

Lab 10

PART 1: LPF AC Noise Analysis

$R = 1k\Omega$ & $C = 1pF$

Output Noise vs Frequency



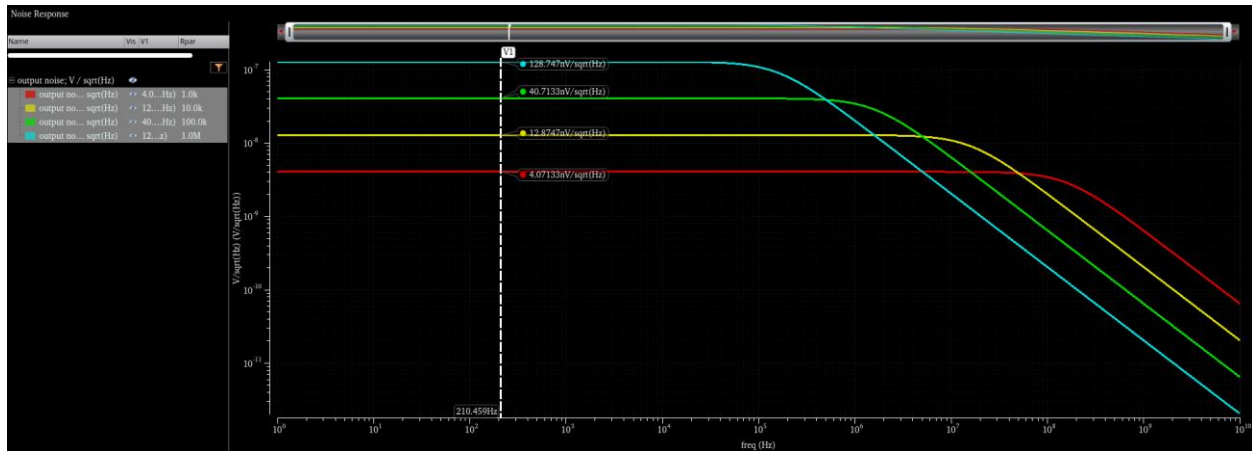
Hand Analysis

- $V_n^2(f) = 4KTR = 4(4.14 * 10^{-21})(1k) = 1.66 * 10^{-17} \rightarrow V_n(f) = 4.069 \frac{nV}{\sqrt{Hz}}$
- $V_{nrms} = \frac{KT}{C} = \frac{4.14 * 10^{-21}}{1p} \rightarrow V_{nrms} = 64.34\mu V$
- $BW = \frac{2}{4\pi RC} = 159.2MHz$

	Simulation	Hand Analysis
Noise Density $\left(\frac{nV}{\sqrt{Hz}}\right)$	4.071	4.069
Noise RMS (μV)	64.32	64.34
Bandwidth (MHz)	158.8	159.2

Parametric Sweep (R = 1k, 10k, 100k, 1000k)

Output Noise vs Frequency (Log. Scale)



Comment: Noise density is directly proportional with resistance (R) and noise bandwidth is inversely proportional with resistance.

