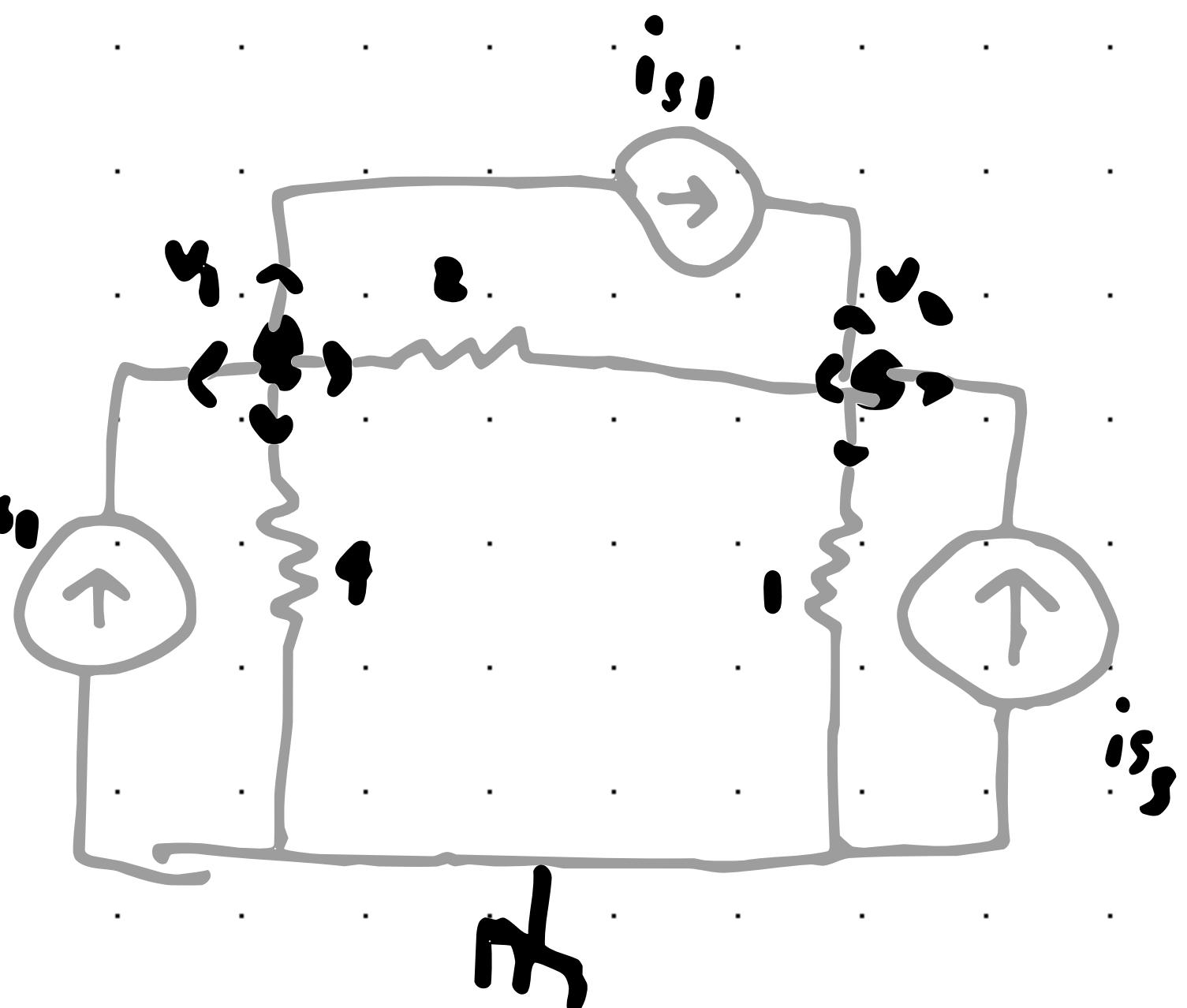


Nodal Analysis

For the following Circuit, write the Nod - Voltage equations.



