

Building Temporal Graphs and Embeddings

A Practitioner's Approach

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About me

- Research background in security and non-monotonic systems
- Currently CTO at a DC-startup SignalFrame



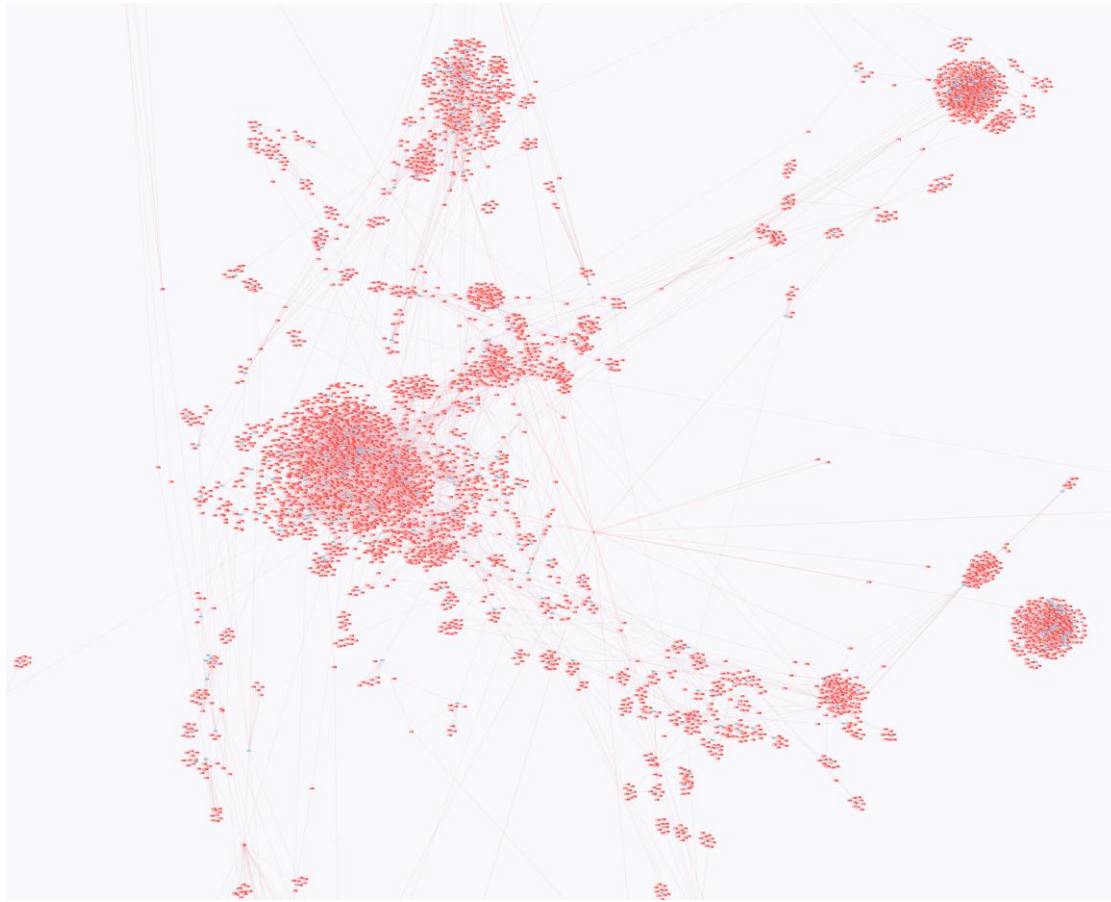
SignalFrame

- Indexing public WiFi/Bluetooth infrastructure
- Analyzing temporal changes and relationships between spaces and devices
 - Supplementing satellite image analysis
 - 2nd Factor Authentication
 - Market intelligence

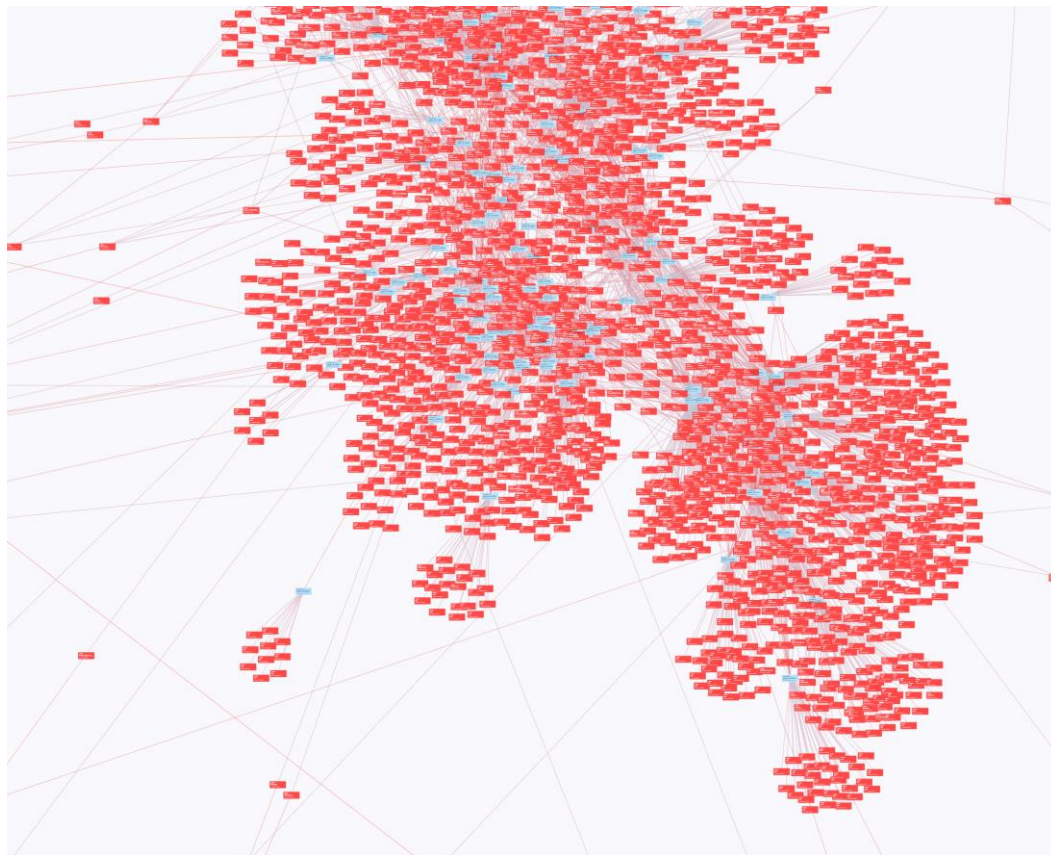
SignalGraph

- Signals are nodes in a streaming temporal graph
- **~ 6 billion nodes**
- **~ 100 billion edges**
- **~ 300 million updated nodes** per day
- **~ 1 billion edge** updates per day

