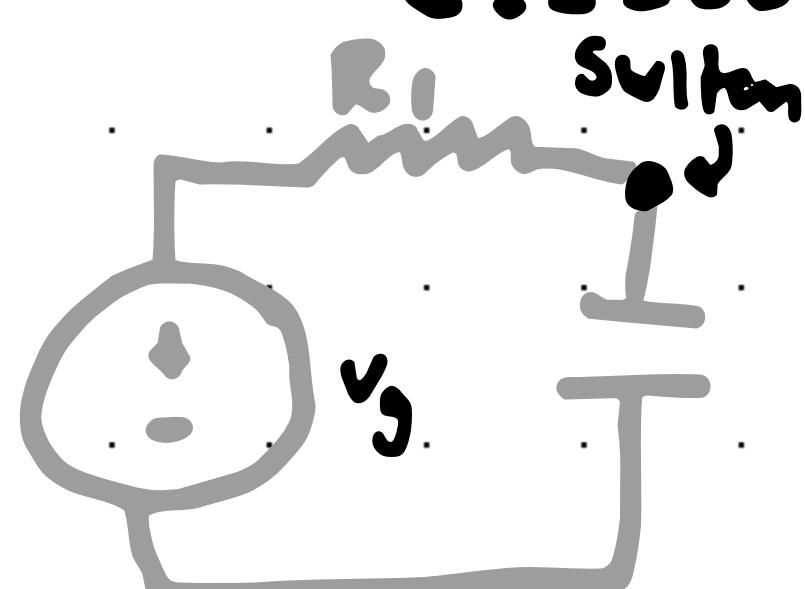
Before moving the switch

After Moving the Switch

$$V_{(1)} = V_{in} e^{-\frac{t}{RC}}$$



- Lab Test checklist
- i) Create Circuit
 - Parallel circuit
 - Parallel vs Series (for Voltage)
 - Can sit anywhere
- ii) and iii)
 - Based on lab questions.
 - R Tries for Circuit
 - Superposition
 - OP AMPS
 - oscilloscope
 - LC and RL



At $t=0$, the switch moves.

So the initial charge for the capacitor is V_g

$$\frac{V}{R} + C \frac{dV}{dt} = 0$$

Solve the above D.E

The Voltage across the capacitor is first changing instantaneously.