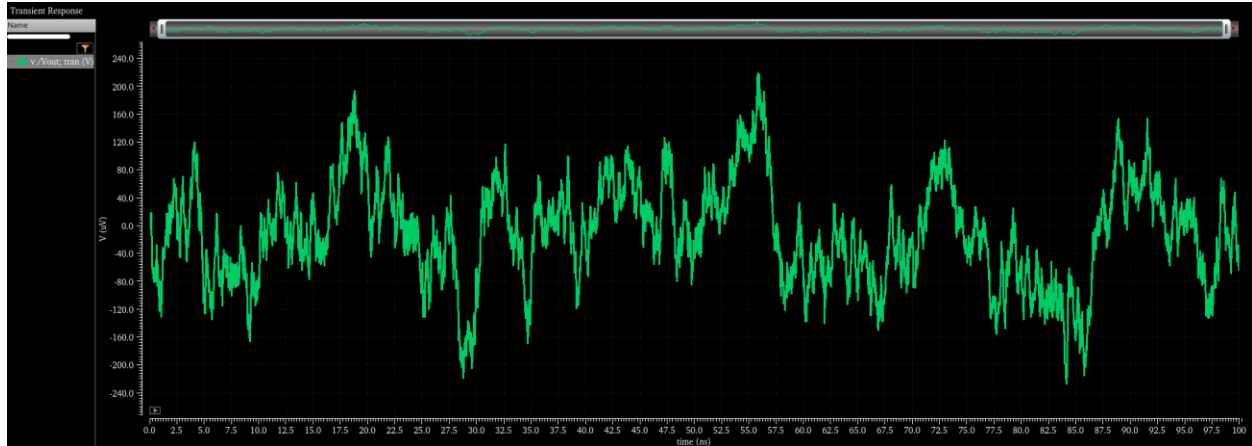
RMS Noise

rmsNoise(1 10G)	
Rpar	rmsNoise(1 10G)
1 1.000E3	64.32E-6
2 10.00E3	64.62E-6
3 100.0E3	64.65E-6
4 1.000E6	64.66E-6

Comment: RMS noise is independent of resistance. Increasing R increases the density but reduces the BW; thus, the total integrated noise (area under the curve) is unchanged.

PART 2: LPF Transient Noise Analysis

Output Waveform ($T_{\text{step}} = \tau/100$)



Expression	Value	Expression	Value	Expression	Value
ymin(vtime("tran "/Vout"))	-226.7E-6	ymax(vtime("tra...	218.0E-6	rms(vtime("tran ...	73.04E-6

	Noise Simulation	Transient Simulation
RMS Noise (μV)	64.32	73.04

$$T_{\text{step}} = \tau/10$$

Expression	Value
rms(vtime("tran "/Vout"))	68.92E-6

Comment: RMS noise decreased when the step increased ($68.92 < 73.04$), because we reduced the frequency window (lower area under the curve).