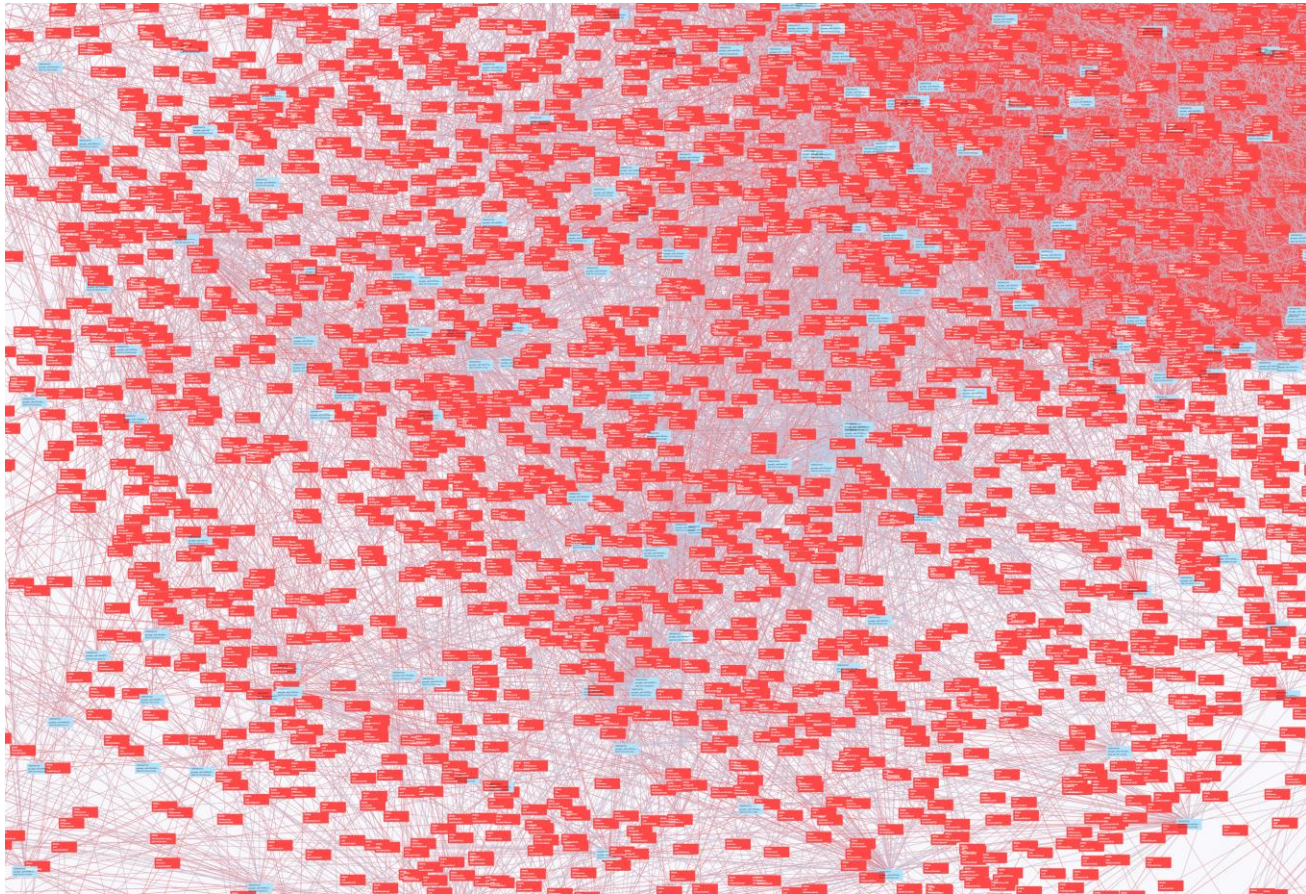
SignalGraph (GWU wifi @ 1 week Feb)



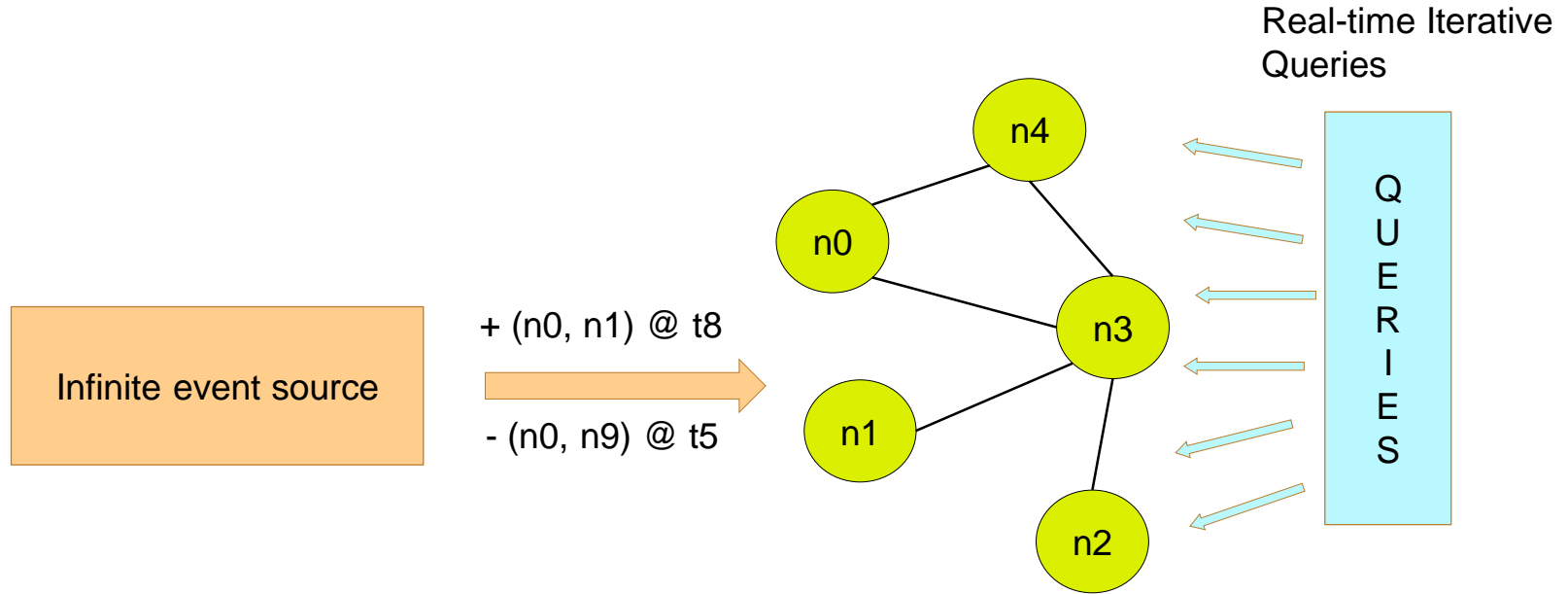
SignalGraph (GWU wifi @ 1 week Feb)



SignalGraph (GWU wifi @ 1 week Feb)



Temporal (Streaming) System Model

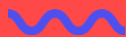


Temporal (Streaming) Systems

- Network analytics
 - Intrusion detection
- Recommendation engines
- User rankings
- Geo-temporal analytics

Practitioner's proposition

Model and analyze temporal graphs via explicit temporal nodes and edges.

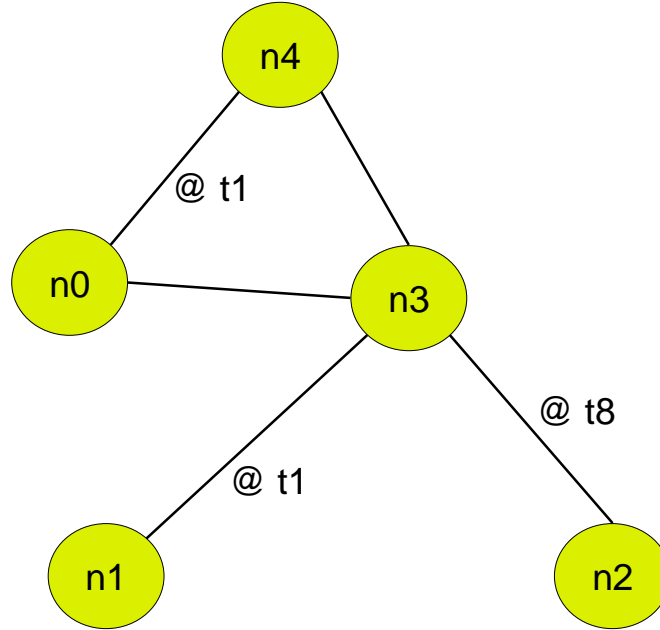


Temporal Graph Schema

Schema Goals

- Queries (lock-free)* parallelizable over time
- Implement on-top of existing DBs
- Maintain constant in-memory size
- Reduce time-filtering in batch queries
 - i.e. process only the necessary data

