# Hand Analysis & Functions Explanation

#### Cluster Size

Since  $SIR_{\min dB}$  & number of sectors are given, we can calculate N from the following equation:

$$SIR_{\min(ratio)} = \frac{1}{Sectorization} * (\sqrt{3 N} - 1)^n$$

**Note:** interference variable is determined from sectorization method to follow the stated equation.

```
function N = cluster_size(S, interference, SIR_dB, n)
    SIR = 10^(SIR_dB/10);
    N = ceil((1/3)*((interference*SIR)^(1/n) + 1)^2);
    N = valid_N(N);
end
```

Then we have to check for nearest valid cluster size from the following equation:

$$N = i^2 + ik + k^2$$

```
function N = valid_N(n)
    limit = 100; % limit of i & k
    i = 0:limit;
    valid = [];
    for k = 0:limit
        valid = [valid (i.^2 + k^2 + i.*k)];
    valid = unique(sort(valid));
    while ~(ismember(n,valid))
        n = n + 1;
        if n > 30000
            print ('N is too large');
            break:
        end
    end
    N = n;
end
```

# **Traffic Intensity**

Number of channels per sector can be calculated from total number of channels (S) by:

$$K = \frac{S}{N * Sectors}$$

Instead of using Erlang charts, we can use probability of blocking equation:

$$P_r = \frac{\frac{A^c}{C!}}{\sum_{K=0}^c \frac{A^k}{K!}} = GOS$$

```
function A = inverlangb(c, gos)
   fun = @(A) gos - (A^c/factorial(c)) / sum(A.^((0:c))./factorial(0:c));
   A = fzero(fun, [0, 1000]);
end
```

The previous function returns the traffic intensity per sector, then we can calculate traffic intensity per cell by:

$$A_{cell} = A_{sector} * number of sectors$$

```
function [Acell, Asector] = traffic_intensity(S, N, sectors, GOS)
   K = floor(S / (N * sectors));
   Asector = inverlangb(K, GOS);
   Acell = Asector * sectors;
end
```

**Note:** We have to floor so that no extra bandwidth is taken.

#### **Number of Cells**

Users per cell can be calculated by:

$$A_{cell} = A_u U_{cell}$$

Total Number of users can be calculated by:

$$Total\ Users = User\ denisty * Area\ of\ city$$

Total number of cells can be calculated by:

$$Total \ Number \ of \ Cells = \frac{Total \ Users}{Users/Cell}$$

```
function Cells = no_of_cells(Area, User_Den, Acell, Au)
    Users_Per_cell = Acell / Au; % number of users per cell
    Total_Users = User_Den * Area; % total number of users
    Cells = ceil(Total_Users / Users_Per_cell); % total number of cells
end
```

Note: We have to ceil so that there are no dead zones.

#### Cell radius

From the given city area, we can calculate the radius by:

Area of cell = 
$$\frac{\text{city area}}{\text{number of cells}}$$
  
Area of cell =  $\frac{3}{2}\sqrt{3}$  R<sup>2</sup>  $\rightarrow$  R =  $\sqrt{\frac{\text{Area of cell}}{\frac{3}{2}\sqrt{3}}}$ 

```
function R = radius(Area, Cells)
   Area_Per_cell = Area / Cells;
   R = sqrt(Area_Per_cell / (3 * sqrt(3) / 2));
end
```

#### Hata Function

The Hata model predicts the path loss in different environments. In our case urbanmedium city is assumed.

$$L_U = 69.55 + 26.16 \log_{10} f - 13.82 \log_{10} h_{Tx} - C_H + (44.9 - 6.55 \log 10 h_{Tx}) * \log_{10} d$$

$$C_H = 0.8 + (1.1 \log_{10} f - 0.7) h_{Rx} - 1.56 (\log_{10} f)$$

Where:

- $h_{Rx}$ : mobile station antenna heigh (m).
- $h_{Tx}$ : base station antenna height of (m).
- $C_H$ : Antenna height correction factor.
- *f*: Frequency (MHz).
- *L<sub>II</sub>*: Path loss in urban areas (dB).
- *d*: Distance between base station and mobile station (Km).
- If Mobile Station is at the edge of the cell, the distance is R.