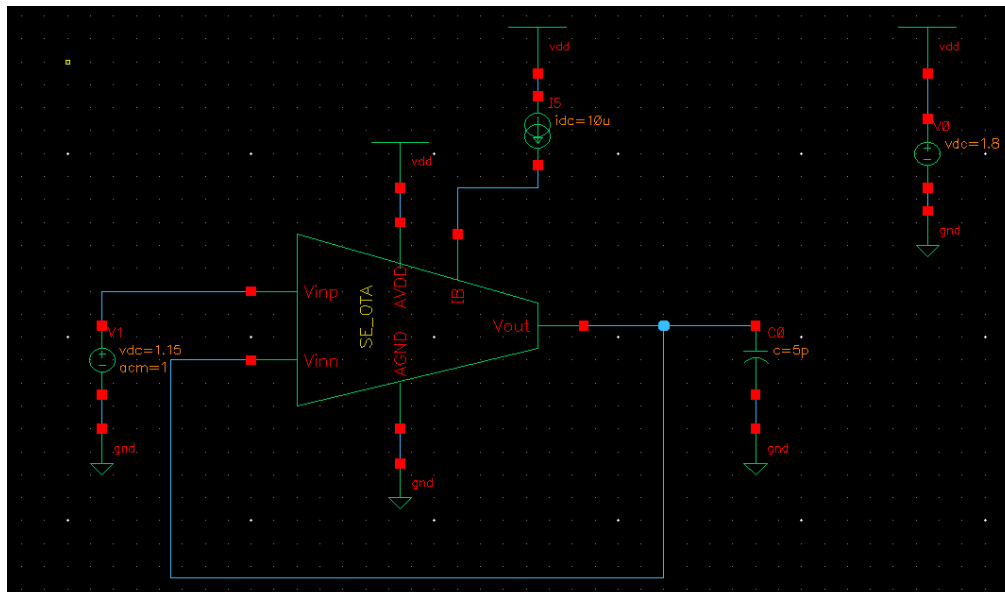
RMS Noise vs Iteration



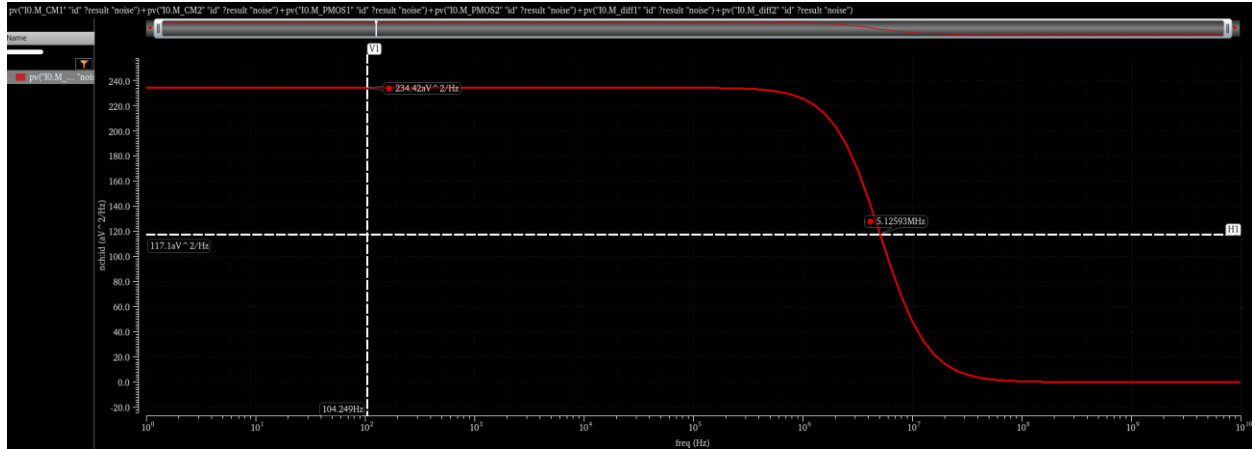
	Noise Simulation	Transient (1iteration)	Transient (avg. 20 iterations)
RMS Noise (μV)	64.32	73.04	63.89

PART 3: 5T OTA AC Noise Analysis

Schematic



Output Thermal Noise vs Frequency



- $V_{out}^2(f) = 234.42a \rightarrow V_{out}(f) = 15.3 \frac{nV}{\sqrt{Hz}}$
- $BW = 5.13MHz$

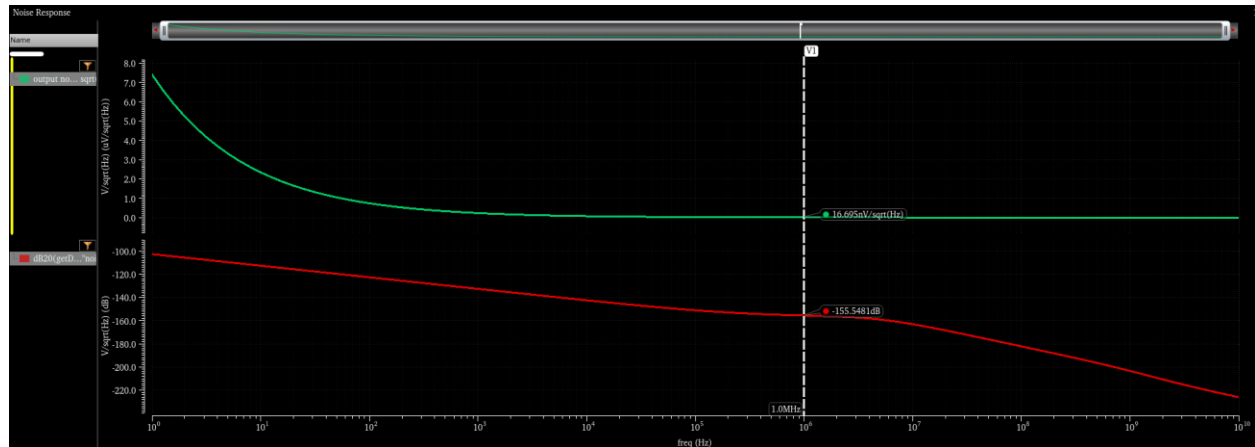
Hand Analysis

I0.M_Pmos1:gm I0.M_diff1:gm I0.M...	
Name	Value
1 I0.M_Pmos1:gm	66.21E-6
2 I0.M_diff1:gm	162.5E-6
3 I0.M_Pmos1:rout	629.6E3
4 I0.M_diff1:rout	623.7E3

