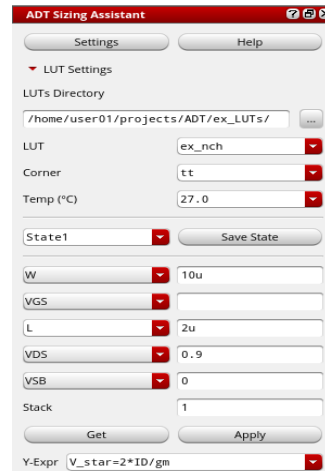


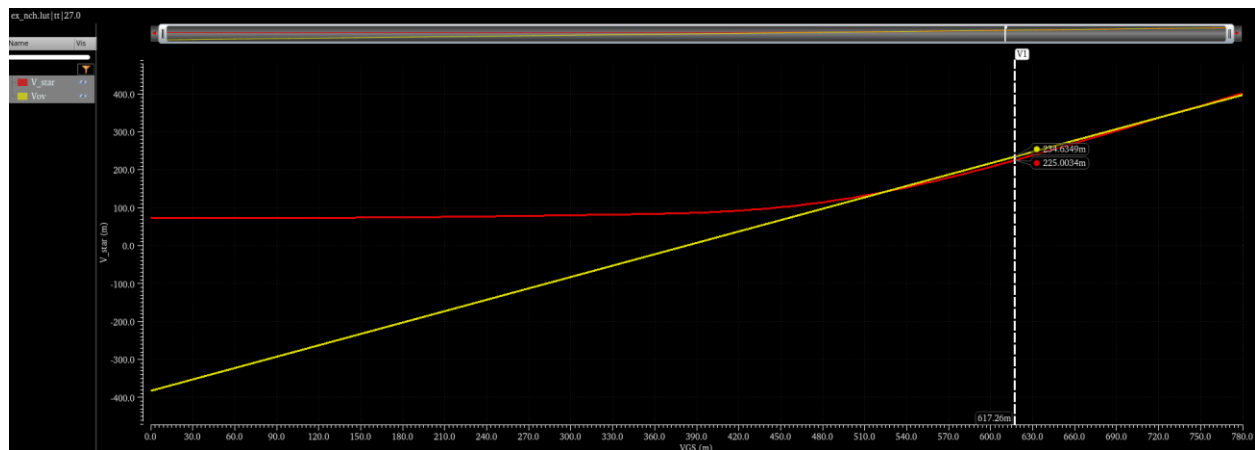
# Lab 2

## Part 1: Sizing Chart

### Sizing Assistant



### V\* & Vov vs VGS

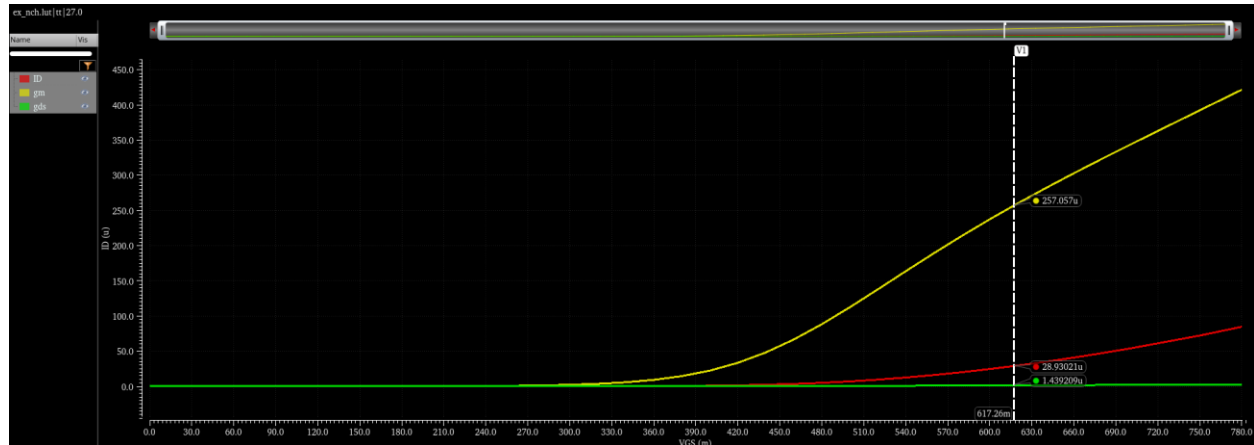


$$\text{Mag}(A_v) = 2V_{RD}/V_{Q^*} \rightarrow 8 = (2(1.8/2))/V_{Q^*} \rightarrow V_{Q^*} = 0.225 \text{ V}$$

