Machine Learning 01

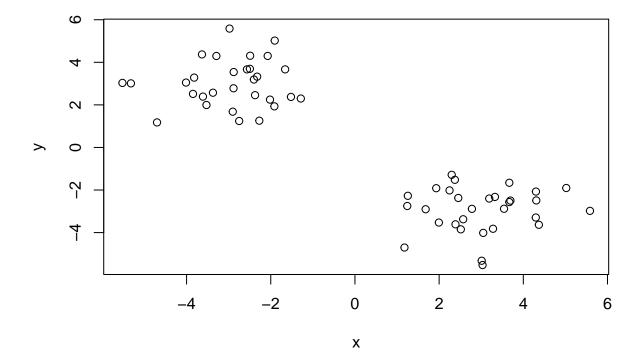
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${\bf Clustering\ methods}$

Kmeans clustering in R is done with the kmeans() function. First we'll make up some data to test and learn with.

```
tmp <- c(rnorm(30,3), rnorm(30,-3))
data <- cbind(x=tmp,y=rev(tmp))
plot(data)</pre>
```



When using Kmeans, we'll need to specify how many clusters (centers) we want. Run kmeans(), setting k = 2 and nstart = 20.

```
km <- kmeans(data, centers=2, nstart=20)</pre>
## K-means clustering with 2 clusters of sizes 30, 30
##
## Cluster means:
##
          Х
## 1 3.008369 -2.945347
## 2 -2.945347 3.008369
##
## Clustering vector:
  ##
## Within cluster sum of squares by cluster:
## [1] 67.48404 67.48404
  (between_SS / total_SS = 88.7 %)
##
## Available components:
## [1] "cluster"
                 "centers"
                             "totss"
                                                     "tot.withinss"
                                         "withinss"
## [6] "betweenss"
                 "size"
                             "iter"
                                         "ifault"
```

Q. How many points are in each cluster?

km\$size

[1] 30 30

There are 30 points in each cluster.

Q. What 'component' of your result object details cluster assignment/membership?

km\$cluster

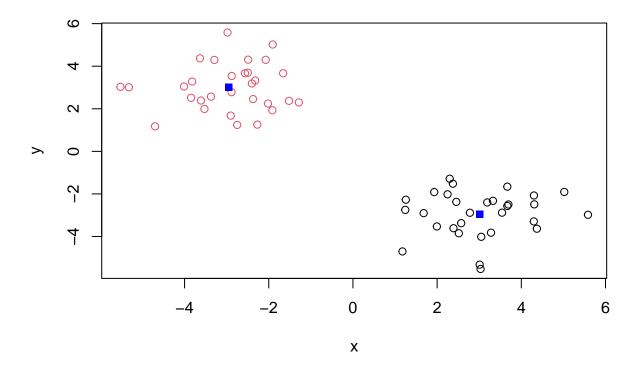
Q. What 'component' of your result object details cluster center?

km\$centers

```
## x y
## 1 3.008369 -2.945347
## 2 -2.945347 3.008369
```

Q. Plot x colored by the kmeans cluster assignment and add cluster centers as blue points.

```
plot(data, col=km$cluster)
points(km$centers, col="blue", pch=15)
```



Hierarchical Clustering

We will use the hclust() function on the same data as before and see how this method works.

Unlike Kmeans, we'll need to do a little more work to determine the cluster membership when using Hclust.

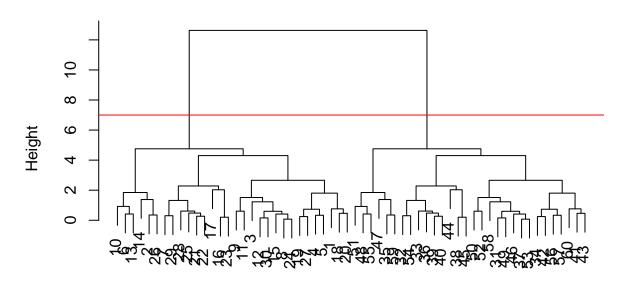
```
hc <- hclust(dist(data))
hc

##
## Call:
## hclust(d = dist(data))
##
## Cluster method : complete
## Distance : euclidean
## Number of objects: 60</pre>
```