- $V_{out}^2(f) = \frac{8KT\gamma}{gm_{diff}} \left(1 + \frac{gm_{load}}{gm_{diff}}\right) * Av^2 = \frac{8(4.14*10^{-21})\left(\frac{2}{3}\right)}{162.5*10^{-6}} \left(1 + \frac{66.2}{162.5}\right) * 1^2 = 191.2aV$
- $V_{out}(f) = 13.8 \frac{nV}{\sqrt{Hz}}$
- $BW_{OL} = \frac{1}{2\pi RC_L} = \frac{1}{2\pi(ro_{diff}||ro_{load})C_L} = \frac{1}{2\pi(313.3k)(5p)} = 101.6kHz$
- $GBW_{OL} = 50 * 101.6k = 5.08MHz$
- $GBW_{OL} = GBW_{CL} = 1 * 5.08M \rightarrow B_N = 5.08MHz$

	Transient Simulation	Hand Analysis
Noise density $\left(\frac{nV}{\sqrt{Hz}}\right)$	15.3	13.8
Bandwidth (MHz)	5.13	5.08

Total Output Noise (Thermal + Flicker) vs Frequency



Flicker noise corner $\approx 1\text{MHz}$

RMS Output Noise

Device	Param	Noise Contribution	% Of Total
/IO/M_diff2	id	6.59705e-10	23.98
/IO/M_diff1	id	6.56537e-10	23.87
/IO/M_PMOS2	fn	3.04181e-10	11.06
/IO/M_PMOS2	id	3.02605e-10	11.00
/IO/M_PMOS1	fn	2.89702e-10	10.53
/IO/M_PMOS1	id	2.70422e-10	9.83
/IO/M_diff2	fn	1.33622e-10	4.86
/IO/M_diff1	fn	1.29858e-10	4.72
/IO/M_CM2	id	2.1769e-12	0.08
/IO/M_CM1	id	1.48858e-12	0.05
/IO/M_PMOS2	rs	9.03722e-14	0.00
/IO/M_PMOS1	rs	8.16347e-14	0.00
/IO/M_CM1	fn	4.55001e-14	0.00
/IO/M_CM2	fn	2.16432e-14	0.00
/IO/M_PMOS2	rd	8.20984e-17	0.00
/IO/M_PMOS1	rd	2.84565e-17	0.00
/IO/M_diff1	rs	0	0.00
/IO/M_diff1	rd	0	0.00
/IO/M_diff2	rs	0	0.00
/IO/M_diff2	rd	0	0.00

Integrated Noise Summary (in V²) Sorted By Noise Contributors
 Total Summarized Noise = 2.75054e-09
 Total Input Referred Noise = 2.1636e-06
 The above noise summary info is for noise data

- Output thermal noise = $V_{rms}^2 = \sum id = 1.89\text{nV}$
- Output RMS thermal noise = $43.47\mu\text{V}$