Solutions

$$\sum \text{I}_{\text{in}} - I_{s_2} + I_{s_1} + \frac{v_1}{4} + \frac{v_1 - v_2}{2} = 0$$

Node 1

$$\sum \text{I}_{\text{out}} = -I_{s_1} - I_{s_3} + \frac{v_1}{1} + \frac{v_2 - v_1}{2} = 0$$

$$\left(\frac{1}{4} + \frac{1}{2}\right)v_1 + \left(-\frac{1}{2}\right)v_2 = i_{s_2} - i_{s_1} \quad ①$$

$$\left(-\frac{1}{2}\right)v_1 + \left(\frac{1}{1} + \frac{1}{2}\right)v_2 = i_{s_1} + i_{s_3} \quad ②$$

$$\left(\frac{1}{4} + \frac{1}{2}\right)V_1 + \left(-\frac{1}{2}\right)V_2 = i_{S_2} - i_{S_1} \quad ①$$

$$\left(-\frac{1}{2}\right)V_1 + \left(\frac{1}{4} + \frac{1}{2}\right)V_2 = i_{S_1} + i_{S_3} \quad ②$$

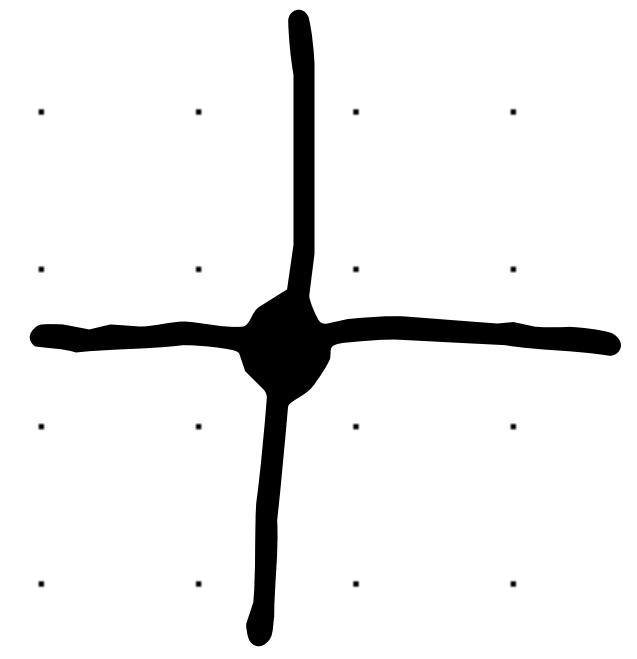
$$\begin{bmatrix} \frac{1}{4} + \frac{1}{2} & -\frac{1}{2} \\ -\frac{1}{2} & \frac{1}{4} + \frac{1}{2} \end{bmatrix} \begin{bmatrix} V_1 \\ V_2 \end{bmatrix} = \begin{bmatrix} i_{S_2} - i_{S_1} \\ i_{S_1} + i_{S_3} \end{bmatrix}$$

This is known as the
Cocientes Method!

Conductance ($G_1 = \frac{1}{R_{S1}}$)