Helust has a plot method:

```
plot(hc)
abline(h=7,col="red")
```

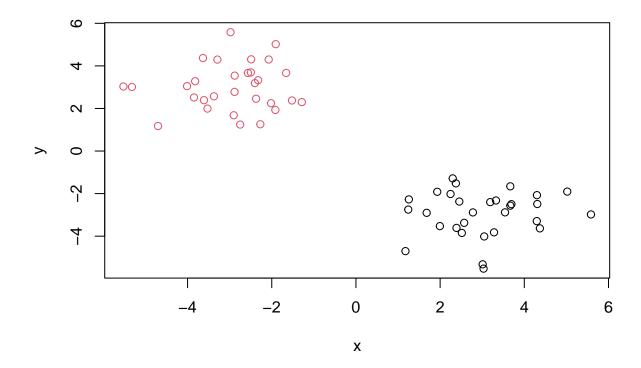
Cluster Dendrogram



dist(data) hclust (*, "complete")

To find our membership vector, we need to "cut the tree/dendrogram; for this, we use the cutree() function and tell it the height to cut at.

We can also use 'cutree()' and state the number of k clusters we want.



In sum, kmeans() requires that we specify the data and number of centers, while hclust() requires that we specify the distance/dissimilarity structure of the data.

Principal Component Analysis (PCA)

PCA is a useful analysis method when you have lots of dimensions in your data...

PCA of UK food data

First going to import the data from the csv file

```
url <- "https://tinyurl.com/UK-foods"
x <- read.csv(url)</pre>
```

Q. Complete the following code to find out how many rows and columns are in x? ____(x)

```
dim(x)
```

[1] 17 5

There's only meant to be 4 col in the dataset, because there are 4 countries. What's gone wrong?

Q. Preview the first 6 rows.

head(x)

```
##
                   X England Wales Scotland N.Ireland
## 1
              Cheese
                          105
                                 103
                                           103
                                                       66
      Carcass_meat
## 2
                          245
                                 227
                                           242
                                                      267
## 3
        Other_meat
                          685
                                 803
                                           750
                                                      586
## 4
                Fish
                          147
                                 160
                                           122
                                                       93
                                                      209
## 5 Fats_and_oils
                          193
                                 235
                                           184
## 6
              Sugars
                                 175
                                           147
                                                      139
                          156
```

We can see that the row titles are being stored as a column. Let's fix it.

```
rownames(x) <- x[,1]
x <- x[,-1]
head(x)
```

```
##
                   England Wales Scotland N. Ireland
                                        103
## Cheese
                        105
                               103
                                                     66
## Carcass_meat
                        245
                               227
                                        242
                                                    267
## Other_meat
                              803
                                        750
                                                    586
                        685
## Fish
                        147
                               160
                                        122
                                                    93
## Fats_and_oils
                        193
                                        184
                                                    209
                               235
## Sugars
                        156
                              175
                                        147
                                                    139
```

```
x <- read.csv(url, row.names=1)
head(x)</pre>
```

##	England	Wales	Scotland	N.Ireland
## Cheese	105	103	103	66
## Carcass_meat	245	227	242	267
## Other_meat	685	803	750	586
## Fish	147	160	122	93
## Fats_and_oils	193	235	184	209
## Sugars	156	175	147	139

dim(x)

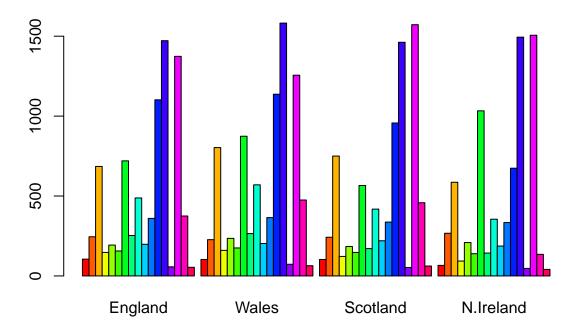
[1] 17 4

Much better!