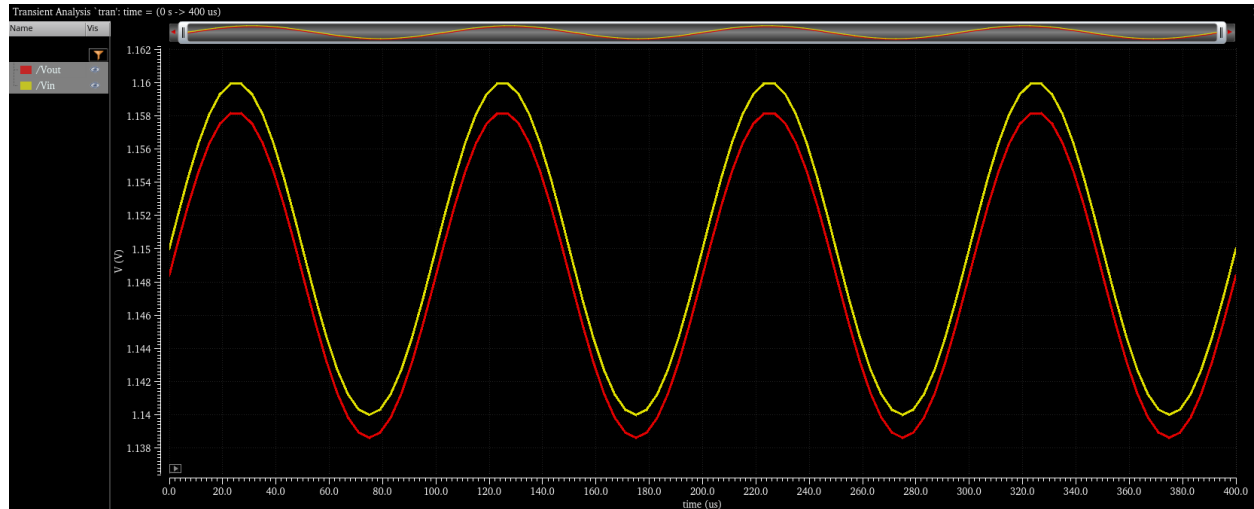
Hand Analysis

- Total noise density \approx thermal noise density (dominant noise) = $13.8 \frac{\text{nV}}{\sqrt{\text{Hz}}}$
- BW = 5.08MHz (noise is multiplied with the same transfer function)
- Output RMS thermal noise = $\sqrt{234.42a * \frac{\pi}{2} * f_p} = 234.42a * \frac{\pi}{2} * 5.13M = 43.46 \mu\text{V}$

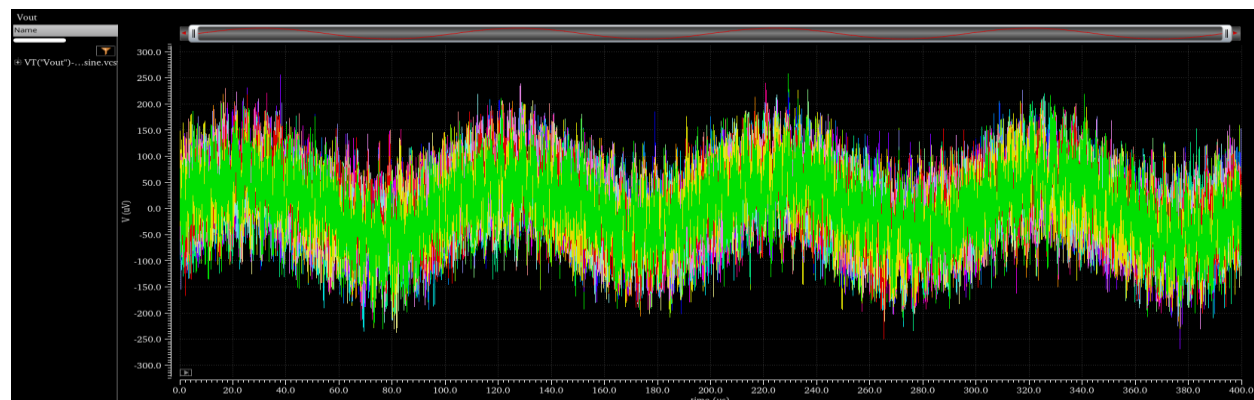
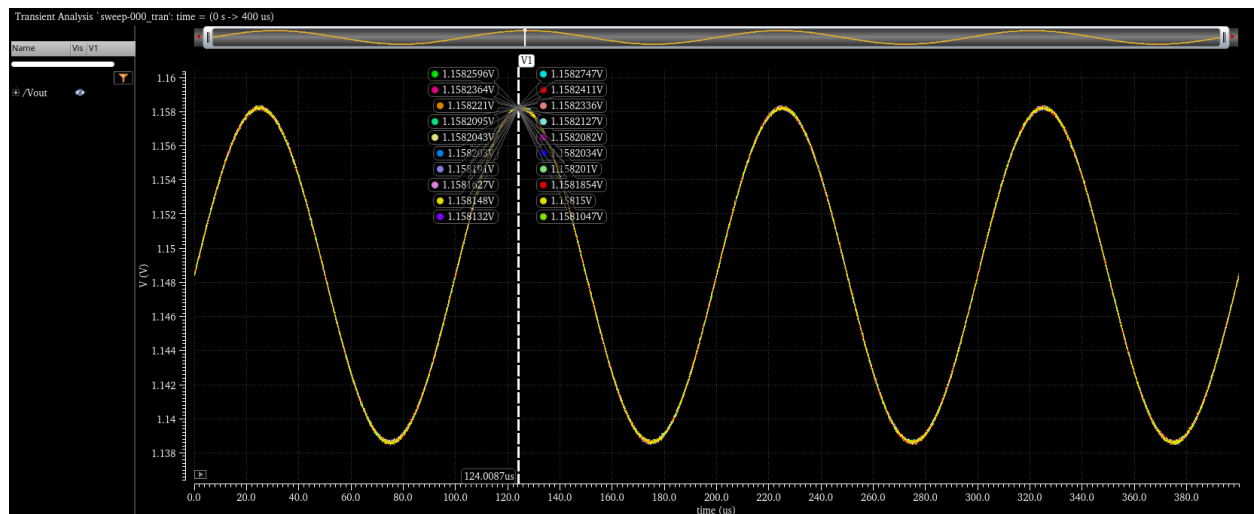
	Simulation	Hand Analysis
RMS Noise (μV)	43.47	43.46