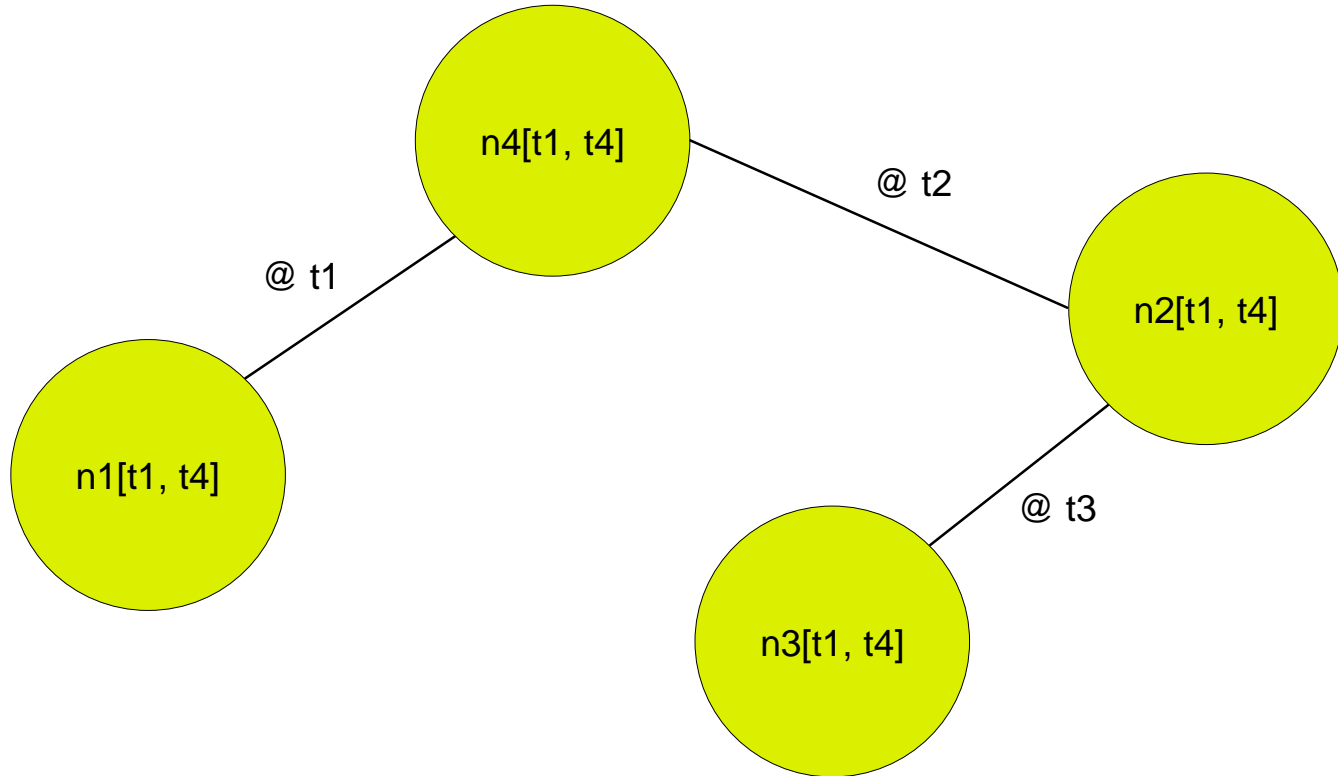
Strawman: Time as a (multi-)edge property



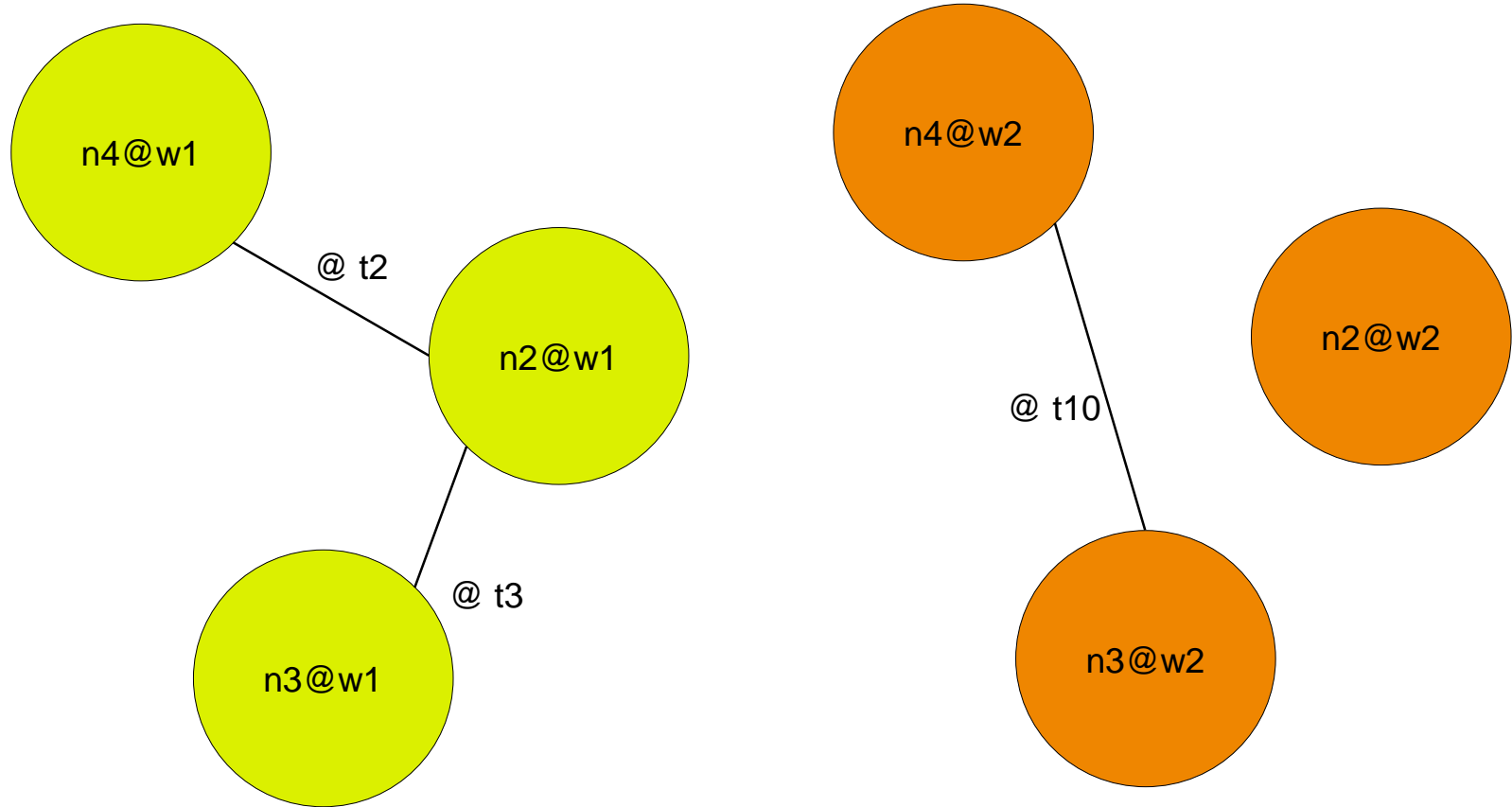
Strawman: Time as a (multi-)edge property

- Density edges/node increases with time
 - Limits the scalability for real-time and batch queries
- Limited concurrent access for reads and writes
- Makes time-constraints hard to implemented and scale