Q2. Which approach to solving the 'row-names problem' mentioned above do you prefer and why? Is one approach more robust than another under certain circumstances?

The first approach (ie. using x <-x[,-1]) will remove data each time it is run (ie. if run again, the England column would disappear and the row names would become the values from that deleted column). We should instead just reload the data using an argument in the read.csv() function, which loads the data in as we'd like without having to manipulate the data further.

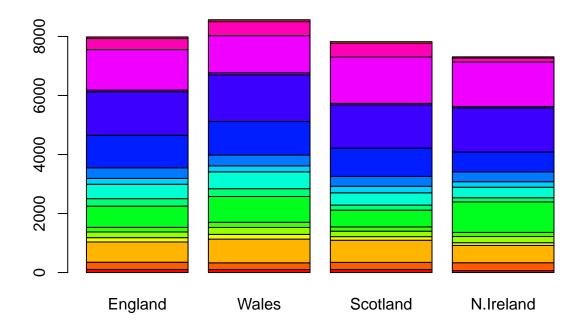
Let's plot the data



Q3. Changing what optional argument in the above barplot() function results in the following plot?

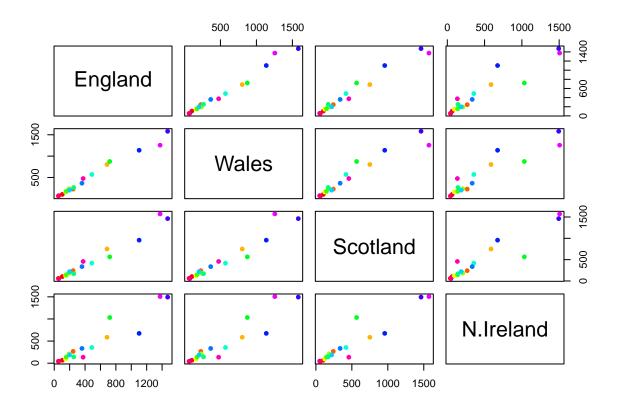
If we remove the beside=T argument, then the bars will not be plotted besides one another. See below.

barplot(as.matrix(x),col=rainbow(nrow(x)))



Q5. Generating all pairwise plots may help somewhat. Can you make sense of the following code and resulting figure? What does it mean if a given point lies on the diagonal for a given plot?

```
mycols <- rainbow(nrow(x))
pairs(x,col=mycols, pch=16)</pre>
```



The axes for each plot are determined by where the countries' names are positioned. The vertical axis for each row of plots is indicated by the country name in that row, while the horizontal axis for each column of plots is indicated by the country name in that column.

Eg. the vertical axis for the first row of plots is England, while the horizontal axis for the first column of plots is England. In the second plot of the first row (ie. plot to the right of 'England'), the axes are England v. Wales.

If the values for each country are the same, the respective point for that value should be found on the diagonal (where x=y). We can look for departures from the diagonal to identify instances in which the values in a comparison are significantly different.

Q6. What is the main differences between N. Ireland and the other countries of the UK in terms of this data-set?

Ask: as in which values are different for N. Ireland? Or just that N. Ireland is the most unique (ie. had the most values that deviate significantly/exhibit values that do not fall along the diagonal)

PCA to the rescue

Here we will use the base R function for PCA, which is called prcomp(). We'll need to transpose the data using t() so that the prcomp() function is analyzing the proper data.

