

Exercise 1: Trivial Exercise

This is an example document.

Question 1

$1 + 1 \stackrel{?}{=} 3.$

?

**Hint.** Consider  $1 + 1 = 2$ .



Claim 1

Yes.



*Proof of Claim 1.* This is a good question.

*quod  
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*Proof by Triviality.* Trivial.

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**Remark 1.** This is very trivial.



Theorem 1 – HelloWorld

This is NOT a theorem.

Definition 1 – Byebye

This is DEFINITELY a theorem.



## Chapter 1: Non-Trivial Chapter

Recall that we have already explained in lecture that all rational function of a single variable can be integrated in finite terms. Starting from there, we introduce integrals of the form, known as the **binomial integrals**:

$$(1) \quad J_{p,q} = \int (a + bz)^p z^q dz, a, b \in \mathbb{R}, p, q \in \mathbb{Q}.$$

This exercise aims at studying the rationalization of the binomial integral, as well as some of its applications.

## Question 1

Assume that  $p \in \mathbb{Z}$ , rationalise the integrand. ?

Since  $q \in \mathbb{Q}$ , this implies there exists  $m \in \mathbb{Z}, n \in \mathbb{N}$  such that  $q = \frac{m}{n}$ . Then,  $J_{p,q}$  can be written as

$$J_{p,q} = \int (a + bz)^p z^{\frac{m}{n}} dz.$$

Let  $z = x^n$ , then  $dz = n \cdot x^{n-1} dx$ . Replace  $z$  with  $x$  we have

$$J_{p,q} = \int (a + b \cdot x^n)^p \cdot (x^n)^{\frac{m}{n}} \cdot n \cdot x^{n-1} dx.$$

Simplify it and we get

$$J_{p,q} = n \int (a + b \cdot x^n)^p \cdot x^{m+n-1} dx.$$

Now, by binomial theorem we can see the integrand is rationalised, as needed. ☺

## Lemma 1

This is a lemma.

This is a math environment. ☺

## Corollary 1

This is a corollary.

## Exercise 2

## Question 1

We can see the question counter is auto reset to 1 when we start a new exercise / chapter / unit. ?

*Proof.* Proof by alittlebear.cls code, left as an exercise to the reader :)

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dem. ■