$$R_D = V_{RD}/I_D = (1.8/2)/100\mu = 9 \text{ k}\Omega$$

**From Graph:**  $V_{GSQ} = 617.26 \text{ mV}$ ,  $V_{ovQ} = 234.6 \text{ mV}$

## ID, gm & gds vs VGS



**From Graph:**  $ID_X = 28.93 \mu A$ ,  $gm_X = 257.057 \mu S$ ,  $gds_X = 1.439 \mu S$

## Width Sizing

$$W = \frac{(100\mu)(10\mu)}{28.93\mu} = 34.566 \approx 34.6 \mu m$$

$$gm_Q = \frac{(257.057\mu)(34.6\mu)}{10\mu} = 889.4 \mu S$$

$$gds_Q = \frac{(1.439\mu)(34.6\mu)}{10\mu} = 4.979 \mu S$$

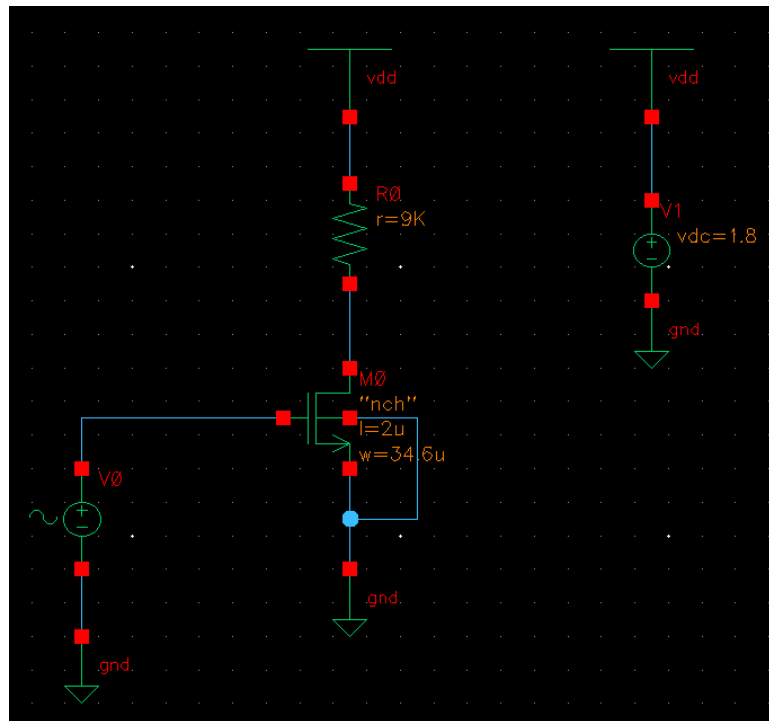
$$r_o = 1/gds_Q = \frac{1}{(4.979\mu)} = 200.8 k\Omega$$

$$\text{Gain} = |A_v| = gm_Q (R_D || r_o) = \frac{889.4\mu}{\frac{1}{9k} + \frac{1}{200.8k}} = 7.66 \approx 8$$

## Part 2: CS Amplifier

### 1) OP & AC Analysis

#### Schematic



#### DC OP (Q-point)

Name	Value
1 M0:vgs	617.3E-3
2 M0:id	100.4E-6
3 M0:gm	893.0E-6
4 M0:gds	4.997E-6
5 M0:vds	896.6E-3
6 M0:region	2.000
7 M0:rout	200.1E3

	ID ( $\mu\text{A}$ )	gm ( $\mu\text{S}$ )	gds ( $\mu\text{S}$ )	VDS (mV)	r <sub>o</sub> (k $\Omega$ )	Region
Part 1	100.0	889.4	4.98	900.0	200.8	Sat.
Part 2	100.4	893.0	4.997	896.6	200.1	Sat.