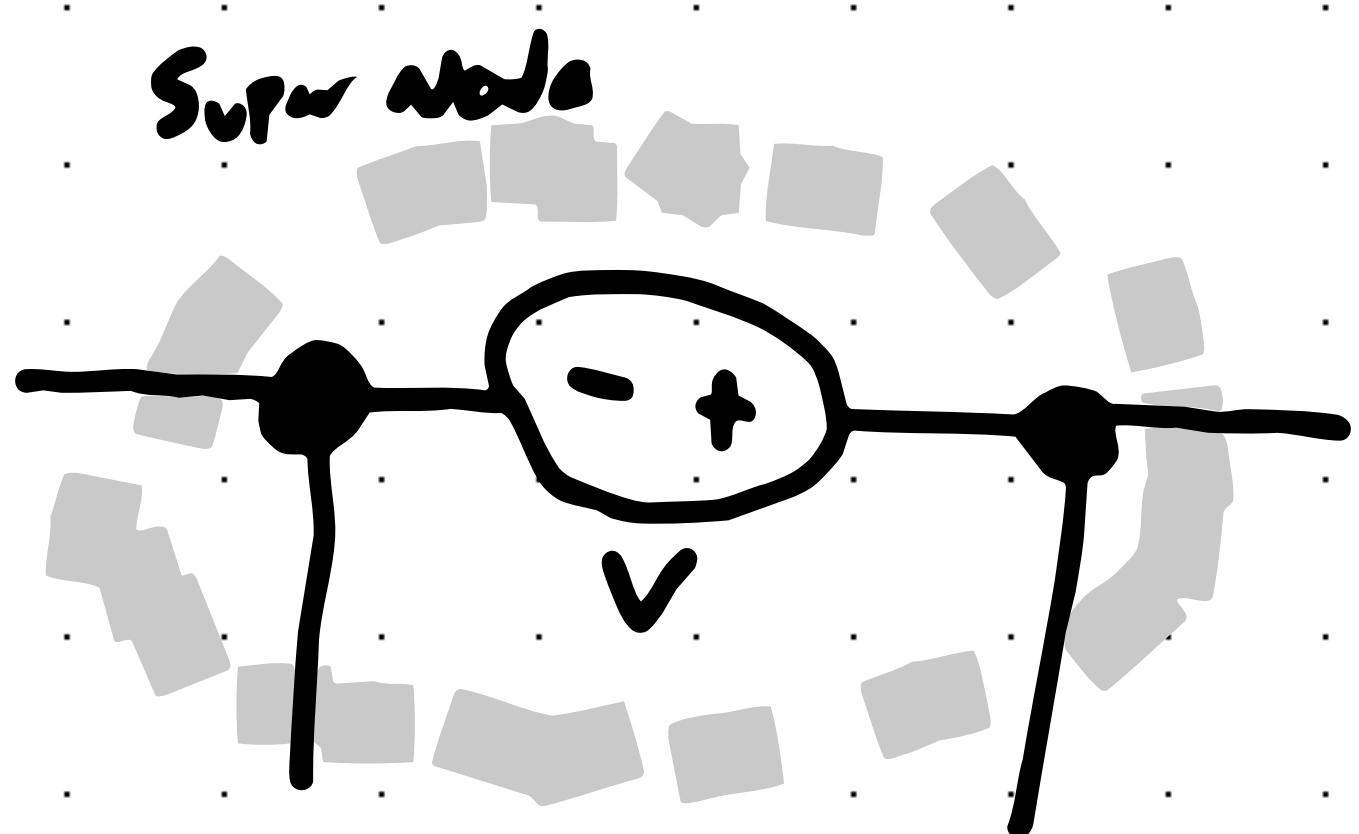
• Aly doesn't
like this method
that much, but
still wants to
discuss it.

Essential Node:



Any node that has three, or more, branches connected together.

Super Node:



Any two nodes in between a Voltage Source

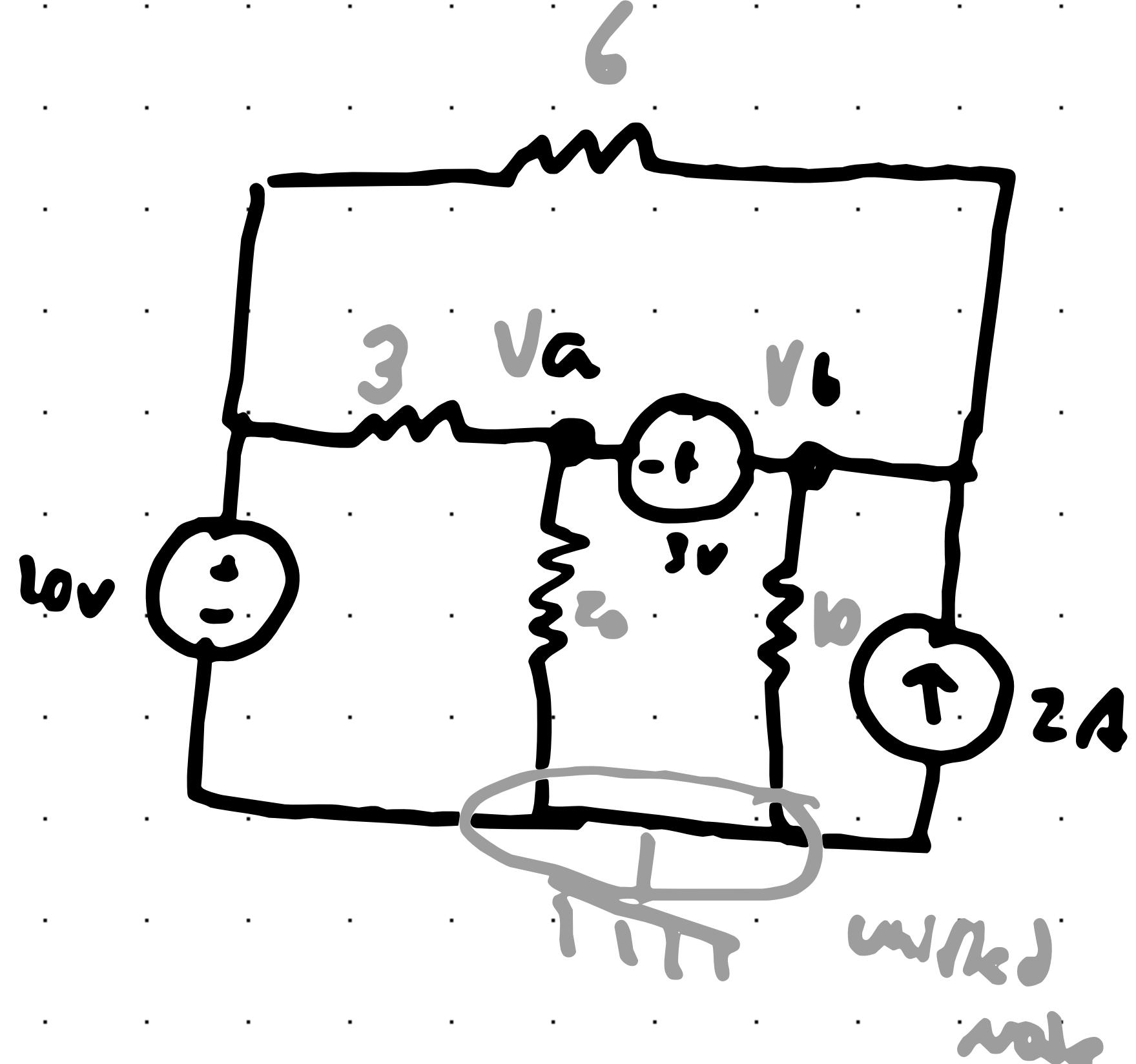
There is a proof to say that

$\sum I = 0$ for the entire Super node.

Example

Use Node Voltage

Method to calculate
the value of V_a



Now Solving these...

$$\frac{V_a - 10}{3} + \frac{V_a}{20} + \frac{V_b}{10} + (-2) + \frac{V_b - 10}{6} = 0 \quad (3)$$

$$V_b - V_a = 3 \quad (4)$$

$$V_a = 10.91V$$

However, there is an easier way to do this....