Timed Nodes: Time window part of a node's id

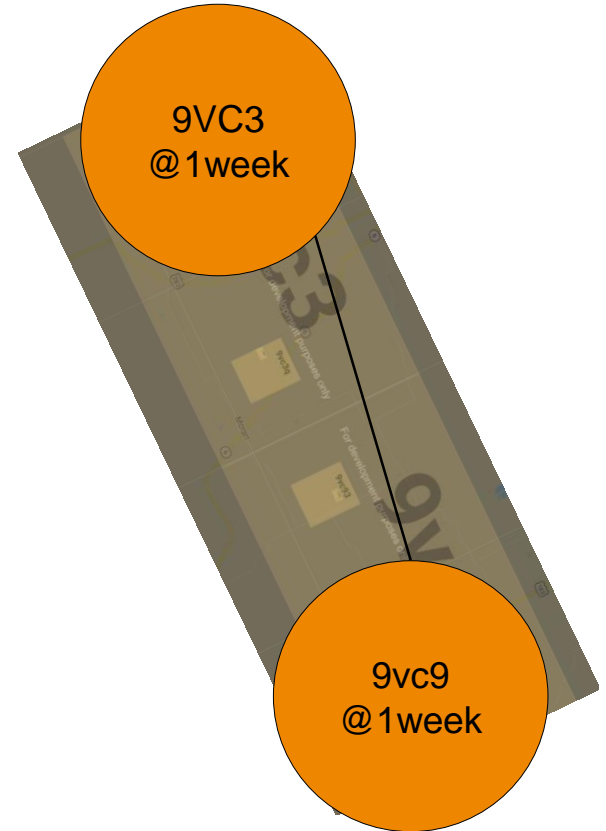


Timed Nodes: Time window part of a node's id

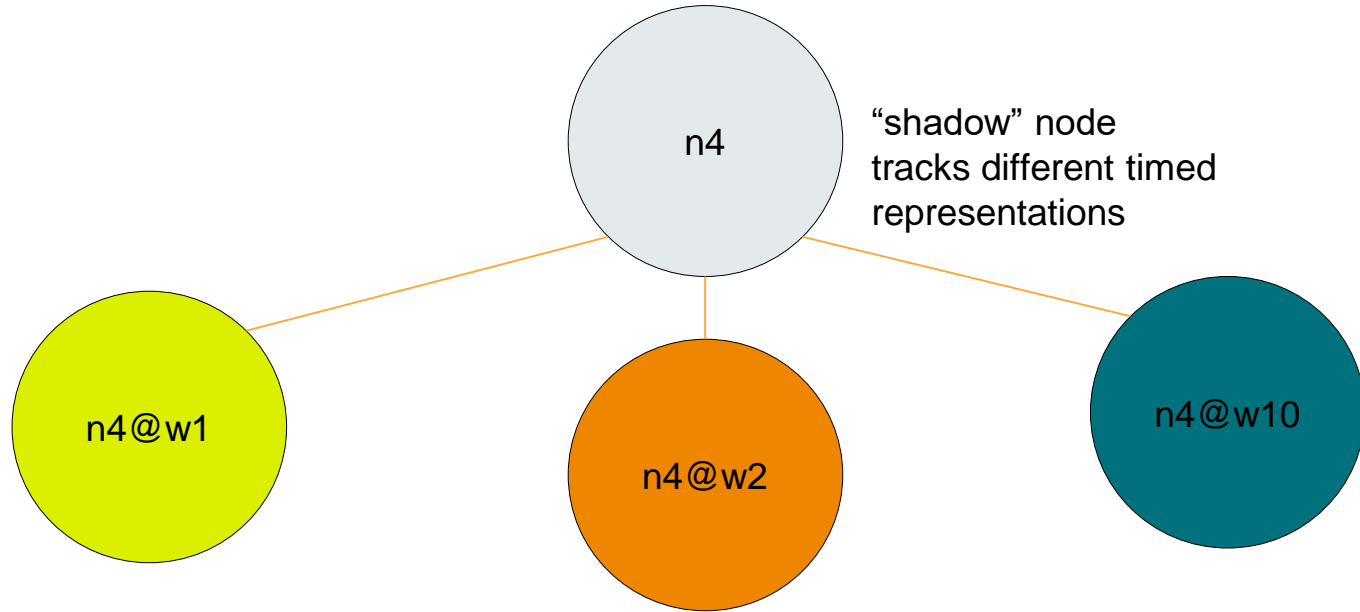


Windows need not be the same:

Geo-temporal analysis

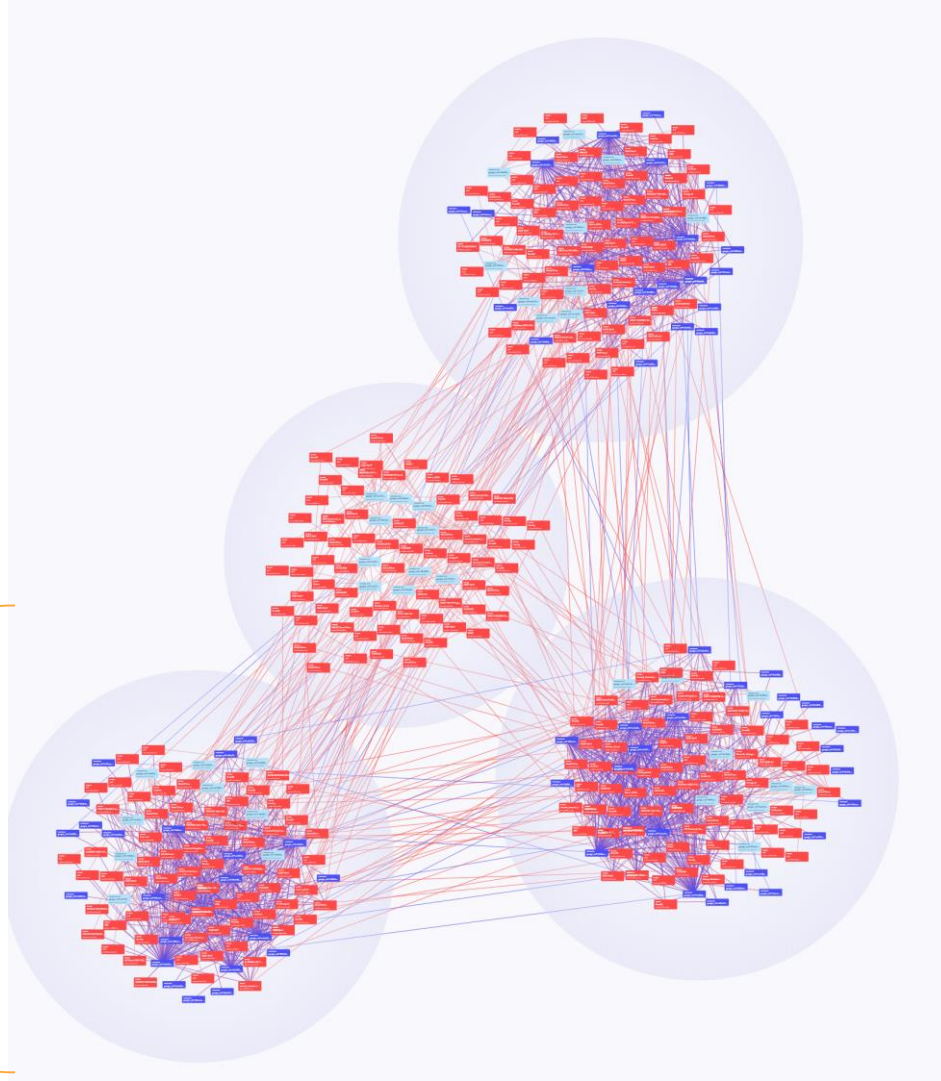


Timed Nodes: Time window part of a node's id



Note: suited for vertex-centric (adjacency list) storage

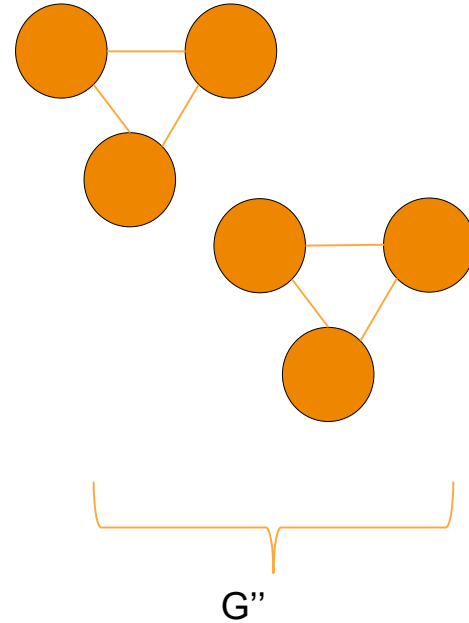
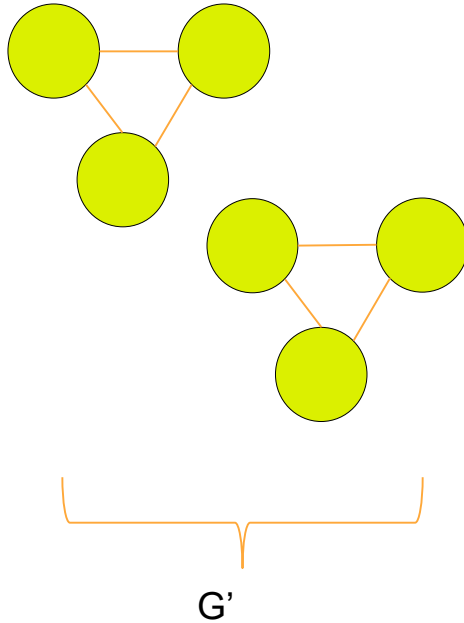
February 11-20