## RD & r<sub>o</sub>

- We notice that RD (9 kΩ) << r<sub>o</sub> (200 kΩ), and gain = -gm (RD || r<sub>o</sub>). Therefore, we can justify ignoring r<sub>o</sub> since that the smaller resistance is more dominant in parallel connection.
- If min. L is used, r<sub>o</sub> decreases, as  $r_o = \frac{v_A}{I_{DS}}$  & Early voltage is directly proportional with L (V<sub>A</sub> ∝ L). Moreover, smaller L causes short channel effects which lead to lower drain current.

## Intrinsic Gain

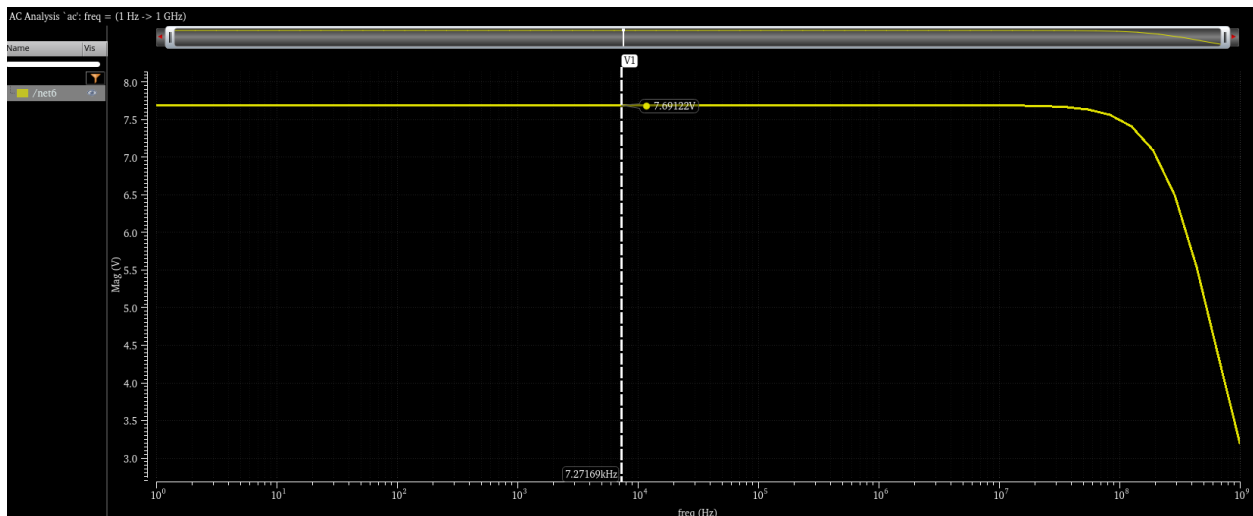
Intrinsic gain = -gm (r<sub>o</sub>) = -(896.6μ)(200.1k) = -179.4 ≈ -179

## Analytical Amplifier Gain

- $A_v = -gm (RD || r_o) = \frac{-896.6\mu}{\frac{1}{9k} + \frac{1}{200.1k}} = -7.72 \approx -8$  (per Part 2)
- $A_v = -7.66$  (per Part 1)
- |Amplifier gain| << |Intrinsic Gain|