$$\text{So } V_c(+)=V_c(-)=V_c(0)$$

The Current is changing across the

Assume

$$T = RC \text{ C time constant}$$

O_+ = Instantly after closing switch

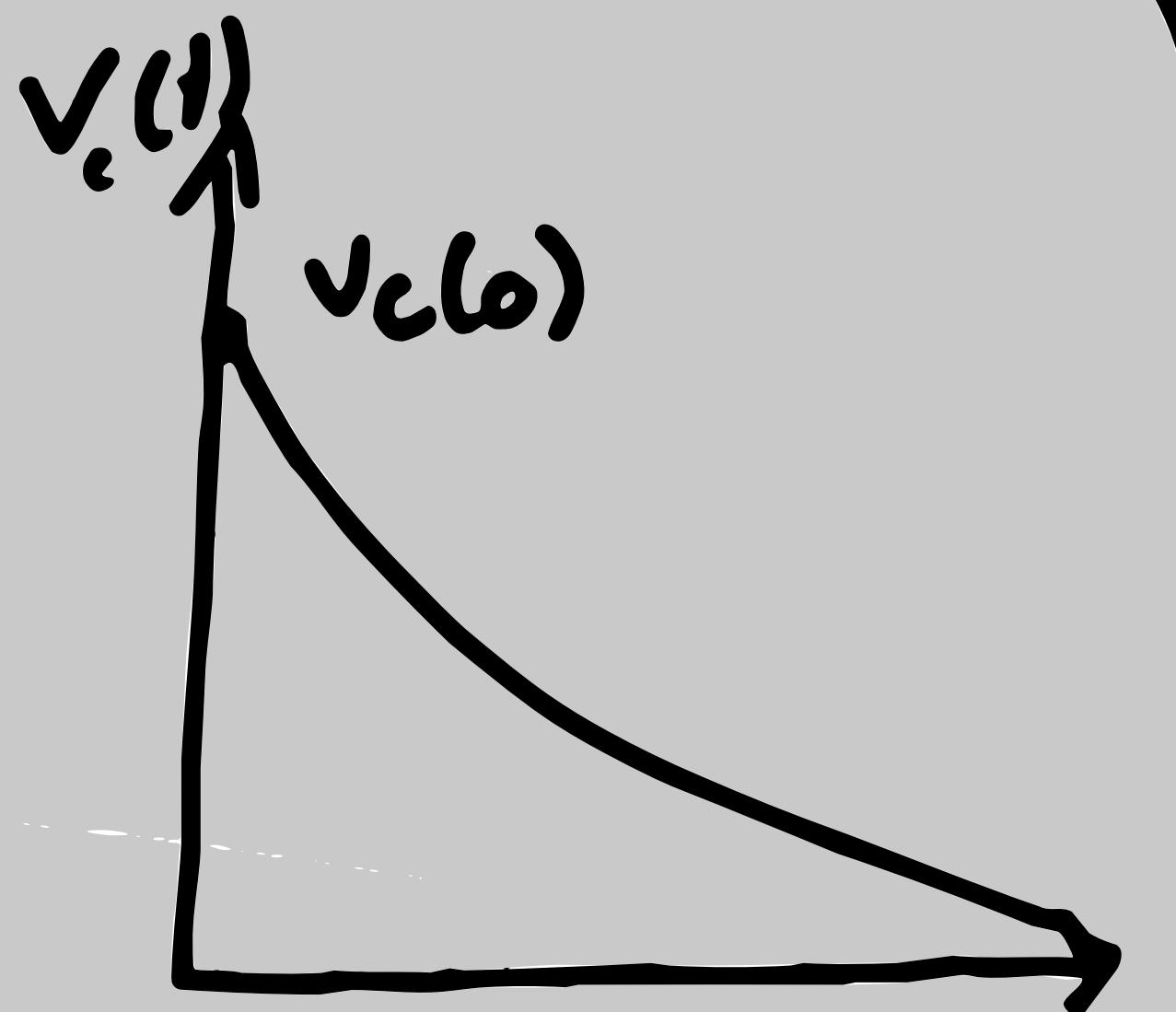
O_- = Instantly before closing switch

$$V_c(t) = V_c(0) e^{-\frac{t}{T}}$$

$$i(t) = \frac{v(t)}{R} = \frac{v(0)}{R} e^{-\frac{t}{T}}$$

$$P_c(t) = \frac{V_c(0)^2}{R} e^{-\frac{2t}{T}}$$

$$W_c(t) = \int P_c(t) dt = \frac{1}{2} C (V_c(0))^2 (1 - e^{-\frac{2t}{T}})$$

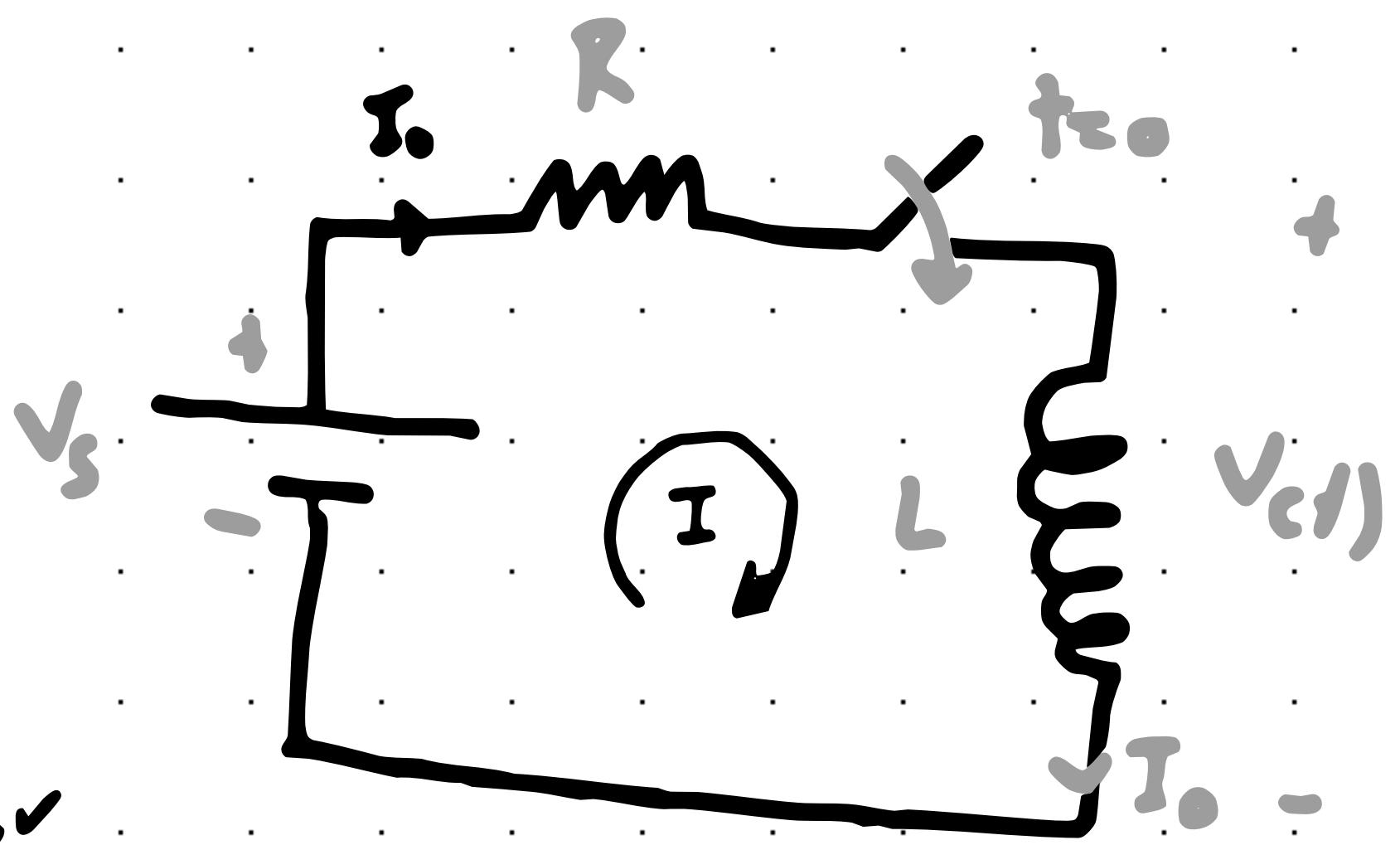


Step Response of RL

$$\sum V = 0$$

imp

$$V_s = IR + L \frac{di}{dt} \quad \leftarrow \text{First Order DE}$$



$$\frac{di}{dt} = -\frac{Ri + V_s}{L} = -\frac{R}{L} \left(i - \frac{V_s}{R} \right)$$

$$\int_{I_0}^I \frac{di}{\left(i - \frac{V_s}{R} \right)} = -\int_{t_0}^t \frac{R}{L} dt \rightarrow \ln \left(i - \frac{V_s}{R} \right) \Big|_{I_0}^I = -\frac{R}{L} t + \Big|_{t_0}^t$$

$$\left(\frac{\left(i(t) - \frac{V_s}{R} \right)}{I_0 - V_s/R} \right) = e^{-\frac{R}{L}(t-t_0)}$$

For simplicity, if $t_0 = 0$ then $\approx e^{-\frac{R}{L}t}$

$$I(t) = \frac{V_s}{R} + \left(I_0 - \frac{V_s}{R} \right) e^{-\frac{R}{L}t}$$



Natural Response

General Eqn
for Step and
natural.