February 3-10

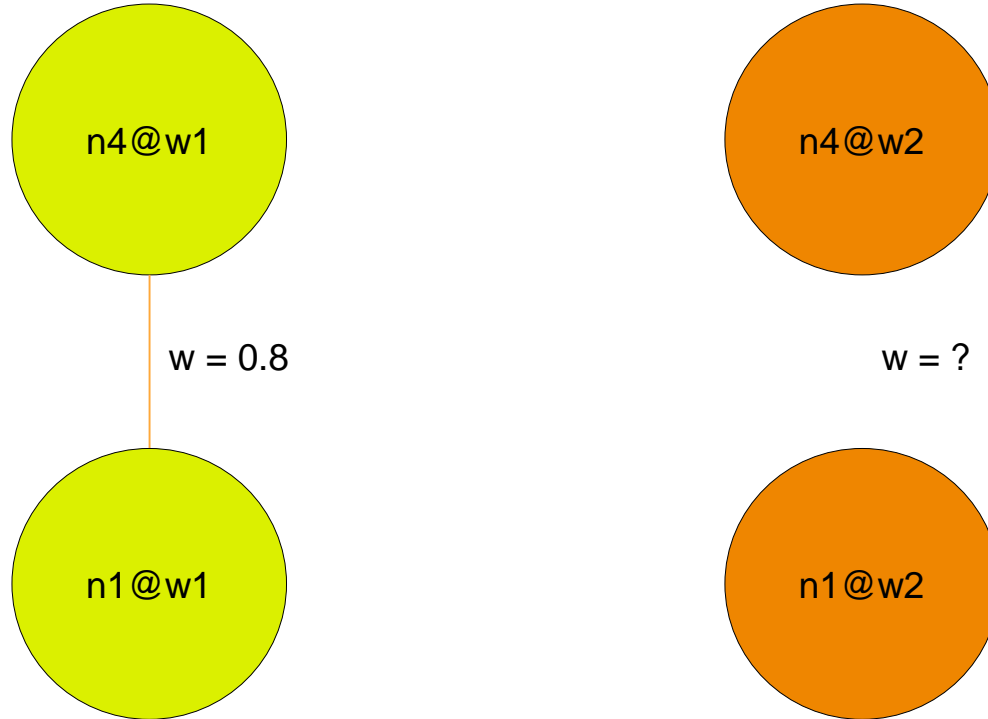
Timed Graphs:

Group windows into graphs for batch processing



Timed Nodes: Open-World Assumption

Are two nodes connected?



Timed Nodes: Open-World Assumption

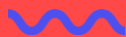
- Assume Closed-World
 - Set $w = 0$ if edge does not exist in past N windows
- Create snapshots of aggregated past windows
 - Propagate aggregated edges as a new edge
 - Can be done in a lazy (amortized) fashion

Related Work on Modelling/Processing Temporal Graphs

- Chronos: A Graph Engine for Temporal Graph Analysis
 - [Han et al 2014]
- **GraphOne: A Data Store for Real-time Analytics on Evolving Graphs**
 - [Kumar et al 2019]
- GraphTau: Time-Evolving Graph Processing at Scale
 - [Iyer et al 2016]
- Kineograph: Taking the Pulse of a Fast-Changing and Connected World
 - [Cheng et al 2012]
- A Foundation of Lazy Streaming Graphs
 - [Dexter et al 2019]
- KickStarter: Fast and Accurate Computations on Streaming Graphs via Trimmed Approximations
 - [Vora et al 2017]

Timed Nodes Schema: Summary

- Nodes sharded across time windows.
- Length of windows can be learnt from the stream.
- Pro: Can be implemented on top of existing Graph/KV DBs
- Pro: Well suited for concurrent reads/writes
- Pro: Reduces density edges/nodes
- Pro: Easy to drop past data and have a constant in-mem size
- Con: Requires an additional query layer
- Con: Requires dealing with Open-World and snapshots



Temporal Embeddings

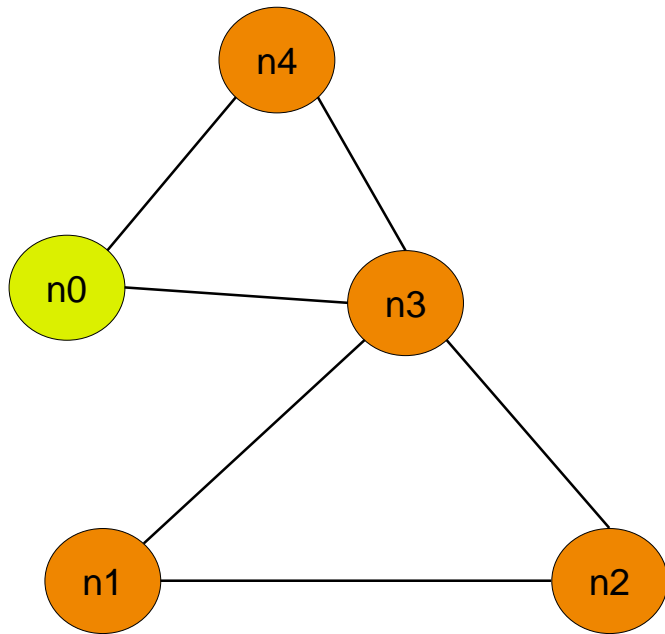
Embedding Goals

- Expose changes in a node's behaviour over arbitrary time windows.
- Account for different levels of activity across time.
- Deal with infinite node sets.
 - or at least billions of nodes

(Static) Embeddings

- $f_{embed} : Node \rightarrow R^d$
 - (Ideally, $d \ll \text{number of nodes}$)
- Two main approaches:
 - Laplacian Eigenvectors
 - Random-walk skip-gram models

Random-walk skip-gram

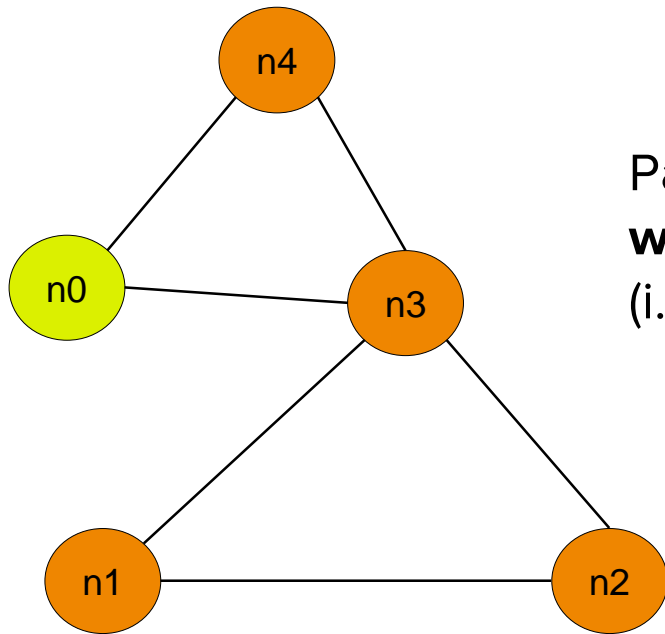


Multiple walks per node
e.g.