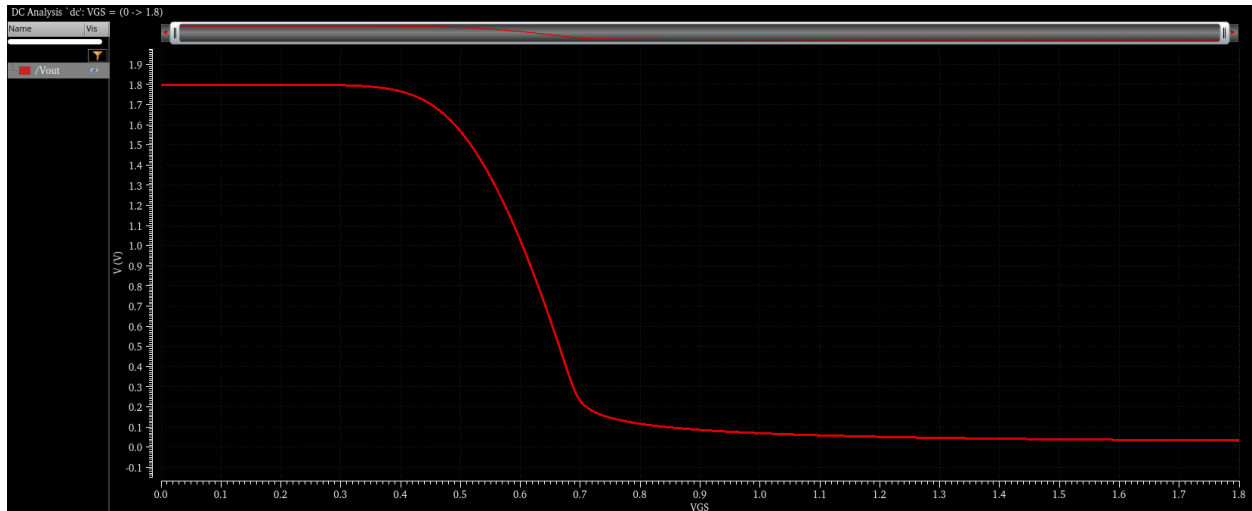
## AC Analysis

**Magnitude = 7.69**



## 2) Gain Non-Linearity

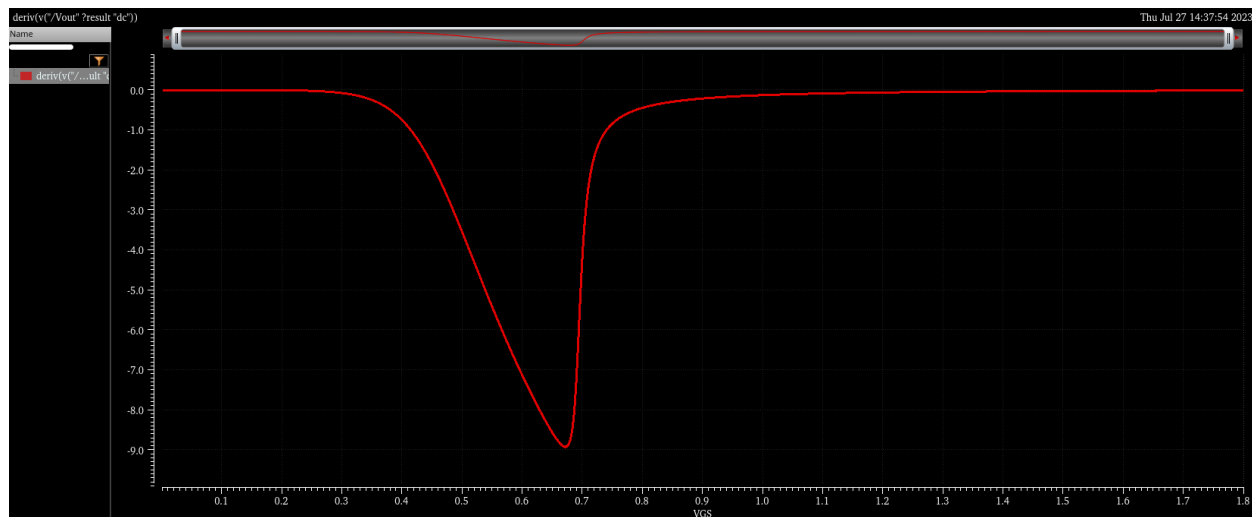
### Vout vs Vin (DC)