Received power calculated with relation:

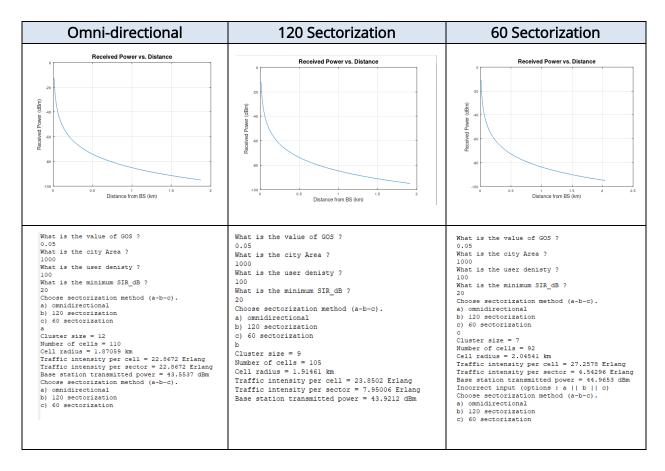
$$P_{Rx} = P_{Tx} - Path loss$$

Reference: 234679133.pdf (core.ac.uk)

```
function L = Hata(f,hm,hb,d)
    CH = 0.8 + (1.1 * log10(f) - 0.7) * hm - 1.5 * log10(f);
    L = 69.55 + 26.16 * log10(f) - 13.82 * log10(hb) ...
    - CH + (44.9 - 6.55 * log10(hb)) * log10(d);
end
```

## **Received Power vs Distance**

- GOS = 0.05 (5%)
- City Area =  $1000 \, km^2$
- User Density =  $100 user/km^2$
- SIRmin dB= 20 dB



#### Comments:

• Received power decreases as distance increases, which is predicted by this formula:

$$P_{Rx} = P_{Tx}G_{Tx}G_{Rx} \left(\frac{H_{Tx} * H_{Rx}}{d^2}\right)^2$$

• Sectorization type does not affect the above graph since transmitted power is kept constant.

## **Complete Code**

```
function A = inverlangb(c, gos)
  fun = @(A) gos - (A^c/factorial(c)) / sum(A.^((0:c))./factorial(0:c));
  A = fzero(fun, [0, 1000]);
end
function L = Hata(f,hm,hb,d)
  CH = 0.8 + (1.1 * log10(f) - 0.7) * hm - 1.5 * log10(f);
  L = 69.55 + 26.16 * log10(f) - 13.82 * log10(hb) ...
   - CH + (44.9 - 6.55 * log10(hb)) * log10(d);
end
function N = valid_N(n)
  limit = 100; % limit of i & k
  i = 0:limit;
  valid = [];
  for k = 0:limit
     valid = [valid (i.^2 + k^2 + i.*k)];
  valid = unique(sort(valid));
  while ~(ismember(n,valid))
     n = n + 1:
     if n > 30000
       print ('N is too large');
       break;
     end
  end
  N = n;
end
```