Walk = [n4,n3,n2,n1]

Skip-window-1 = [
(n4,n3)
(n3,n4)
(n3,n2)
(n1,n2)
]

Random-walk skip-gram



Pairs can be fed into an encoder, ala **word2vec**, to produce the embeddings (i.e. the net's inner layer).

Strawman Temporal Embedding 1

- Train on random walks across all time windows to produce one embedding per node.
- Does not model change over time.
- Does not differentiate between different levels of activity over time.

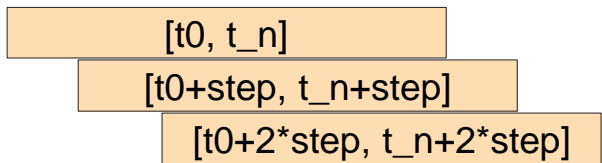
Strawman Temporal Embedding 2

- Apply skip-gram model to each timed node
 - Add regularization to “shadow” (non-temporal) nodes
 - Use strawman-1 embeddings as priors
- Still need to deal with:
 - “infinite” (streaming) graphs?
 - no activity?
 - different levels of activity?

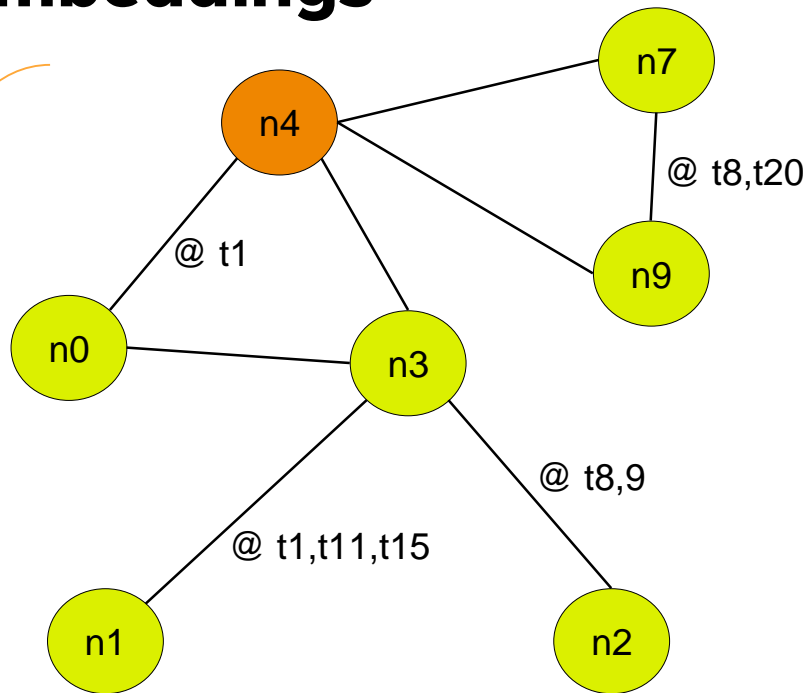
SignalFrame's Quasi-Embeddings

1. Build random-walks per node per sliding windows
2. **Aggregate random-walks from connected components into a sparse vector**
 - **NLP/IR: Each vector is a document with nodes as dimensions.**
3. Collect all sparse vectors per connected components per sliding windows

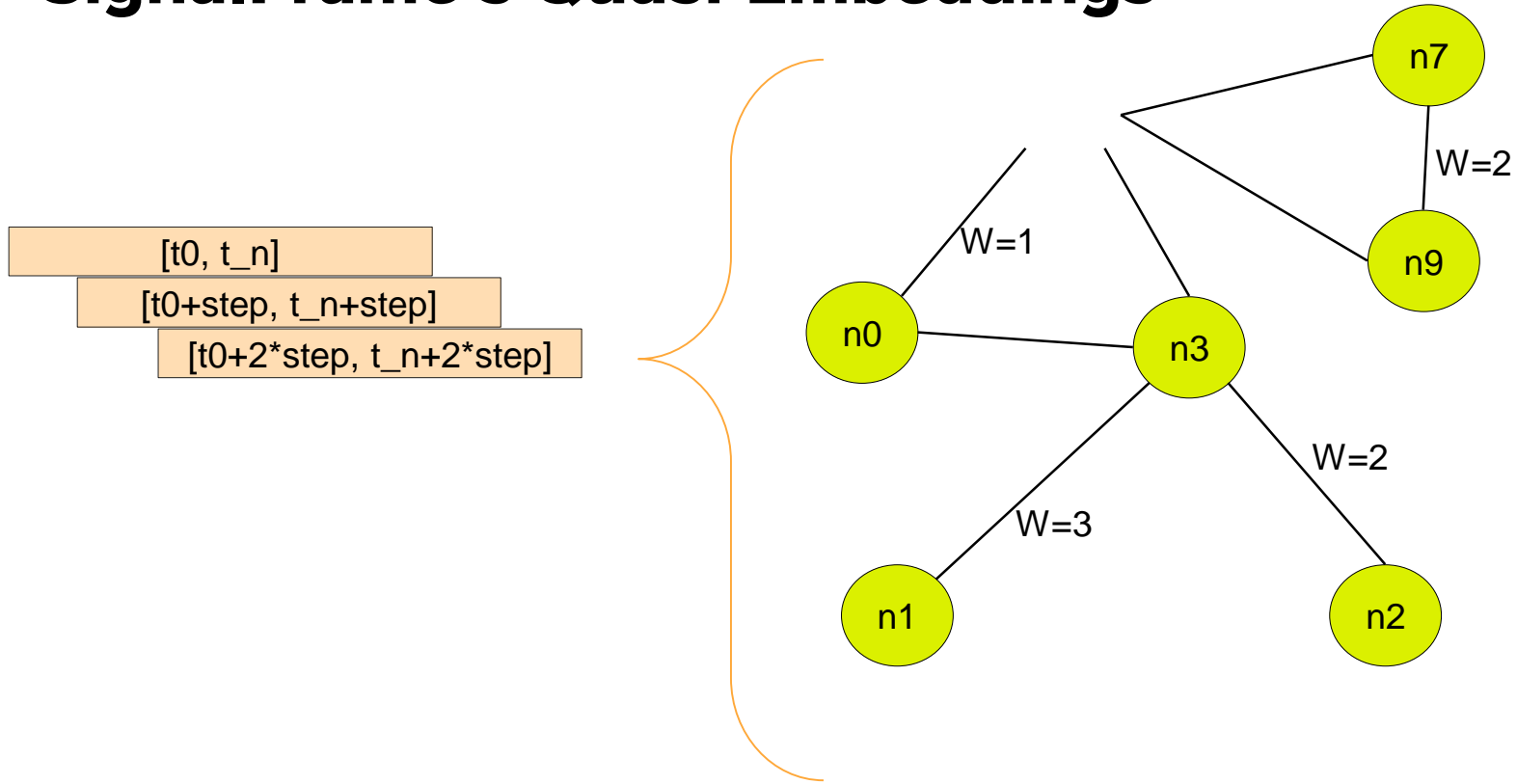
SignalFrame's Quasi-Embeddings



Build embeddings for $[t_0, t_m]$ with some step.
Step and size hyper-params can result in a smoother-transition between embeddings.