#### Comment:

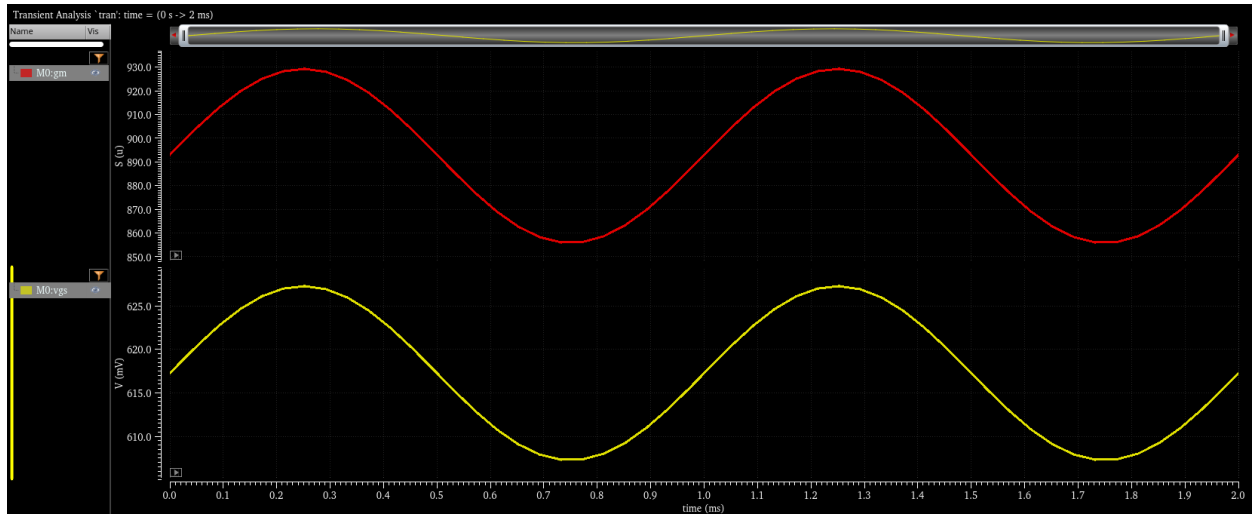
- It is a non-linear relation.
- Gain =  $-g_m (R_D)$  &  $g_m = f(V_{in})$ , which means that any change in input voltage would change  $g_m$ , thus changing the Q-point on the quadratic  $I_D$  vs  $V_{GS}$  curve.

### Small Signal Gain



**Comment:** It is a non-linear relation due to dependence of  $g_m$  on the input voltage, thus changing the Q-point on the quadratic  $I_D$  vs  $V_{GS}$  curve. The absence of source resistance increases the non-linearity.