PART 4: 5T OTA Transient Noise Analysis

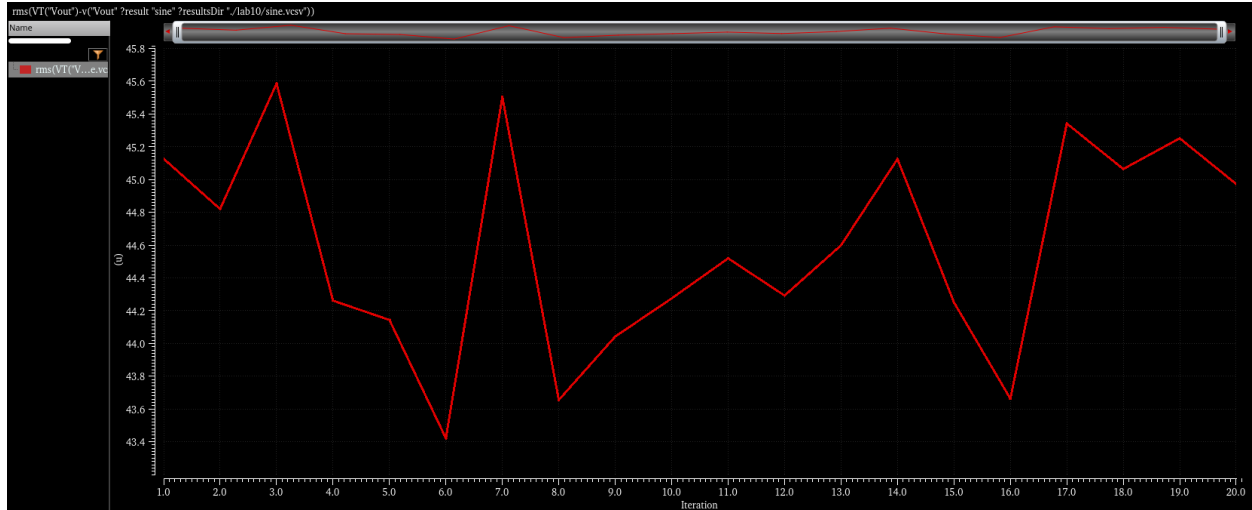
Input & Output vs Time



Noisy Output Waveform



RMS Noise vs Iteration



average(rms(VT("Vout")-v("Vout")?re...	
Expression	Value
1 average(rms(VT(...	44.57E-6

	Part 3 Simulation	Part 4 Simulation
RMS Noise (μV)	43.47	44.57

Comment: Part 4 is the total rms noise, and part 3 is thermal rms noise only.