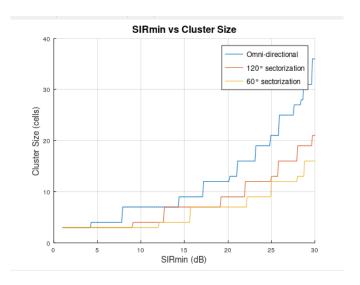
```
function N = cluster_size(S, interference, SIR_dB, n)
  SIR = 10^{(SIR dB/10)};
  N = ceil((1/3)*((interference*SIR)^(1/n) + 1)^2);
  N = valid N(N);
end
function [Acell, Asector] = traffic intensity(S, N, sectors, GOS)
  K = floor(S / (N * sectors));
  Asector = inverlangb(K, GOS);
  Acell = Asector * sectors;
end
function Cells = no of cells(Area, User Den, Acell, Au)
  Users_Per_cell = Acell / Au; % number of users per cell
  Total Users = User Den * Area; % total number of users
   Cells = ceil(Total Users / Users Per cell); % total number of cells
end
function R = radius(Area, Cells)
  Area Per cell = Area / Cells;
   R = sqrt(Area_Per_cell / (3 * sqrt(3) / 2));
end
close all;
clear:
clc;
pkg load communications;
S = 340; % Total number of channels : S= N*K
freq = 900; % Frequency in MHz
sensitivity = -95; % in db
Au = 0.025; % in erlangs
n = 4; % path loss exponent
h BS = 20; % Base Station height
h MS = 1.5; % Mobile Station height
```

```
prompt = "What is the value of GOS ? \n";
GOS = input(prompt);
prompt= "What is the city Area ? \n";
Area = input(prompt);
prompt = "What is the user denisty ? \n";
User Den = input(prompt);
prompt = "What is the minimum SIR dB ? \n";
SIR dB = input(prompt);
prompt = "Choose sectorization method (a-b-c).\na) omnidirectional\nb) 120
sectorization\nc) 60 sectorization \n";
sectorization = input(prompt, 's');
sf = 0; % flag for sectorization method check
while ~sf
   switch sectorization
       case 'a'
           sectors = 1;
           interference = 6;
           sf = 1;
       case 'b'
           sectors = 3;
           interference = 2;
           sf = 1;
       case 'c'
           sectors = 6;
           interference = 1;
           sf = 1;
       otherwise
           fprintf ('Incorrect input (options : a || b || c) \n');
           sectorization = input(prompt, 's');
   end
end
N = cluster size(S, interference, SIR dB, n); % cluster size
[Acell, Asector] = traffic_intensity(S, N, sectors, GOS); % traffic intensity per
cell
Cells = no_of_cells(Area, User_Den, Acell, Au); % number of cells
Cell Radius = radius(Area, Cells); % cell radius
```

```
path_loss = Hata(freq, h_MS, h_BS, Cell_Radius);
P_tx = path_loss + sensitivity;
fprintf ('Cluster size = %d \n', N);
fprintf ('Number of cells = %d \n', Cells);
fprintf ('Cell radius = %d km\n', Cell Radius);
fprintf ('Traffic intensity per cell = %d Erlang\n', Acell);
fprintf ('Traffic intensity per sector = %d Erlang\n', Asector);
fprintf ('Base station transmitted power = %d dBm\n', P_tx);
D = 0:0.01:Cell Radius;
L = Hata(freq, h_MS, h_BS, D);
Prx = P_tx - L;
figure(1);
plot(D, Prx);
xlabel('Distance from BS (km)', 'FontSize', 14);
ylabel('Received Power (dBm)', 'FontSize', 14);
title('Received Power vs. Distance', 'FontSize', 16);
grid on
```

# Part B

# SIRmin Sweep



#### Comments

We can notice that the graph is stair-shaped because N has discrete values given by this equation:

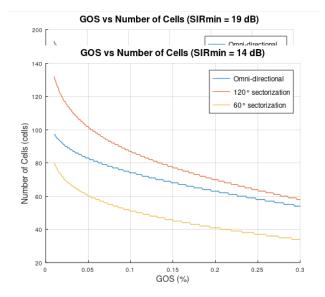
$$N = i^2 + ik + k^2$$

Cluster size increases as the SIRmin increases as 
$$N \propto SIR_{min}$$
. 
$$SIR_{\min(ratio)} = \frac{1}{Sectorization} * \left(\sqrt{3} \ N - 1\right)^n$$

For the same SIRmin, we can see that  $N_{\text{omni-directional}} > N_{120} > N_{60}$ , because propagation in more directions causes higher cochannel interference.

Number of cells vs GOS (User Density = 1400 users/km<sup>2</sup>)

#### SIRmin = 19dB



#### SIRmin = 14dB

#### Comments

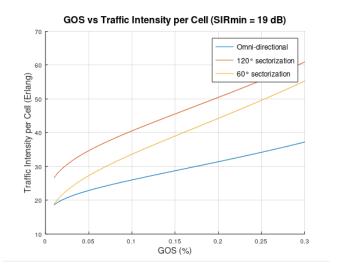
- With higher grade of service (GOS), the number of cells reduces roughly exponentially.
- For any sectorization type:
  - $\blacktriangleright$  We have constant  $SIR_{min} \rightarrow$  constant cluster size (N)
  - $\triangleright$  As GOS increase for constant number of channels, Traffic intensity per cell ( $A_{cell}$ ) increase (from Erlang graph)
  - As traffic intensity increase, User per cell increases (  $User\ per\ cell = \frac{A_{cell}}{A_u\ (given\ constant)}$ )
  - > As user per cell increase, number of cells decrease:

ease, number of cells decrease:
$$cells = ceil \left( \frac{Total \ number \ of \ users}{user \ per \ cell} \right)$$

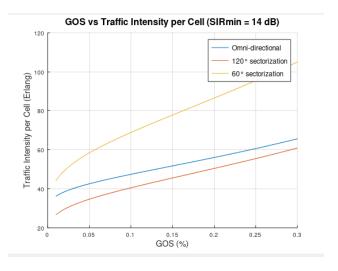
• The number of cells is higher in the graphs at SNR = 19 dB than in the graphs at SNR = 14 dB.