SignalFrame's Quasi-Embeddings



SignalFrame's Quasi-Embeddings

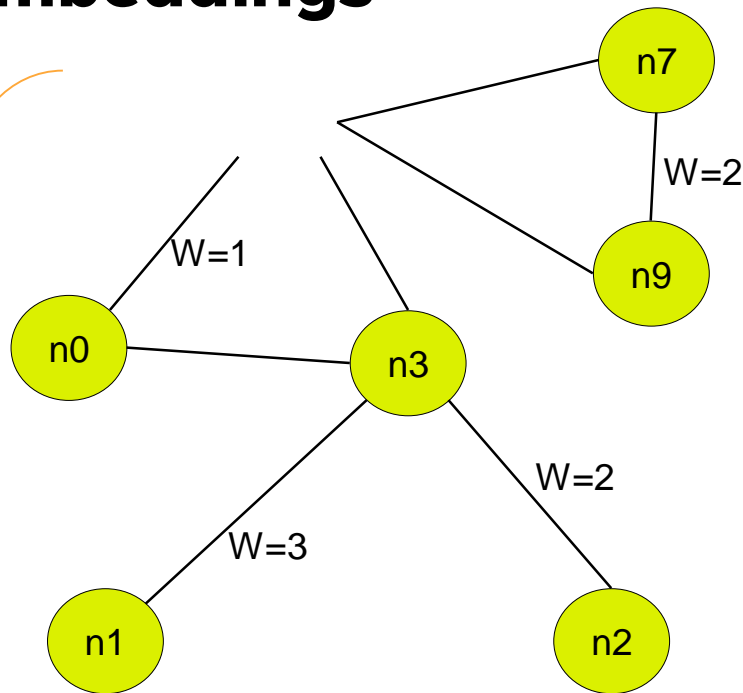
Generate weighted random walks per connected component.
Starting at the hidden node (in this case n4)

(n0, n3, n1)
(n0, n3, n2)
...

} \sum "document" vector

(n7, n9)
(n7, n9)
...

} \sum "document" vector

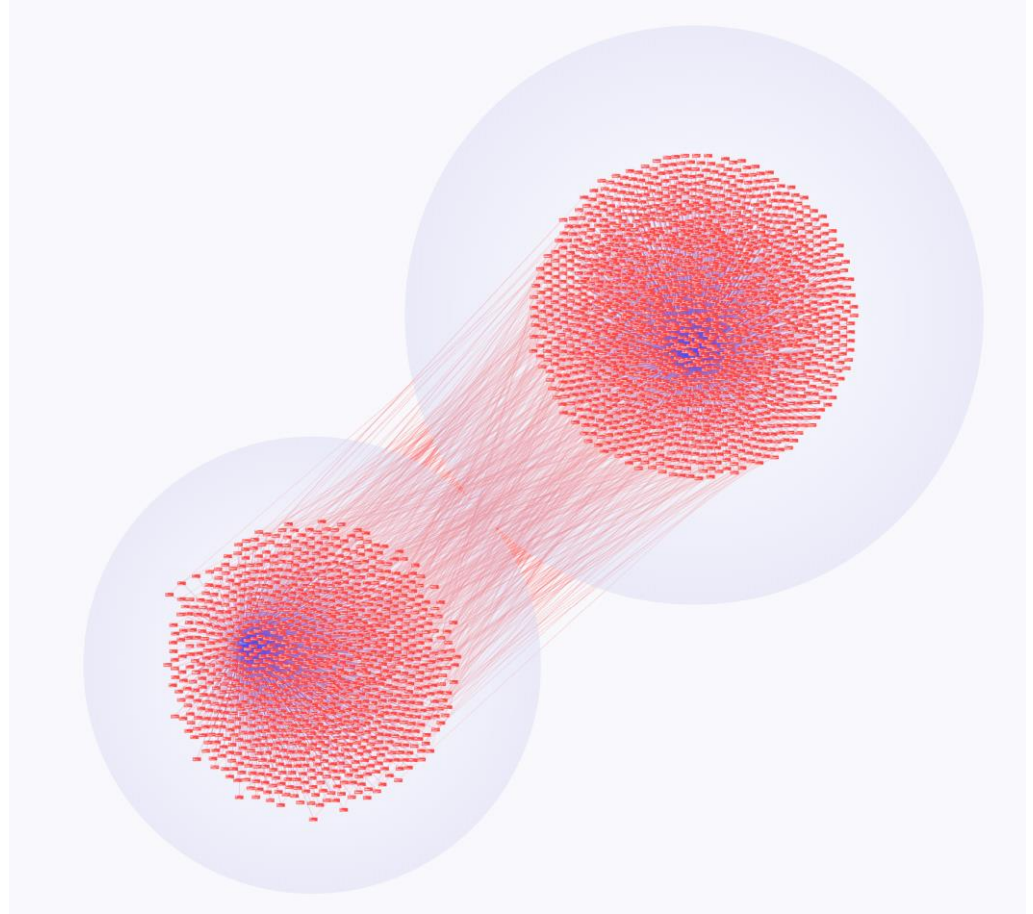


SignalFrame's 2nd Factor Authentication

A bubble is a time window of 14 days, with a 3-day overlap.

A bubble represents all 1-hop neighbours of a device that we want to authenticate.

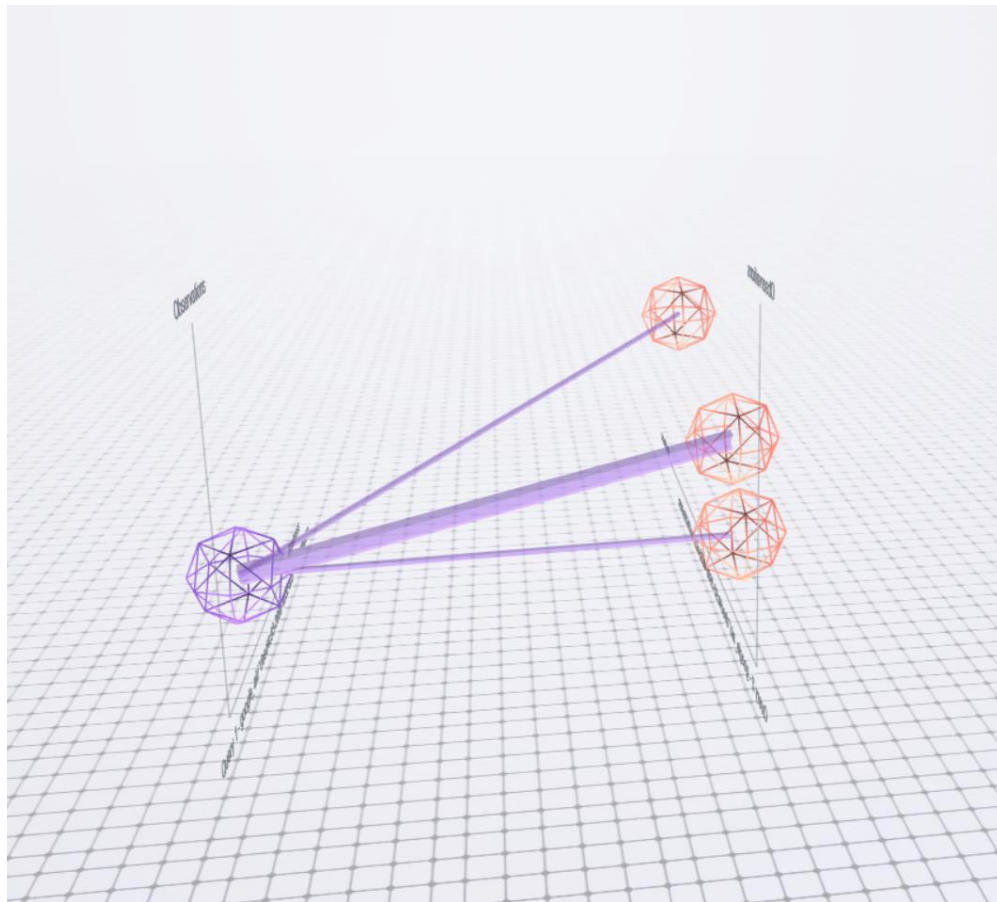
Has the behaviour changed?



SignalFrame's 2nd Factor Authentication

Reduction to temporal embeddings.

Has the behaviour changed?