t(x)

```
Cheese Carcass_meat Other_meat Fish Fats_and_oils Sugars
##
## England
                105
                               245
                                            685 147
                                                                 193
                                                                        156
## Wales
                103
                               227
                                            803
                                                                 235
                                                                        175
                                                 160
## Scotland
                103
                               242
                                            750
                                                 122
                                                                 184
                                                                        147
## N.Ireland
                 66
                               267
                                            586
                                                  93
                                                                 209
                                                                        139
##
             Fresh_potatoes Fresh_Veg Other_Veg Processed_potatoes
## England
                          720
                                     253
                                                 488
                                                                      198
## Wales
                          874
                                     265
                                                 570
                                                                      203
## Scotland
                          566
                                     171
                                                 418
                                                                      220
## N.Ireland
                         1033
                                     143
                                                 355
                                                                      187
             Processed_Veg Fresh_fruit
                                           Cereals
                                                    Beverages Soft_drinks
                                                           57
## England
                         360
                                     1102
                                               1472
                                                                       1374
## Wales
                         365
                                      1137
                                               1582
                                                            73
                                                                       1256
## Scotland
                         337
                                       957
                                               1462
                                                            53
                                                                       1572
## N.Ireland
                         334
                                       674
                                               1494
                                                            47
                                                                       1506
##
             Alcoholic_drinks
                                Confectionery
## England
                            375
                                             54
## Wales
                                             64
                            475
## Scotland
                            458
                                             62
## N.Ireland
                            135
                                             41
```

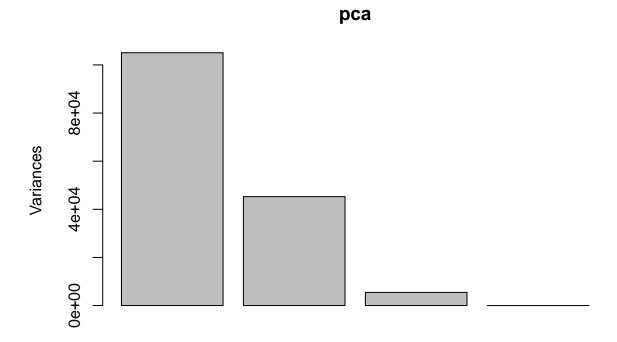
```
pca <- prcomp(t(x))
summary(pca)</pre>
```

```
## Importance of components:
```

```
## PC1 PC2 PC3 PC4
## Standard deviation 324.1502 212.7478 73.87622 4.189e-14
## Proportion of Variance 0.6744 0.2905 0.03503 0.000e+00
## Cumulative Proportion 0.6744 0.9650 1.00000 1.000e+00
```

What happens if we plot this pca data?

```
plot(pca)
```



We really want to visualize something called the score plot (a.k.a. PCA plot). This is basically the plot of PCA1 v. PCA2... etc.

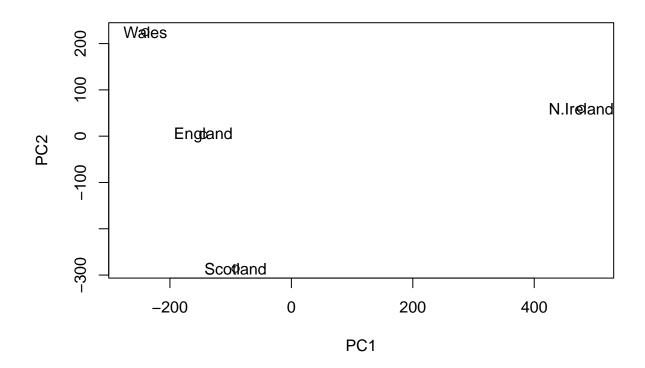
```
## $names
## [1] "sdev" "rotation" "center" "scale" "x"
##
## $class
```

We are after the pca\$x component for this plot. . .