## gm vs Time

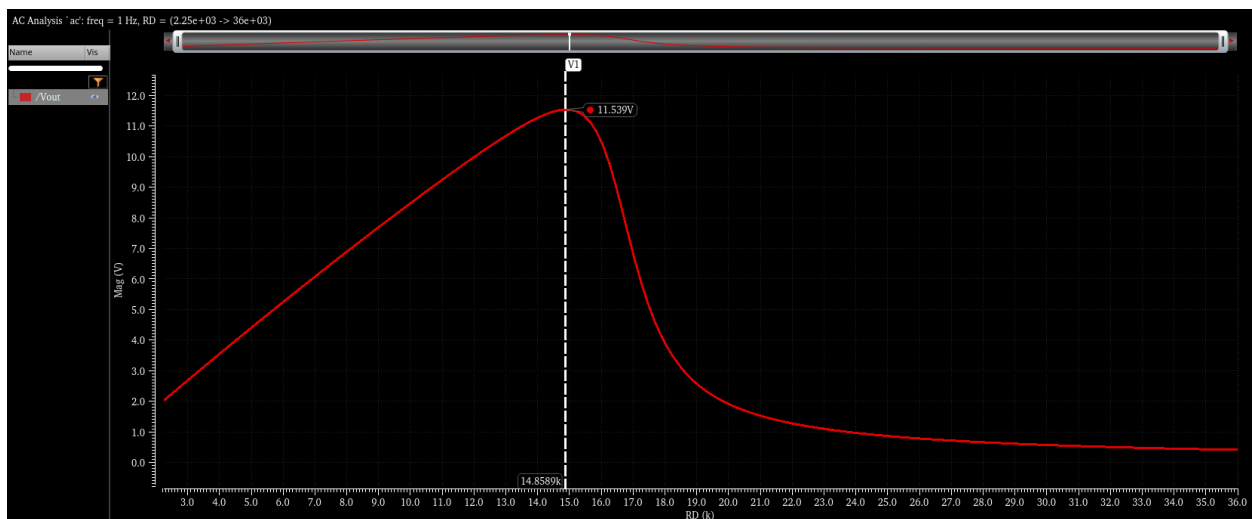


### Comments:

- $g_m$  has the same waveform as  $V_{in}$ , so  $g_m = f(V_{in})$
- The amplifier is non-linear as it is function of  $g_m$  and  $g_m$  varies with  $V_{in}$

## 3) Maximum Gain

### Gain vs RD



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## Behavior Justification

At the beginning, the relation is linear since  $A_v = (2 \cdot V_{RD})/V_{ov}$  per square-law. This relation holds until the voltage drop on  $R_D$  incredibly increases making the transistor go out from saturation region, so this relation is not valid anymore.

## Highest Gain

$$R_D = 14.86 \text{ k}\Omega \text{ and } A_v = 11.539$$

## Analytical Analysis

Maximum gain happens when  $V_{out} = V_{ov} = V_{GS} - V_{th} = 0.617 - 0.38 = 0.24$

$$(V_{DD} - V_{ov})/I_D = \frac{1.8 - 0.24}{100.4 \mu} = 15.54 \text{ k}\Omega$$

$$|A_v| = 889.4 \text{ m} \cdot \frac{200.8 \times 15.54}{200.8 + 15.54} \approx 12.8$$

	<b><math>R_D</math> (k<math>\Omega</math>)</b>	<b><math>A_v</math></b>
<b>Simulation</b>	14.86	15.54
<b>Analytical</b>	11.54	12.8

## Signal Swing at Maximum Gain

Available swing zero since output is set to  $V_{ov}$ . Any swing would lead to driving the transistor out of saturation.

## Supply Voltage Scaling Down

From this equation  $A_v = (2 \cdot V_{RD})/V_{ov}$ , decreasing  $V_{DD}$  would lead to a lower voltage drop on drain resistance leading to a smaller gain.

## 4) Gain Linearization (Feedback)

### Sizing

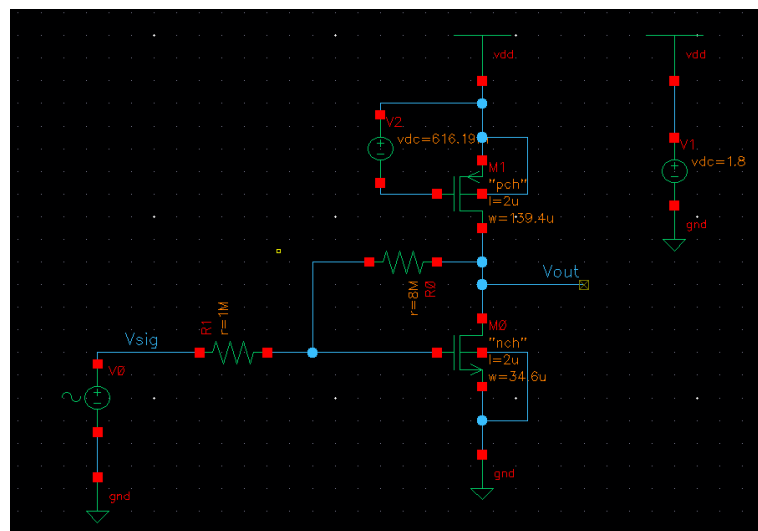
LUT	ex_pch
Corner	1t
Temp (°C)	27.0
State1	Save State
W	10u
VGS	0:10m:0.78
L	2u
VDS	0.9
VSB	0
Stack	1
Get	Apply
V-Expr	Vov=VGS-vth