# Traffic Intensity/Cell vs GOS (User Density = 1400 users/km²)

SIRmin = 19dB



### SIRmin = 14dB

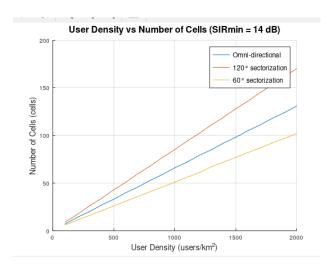


#### Comments

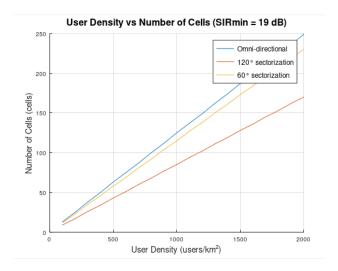
- Traffic intensity increases as GOS increases, as we can assign more users in one cell.
- The traffic intensity per cell is higher in the graphs at SIR = 14 dB than in the graphs at SIR = 19 dB, because the number of Trunked channels (k) for SIR = 14 dB is larger than (k) for SIR = 19 dB, and traffic intensity per cell ∝ number of Trunked channels (k).

# Number of cells versus user density (GOS = 2%)

SIRmin = 14dB



SIRmin = 19dB



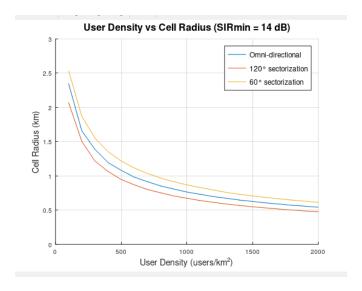
### Comments

• With higher user density, the number of cells increases linearly as: 
$$Number\ of\ Cells\ = \left[\frac{Total\ traffic\ intensity}{Traffic\ intensity\ per\ cell}\right] = \left[\frac{User\ Density\ *\ City\ Area\ *\ Au}{Traffic\ intensity\ per\ cell}\right]$$

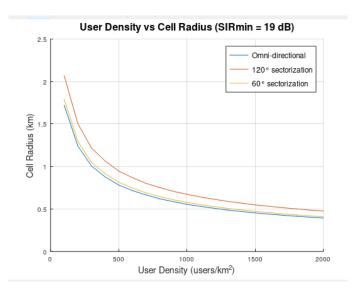
The number of cells increases with higher SIR (Number of cells is greater with SIR = 19 dB).

# Cell Radius vs User Fensity (GOS = 2%)

## SIRmin = 14dB



### SIRmin = 19dB



### Comments

• Cell radius decreases with increasing user density as 
$$Cell\ Area = \frac{Total\ Area}{Number\ of\ Cells}$$
 
$$Cell\ Radius\ (R) = \sqrt{\frac{Cell\ Area}{\frac{3\sqrt{3}}{2}}}$$

- The cell radius therefore has an inverse relationship with the number of cells.
- The cell radius increases with SIR (Cell radius is larger with SIR = 19 dB).