* When DC source, these equal zero.
So happens to be the natural Response Eqn

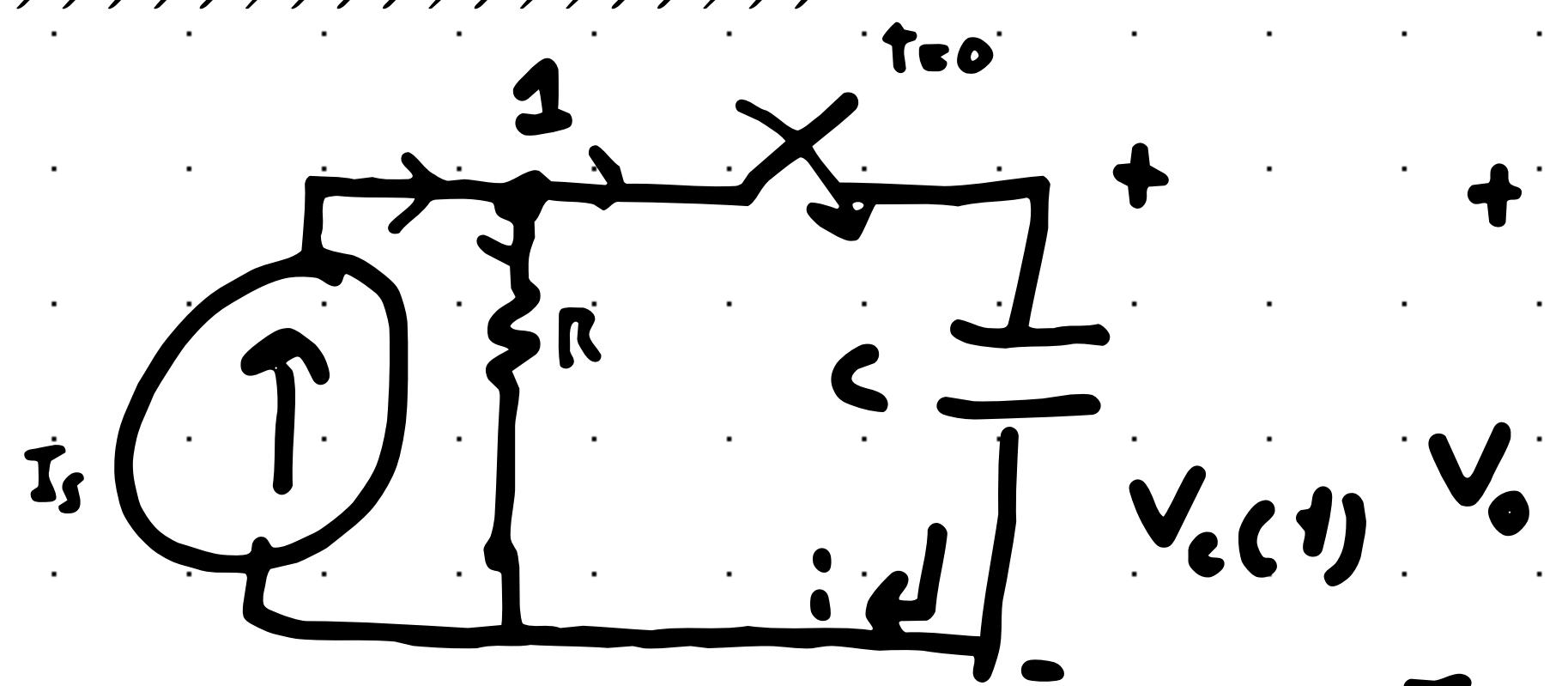
$$V(t) = L \frac{di}{dt} = L(-R)(I_0 - \frac{V_s}{R}) e^{-\frac{R}{L}t} +$$

$$= (V_s - I_0 R) e^{-\frac{R}{L}t} +$$

b) Step Response of RC Circuit

$$\sum I = 0$$

No. 1



$$I_s = \frac{V_0}{R} + C \frac{dV_c}{dt}$$

D.E

$$\frac{dV_c}{dt} + \frac{V_c}{RC} = \frac{I_s}{C}$$

$$V_c(t) = I_s R + (V_0 - I_s R) e^{-\frac{t}{RC}} \quad t \geq 0$$

$$i(t) = (I_s - \frac{V_0}{R}) e^{-\frac{t}{RC}} \quad t \geq 0^+$$



Now, we only have derived these graphs for one resistor, and indeed! but I'll do in tomorrow's notes, is show how to create an equivalent system....