**From Graph:**  $V_{GSQ} = 616.19 \text{ mV}$ ,  $V_{ovQ} = 222.84 \text{ mV}$ ,  $I_{DQ} = 7.175 \text{ } \mu\text{A}$

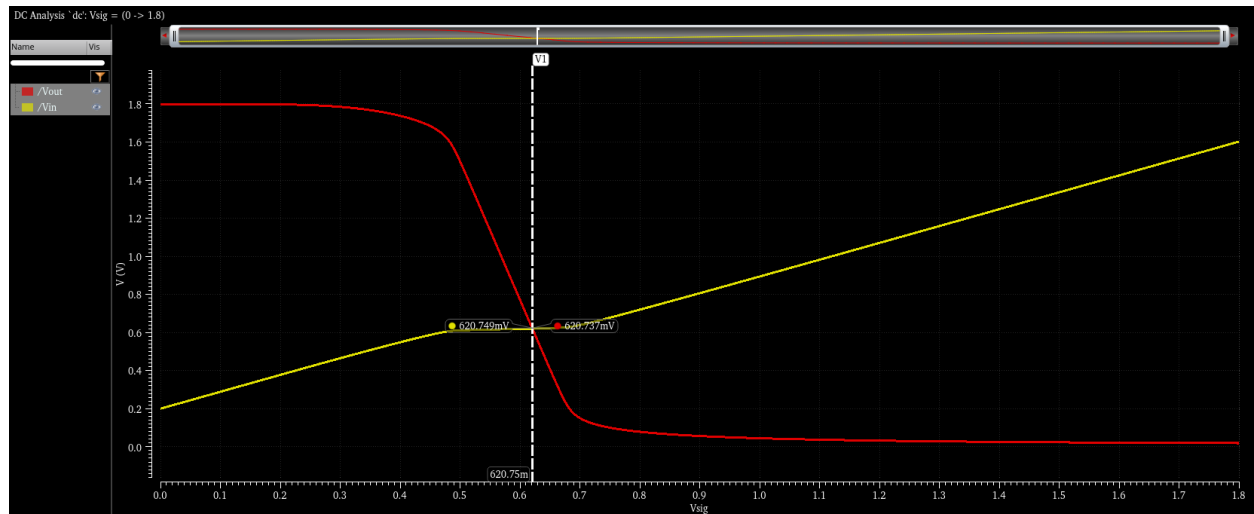
$$W = \frac{(100\mu)(10\mu)}{7.175\mu} = 139.37 \approx 139.4 \text{ } \mu\text{m}$$