[1] "prcomp"

Q7. Complete the code below to generate a plot of PC1 vs PC2. The second line adds text labels over the data points.

```
plot(pca$x[,1], pca$x[,2], xlab="PC1", ylab="PC2", xlim=c(-270,500))
text(pca$x[,1], pca$x[,2], colnames(x))
```



```
# In class, a shortened version of this was used:
# plot(pca$x[,1:2])
# text(pca$x[,1:2],labels=colnames(x))
```

Q8. Customize your plot so that the colors of the country names match the colors in our UK and Ireland map and table at start of this document.

vnskdfjbn

PCA "Loadings"

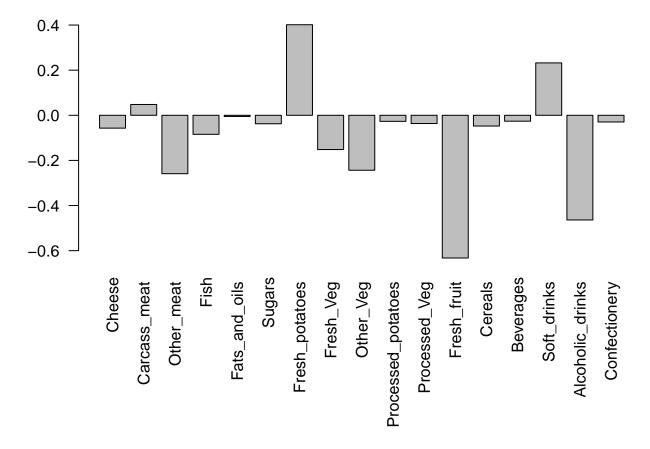
We can also examine the PCA "loadings", which tell us how much the original variable contibute to each PC. Lets focus on PC1 as it accounts for > 90% of variance.

pca\$rotation

```
##
                             PC1
                                          PC2
                                                     PC3
                                                                 PC4
                     -0.056955380 -0.016012850 -0.02394295 -0.691718038
## Cheese
## Carcass_meat
                      0.047927628 -0.013915823 -0.06367111
                                                          0.635384915
## Other_meat
                                  0.015331138 0.55384854
                     -0.258916658
                                                          0.198175921
## Fish
                     -0.084414983
                                  0.050754947 -0.03906481 -0.015824630
                                              0.12522257
## Fats_and_oils
                     -0.005193623
                                  0.095388656
                                                          0.052347444
## Sugars
                     -0.037620983
                                  0.043021699
                                              0.03605745
                                                          0.014481347
## Fresh_potatoes
                      0.401402060
```

```
## Fresh_Veg
                     -0.151849942  0.144900268  -0.21382237
                                                         0.056182433
                     ## Other_Veg
## Processed_potatoes -0.026886233 -0.042850761
                                              0.07364902 -0.022618707
## Processed_Veg
                     -0.036488269
                                 0.045451802 -0.05289191
                                                         0.009235001
## Fresh_fruit
                     -0.632640898
                                 0.177740743 -0.40012865 -0.021899087
## Cereals
                                              0.35884921
                                                         0.084667257
                     -0.047702858
                                 0.212599678
## Beverages
                                              0.04135860 -0.011880823
                     -0.026187756
                                 0.030560542
## Soft_drinks
                      0.232244140 -0.555124311
                                              0.16942648 -0.144367046
## Alcoholic_drinks
                     -0.463968168 -0.113536523
                                              0.49858320 -0.115797605
## Confectionery
                     -0.029650201 -0.005949921
                                              0.05232164 -0.003695024
```

```
par(mar=c(10,3,0.35,0))
barplot(pca$rotation[,1],las=2)
```



Along PC1 we can go in the positive or negative direction. Comparing this plot to the

One more PCA for today

```
url2 <- "https://tinyurl.com/expression-CSV"
rna.data <- read.csv(url2, row.names=1)
head(rna.data)</pre>
```

wt1 wt2 wt3 wt4 wt5 ko1 ko2 ko3 ko4 ko5

```
## gene1 439 458 408 429 420 90 88 86 90 93  
## gene2 219 200 204 210 187 427 423 434 433 426  
## gene3 1006 989 1030 1017 973 252 237 238 226 210  
## gene4 783 792 829 856 760 849 856 835 885 894  
## gene5 181 249 204 244 225 277 305 272 270 279  
## gene6 460 502 491 491 493 612 594 577 618 638
```