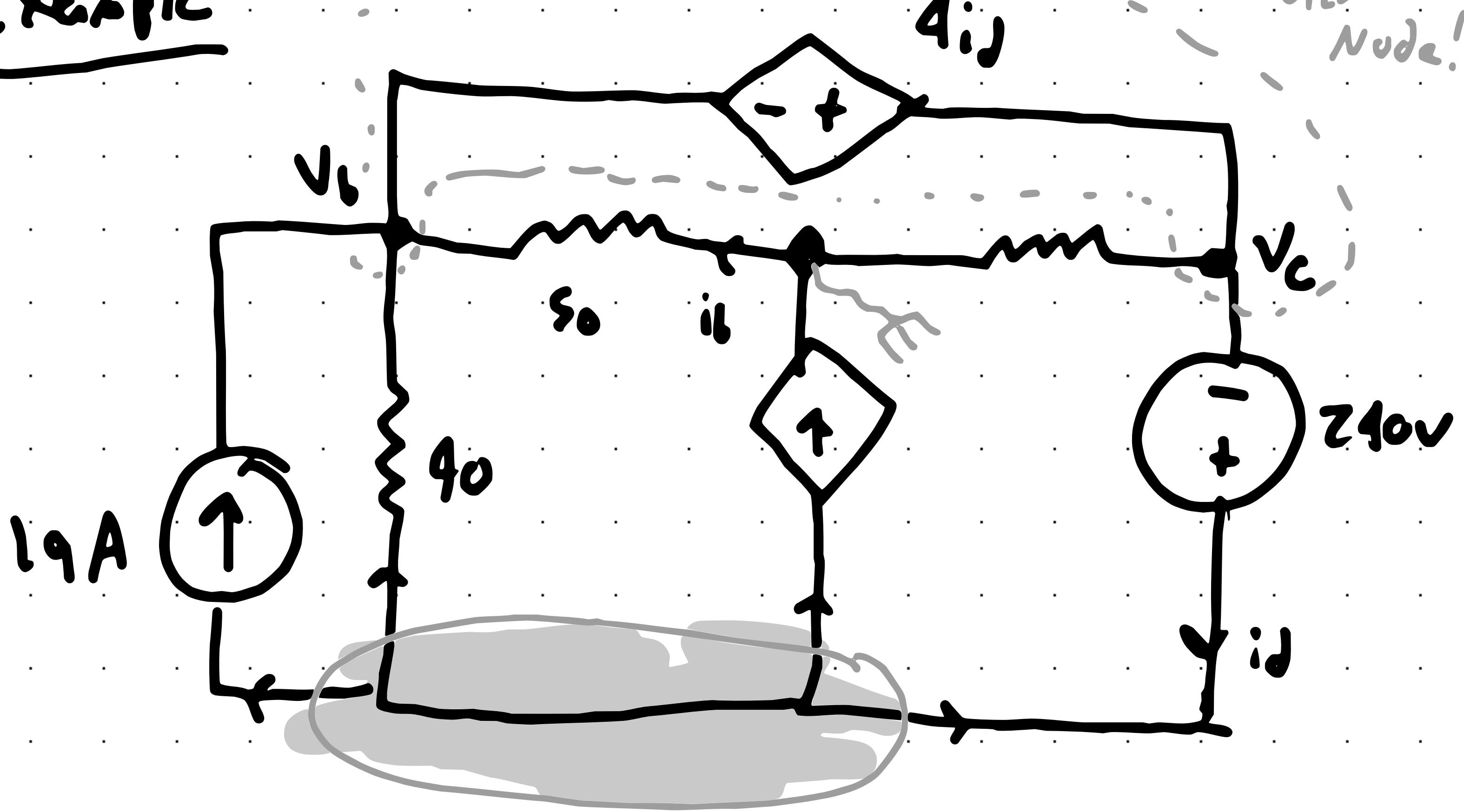
Recognize the Super node in between V_a and V_b

$\sum I = 0$, Super node

$$\frac{V_a - 10}{3} + \frac{V_a}{20} + \frac{V_b}{10} + (-2) + \frac{V_b - 10}{6}$$

Now! This is the sum equality as the one from both initial equations!

Example



Solution

$$\sum I = 0 \quad @ \text{Node } A \quad i_Q + \frac{V_A - V_L}{40} + Z i_B + (-i_D) = 0$$

Superknot

$$\sum I = 0 \quad -i_Q + \frac{V_L - V_A}{40} + \frac{V_L - 0}{5} + i_D + \frac{V_C}{5} = 0$$

$$V_C - V_L = 4i_D$$

$$i_L = \frac{0 - V_L}{5}$$

$$\sum I = \sum_{\text{nodes}} i_D = 2i_B + \frac{V_A - V_L}{40} + i_Q$$