## **Complete Code**

```
function A = inverlangb(c, gos)
  fun = @(A) gos - (A^c/factorial(c)) / sum(A.^((0:c))./factorial(0:c));
  A = fzero(fun, [0, 1000]);
end
function L = Hata(f,hm,hb,d)
  CH = 0.8 + (1.1 * log10(f) - 0.7) * hm - 1.5 * log10(f);
  L = 69.55 + 26.16 * log10(f) - 13.82 * log10(hb) ...
   - CH + (44.9 - 6.55 * log10(hb)) * log10(d);
end
function N = valid N(n)
  limit = 100; % limit of i & k
  i = 0:limit;
  valid = [];
  for k = 0:limit
     valid = [valid (i.^2 + k^2 + i.*k)];
  end
  valid = unique(sort(valid));
  while ~(ismember(n,valid))
     n = n + 1;
     if n > 30000
        print ('N is too large');
       break;
     end
  end
  N = n;
end
function N = cluster size(S, interference, SIR dB, n)
```

```
SIR = 10^(SIR dB/10);
  N = ceil((1/3)*((interference*SIR)^(1/n) + 1)^2);
  N = valid N(N);
end
function [Acell, Asector] = traffic_intensity(S, N, sectors, GOS)
  K = floor(S / (N * sectors)); % number of channels per cell
  Asector = inverlangb(K, GOS);
  Acell = Asector * sectors;
end
function Cells = no of cells(Area, User Den, Acell, Au)
  Users Per cell = Acell / Au; % number of users per cell
  Total Users = User Den * Area; % total number of users
  Cells = ceil(Total Users / Users Per cell); % total number of cells
end
function R = radius(Area, Cells)
  Area Per cell = Area / Cells;
   R = sqrt(Area Per cell / (3 * sqrt(3) / 2));
end
close all;
clear;
clc;
pkg load communications;
S = 340; % Total number of channels : S= N*K
freq = 900; % Frequency in MHz
sensitivity = -95; % in db
Au = 0.025; % in erlangs
n = 4; % path loss exponent
h BS = 20; % Base Station height
h_MS = 1.5; % Mobile Station height
Area = 100;
```

```
s sweep = [1, 3, 6]; % sectorization sweep
i_sweep = [6, 2, 1];  % interference sweep
%%% 1) SIR Sweep
sir sweep = 1:0.1:30;
N_sweep = [];
figure(2);
for j=1:3
    for i=1:length(sir sweep)
        N sweep(i) = cluster size(S, i sweep(j), sir sweep(i), n);
    end
   hold on:
    plot(sir_sweep, N_sweep);
   xlabel('SIRmin (dB)', 'FontSize', 14);
   ylabel('Cluster Size (cells)', 'FontSize', 14);
   if j == 3
        legend('Omni-directional', '120° sectorization', '60° sectorization',
 FontSize', 12);
    end
    title('SIRmin vs Cluster Size', 'FontSize', 16);
    grid on;
end
%%% 2) SIRmin = 19dB & user density = 1400 users/km2
% Plot the number of cells & traffic intensity per cell versus GOS (1% to 30%).
gos_sweep = 1:0.1:30;
gos_sweep = gos_sweep / 100;
cells sweep = [];
Acell sweep = [];
Asector sweep = [];
User_Den = 1400;
for j=1:3
    N = cluster_size(S, i_sweep(j), 19, n);
    for i=1:length(gos sweep)
        [Acell_sweep(i), Asector_sweep(i)] = traffic_intensity(S, N, s_sweep(j),
gos sweep(i));
        cells_sweep(i) = no_of_cells(Area, User_Den, Acell_sweep(i), Au);
    end
```

```
figure(3);
    hold on;
    plot(gos_sweep, cells_sweep);
    xlabel('GOS (%)', 'FontSize', 14);
    ylabel('Number of Cells (cells)', 'FontSize', 14);
    if j == 3
        legend('Omni-directional', '120° sectorization', '60° sectorization',
 FontSize', 12);
    end
   title('GOS vs Number of Cells (SIRmin = 19 dB)', 'FontSize', 16);
    grid on;
    figure(4);
   hold on;
   plot(gos_sweep, Acell_sweep);
   xlabel('GOS (%)', 'FontSize', 14);
   ylabel('Traffic Intensity per Cell (Erlang)', 'FontSize', 14);
   if j == 3
        legend('Omni-directional', '120° sectorization', '60° sectorization',
 FontSize', 12);
    end
    title('GOS vs Traffic Intensity per Cell (SIRmin = 19 dB)', 'FontSize', 16);
    grid on;
end
% 3) At SIRmin = 14dB & user density= 1400 users/km2