Q10: How many genes and samples are in this data set?

```
nrow(rna.data)
```

[1] 100

```
ncol(rna.data)
```

[1] 10

```
colnames(rna.data)
```

```
## [1] "wt1" "wt2" "wt3" "wt4" "wt5" "ko1" "ko2" "ko3" "ko4" "ko5"
```

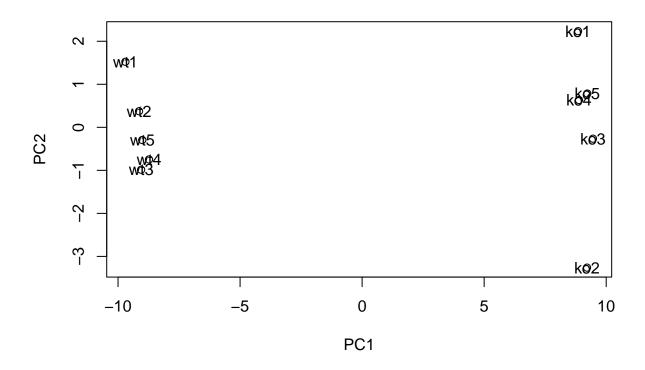
Let's run PCA!

Using the scale argument helps us to normalize for the differences in ranges between observations.

```
pca.rna <- prcomp(t(rna.data), scale=TRUE)</pre>
```

Let's make a basic plot of the data.

```
plot(pca.rna$x[,1], pca.rna$x[,2], xlab="PC1", ylab="PC2")
text(pca.rna$x[,1:2], labels = colnames(rna.data))
```



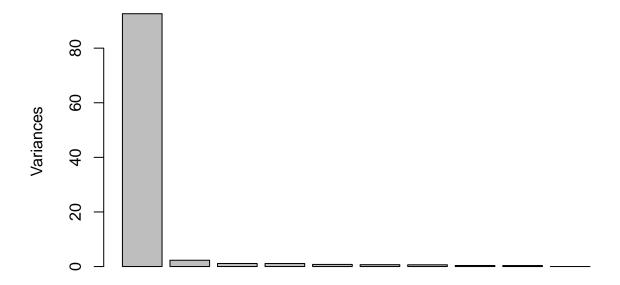
summary(pca.rna)

```
## Importance of components:
                                    PC2
                                                     PC4
##
                             PC1
                                            PC3
                                                             PC5
                                                                     PC6
                                                                             PC7
## Standard deviation
                          9.6237 1.5198 1.05787 1.05203 0.88062 0.82545 0.80111
## Proportion of Variance 0.9262 0.0231 0.01119 0.01107 0.00775 0.00681 0.00642
## Cumulative Proportion 0.9262 0.9493 0.96045 0.97152 0.97928 0.98609 0.99251
##
                              PC8
                                      PC9
                                               PC10
## Standard deviation
                          0.62065 0.60342 3.348e-15
## Proportion of Variance 0.00385 0.00364 0.000e+00
## Cumulative Proportion 0.99636 1.00000 1.000e+00
```

PC1 does very good at capturing the variance in the data, over 92% of variance is captured by PC1! Let's make a scree plot to visualize this.

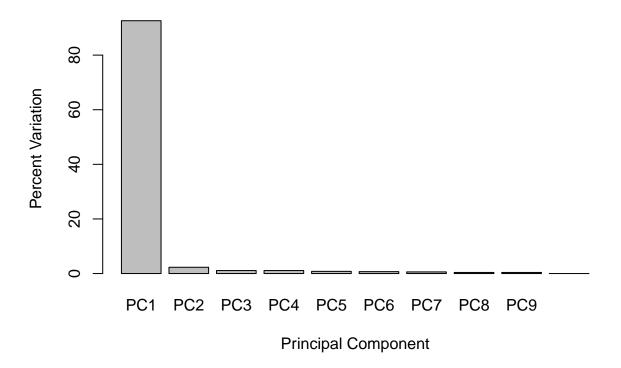
```
plot(pca.rna, main="Quick scree plot")
```

Quick scree plot



We can make our own scree plots too!

Scree Plot



We can make this a bit more useful and attractive by updating the script