### Schematic



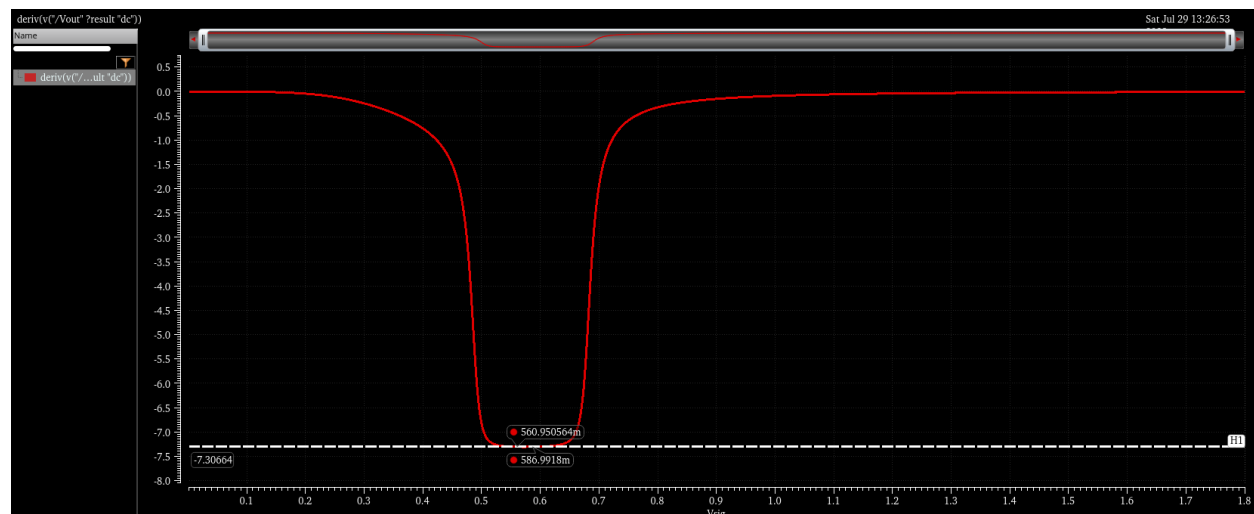


## Vin and Vout vs Vsig



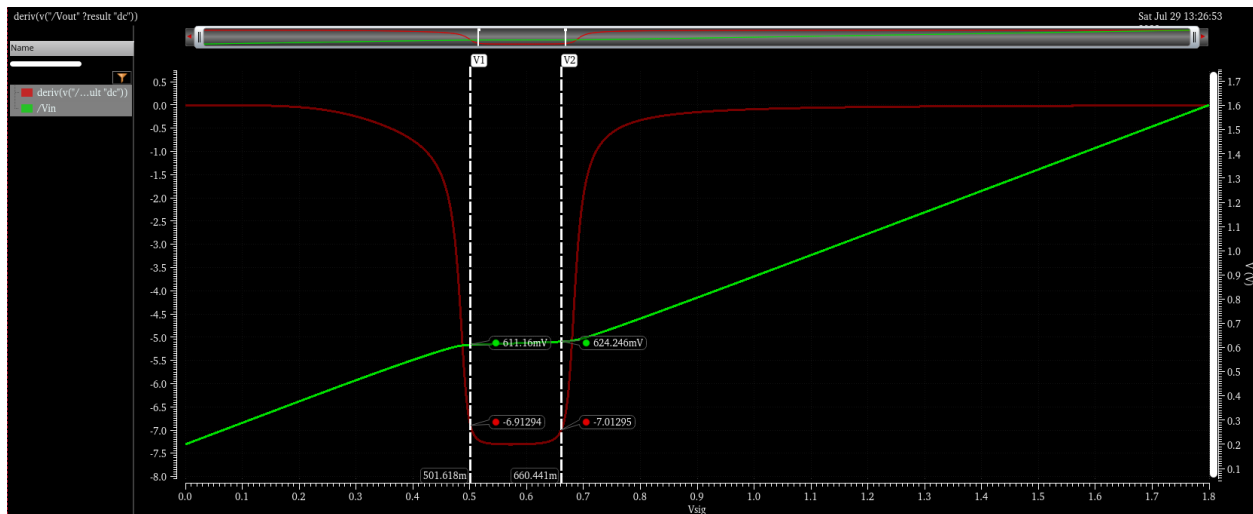
- $V = 620.75 \text{ mV}$  is the voltage where the two curves cross. Note that this voltage is approximately equal to  $V_{GS_{M1}}$ . At this point  $V_{out}$  is also equal to  $V_{in}$  because no current flows in the two resistors.
- $V_{out}$  vs  $V_{sig}$  is non-linear per square law as  $g_m$  is non-linear and function in input voltage.

## Small Signal Gain



- Small signal gain = -7.3
- The gain is approximately **linear** only in the part where the derivative is constant (saturation region). Despite the non-linearity in large signal, we linearize the curve around the operating point making a linear relation in small signal. The gain is non-linear in triode and cutoff regions.

## Simulation Input Range



$V_{in} \approx 610 \text{ mV} - 625 \text{ mV}$

## Analytical Input Range

Input range =  $(1.8 - 2 \cdot 0.225)/8 = 168 \text{ mV}$

From graph:  $V_{sig} \text{ range} = 660 - 500 = 160 \text{ mV}$

	Input Range (mV)
Analytic	168
Simulation	160