gos_sweep = 1:0.1:30;
gos_sweep = gos_sweep / 100;
cells sweep = [];
Acell sweep = [];
Asector_sweep = [];
User_Den = 1400;
for j=1:3
   N = cluster_size(S, i_sweep(j), 14, n);
    for i=1:length(gos sweep)
        [Acell_sweep(i), Asector_sweep(i)] = traffic_intensity(S, N, s_sweep(j),
gos_sweep(i));
        cells sweep(i) = no of cells(Area, User Den, Acell sweep(i), Au);
    end
    figure(5);
```

```
hold on:
    plot(gos sweep, cells sweep);
    if j == 3
        legend('Omni-directional', '120° sectorization', '60° sectorization',
 FontSize', 12);
    end
    xlabel('GOS (%)', 'FontSize', 14);
    ylabel('Number of Cells (cells)', 'FontSize', 14);
    title('GOS vs Number of Cells (SIRmin = 14 dB)', 'FontSize', 16);
    grid on;
   figure(6);
   hold on;
    plot(gos sweep, Acell sweep);
        legend('Omni-directional', '120° sectorization', '60° sectorization',
 FontSize', 12);
    end
   xlabel('GOS (%)', 'FontSize', 14);
    ylabel('Traffic Intensity per Cell (Erlang)', 'FontSize', 14);
    title('GOS vs Traffic Intensity per Cell (SIRmin = 14 dB)', 'FontSize', 16);
    grid on;
end
% 4) At SIRmin = 14dB & GOS= 2%
User Den sweep = 100:100:2000;
GOS = 2/100;
cells sweep = [];
Acell sweep = [];
Asector sweep = [];
radius_sweep = [];
for i=1:3
    N = cluster_size(S, i_sweep(j), 14, n);
    for i=1:length(User_Den_sweep)
        [Acell_sweep(i), Asector_sweep(i)] = traffic_intensity(S, N, s_sweep(j),
GOS);
        cells sweep(i) = no of cells(Area, User Den sweep(i), Acell sweep(i),
Au);
        radius sweep(i) = radius(Area, cells sweep(i));
    end
    figure(7);
```

```
hold on:
    plot(User Den sweep, cells sweep);
    if j == 3
        legend('Omni-directional', '120° sectorization', '60° sectorization',
 FontSize', 12);
    end
    xlabel('User Density (users/km^2)', 'FontSize', 14);
    ylabel('Number of Cells (cells)', 'FontSize', 14);
    title('User Density vs Number of Cells (SIRmin = 14 dB)', 'FontSize', 16);
    grid on;
   figure(8);
   hold on;
    plot(User Den sweep, radius sweep);
        legend('Omni-directional', '120° sectorization', '60° sectorization',
 FontSize', 12);
    end
   xlabel('User Density (users/km^2)', 'FontSize', 14);
    ylabel('Cell Radius (km)', 'FontSize', 14);
    title('User Density vs Cell Radius (SIRmin = 14 dB)', 'FontSize', 16);
    grid on;
end
% 5) At SIRmin = 19dB & GOS= 2%
User Den sweep = 100:100:2000;
GOS = 2/100;
cells sweep = [];
Acell sweep = [];
Asector sweep = [];
radius_sweep = [];
for i=1:3
    N = cluster_size(S, i_sweep(j), 19, n);
    for i=1:length(User Den sweep)
        [Acell_sweep(i), Asector_sweep(i)] = traffic_intensity(S, N, s_sweep(j),
GOS);
        cells sweep(i) = no of cells(Area, User Den sweep(i), Acell sweep(i),
Au);
        radius sweep(i) = radius(Area, cells sweep(i));
    end
    figure(9);
```

```
hold on;
    plot(User Den sweep, cells sweep);
    if j == 3
        legend('Omni-directional', '120° sectorization', '60° sectorization',
 FontSize', 12);
    end
   xlabel('User Density (users/km^2)', 'FontSize', 14);
   ylabel('Number of Cells (cells)', 'FontSize', 14);
   title('User Density vs Number of Cells (SIRmin = 19 dB)', 'FontSize', 16);
   grid on;
   figure(10);
   hold on;
    plot(User_Den_sweep, radius_sweep);
        legend('Omni-directional', '120° sectorization', '60° sectorization',
 FontSize', 12);
    end
   xlabel('User Density (users/km^2)', 'FontSize', 14);
   ylabel('Cell Radius (km)', 'FontSize', 14);
   title('User Density vs Cell Radius (SIRmin = 19 dB)', 'FontSize', 16);
    grid on;
end
```