SignalFrame's 2nd Factor Authentication

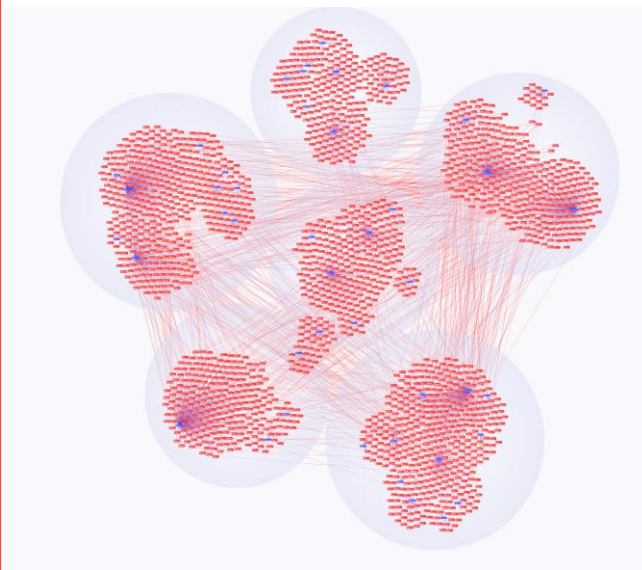
Embedding is a “signal” document.

All other signals are noise.

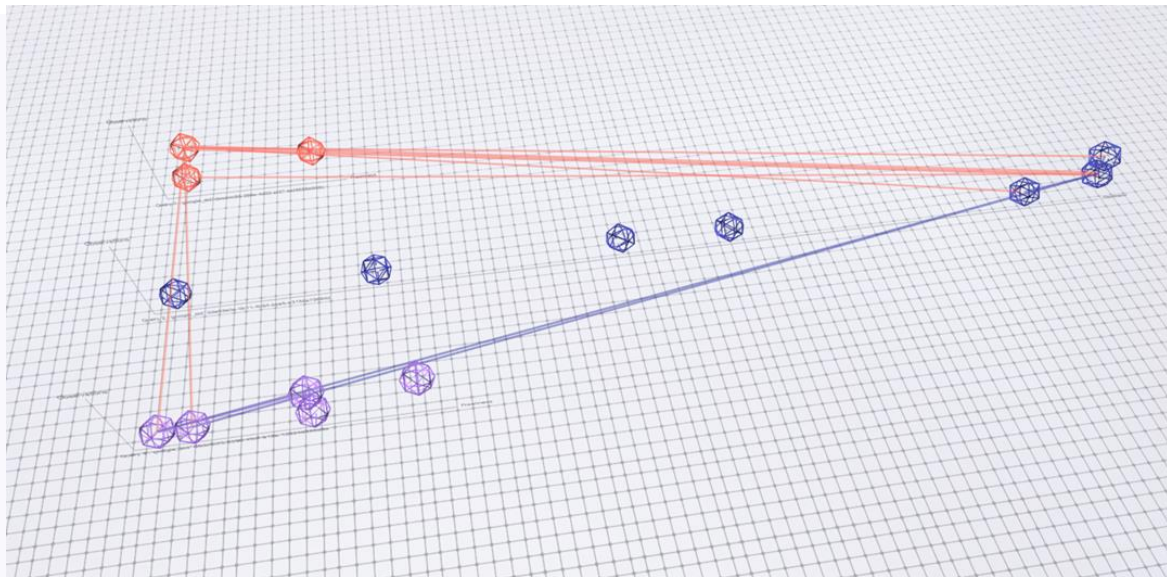


Similarity between sets of temporal embeddings

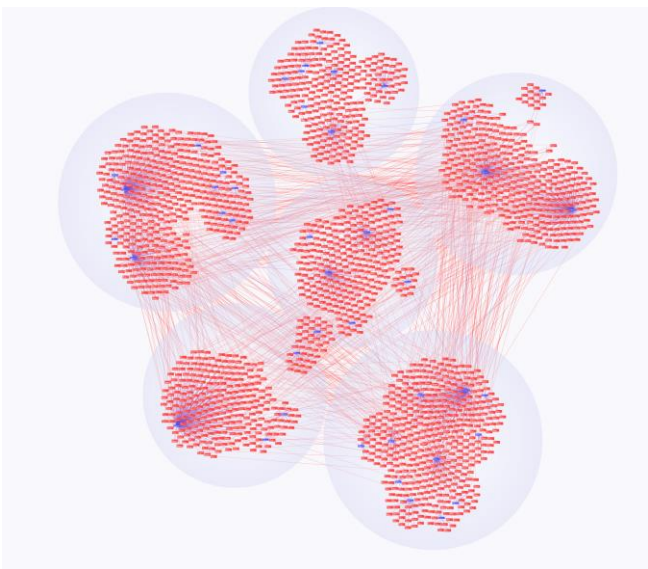
- Still need to address:
 - Different amount of evidence for the activity during a time window
 - Different set sizes, i.e. presence and absence of activity



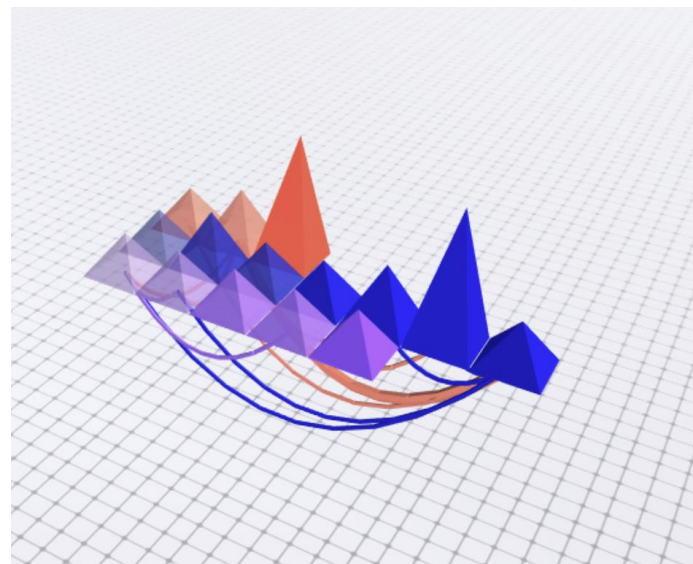
3 devices; 2 temporal
communities per device



Embeddings per device (derived from
sliding over temporal communities)



3 devices; 2 temporal
communities per device



Embeddings per device (derived from
sliding over temporal communities)

Similarity between sets of temporal embeddings

- $f : 2^{Embedding} \times 2^{Embedding} \rightarrow R$
- Input:
 - $M(n,m)$ – pairwise cosine between sets A, B
 - `weights_a` – weights associated to members of A
 - `weights_b` – weights associated to members of B

Sketch

1. W , where $w(i,j) = \mathbf{min}(\text{weights_a}(i), \text{weights_b}(j))$
2. $S = M \circ W$ // *Hadamard product*
3. $\text{score} = \mathbf{max}(\sum_i^n \mathbf{max}(S(i,.)), \sum_j^m \mathbf{max}(S(.,j)))$
4. $\text{decay} = \mathbf{max}(\mathbf{Onorm}(\text{Max}_i^n M(i,.)), \mathbf{Onorm}(\text{Max}_j^m M(.,j)))$
 1. $\text{Onorm}(\text{vector}) := (\text{len_non_zero}(\text{vector}) + 1) / (\text{len}(\text{vector}) + 1)$
5. **return** $\text{score} * \text{decay}$

Related Work on Graph Embeddings

- Laplacian Eigenmaps and Spectral Techniques for Embedding and Clustering
 - [Belkin et al 2000]
- DeepWalk: Online Learning of Social Representations
 - [Perozzi et al 2014]
- node2vec: Scalable Feature Learning for Networks
 - [Grover et al 2016]
- struc2vec: Learning Node Representations from Structural Identity
 - [Ribeiro et al 2017]
- **Is a Single Embedding Enough? Learning Node Representations that Capture Multiple Social Contexts**
 - [Epasto et al 2019]

Temporal (Quasi-)Embeddings Summary

- Pro: Can be done in pseudo real-time for some use-cases
- Pro: Explicit similarity model for sets of embeddings
- Pro: Process new nodes in a streaming mode
- Con: Dimensions are not reduced
- Con: No explicit cost function

Future Work

- Focus on structural embeddings (ala struct2vec) but with infinite inputs
 - Use quasi-embeddings as “syntactic” embedding
- Explore how/if Graph NNs can be used for structural analysis

Thanks.