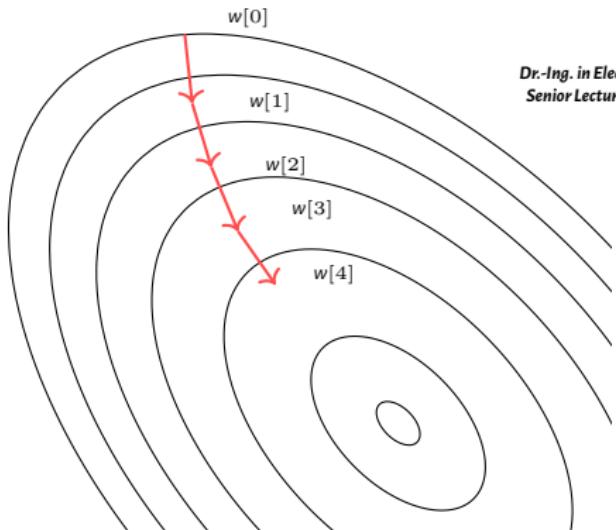


An Introduction To Machine Learning¹

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Senior Lecturer at ISET Bizerte*



“Computers are able to see, hear and learn.
Welcome to the future.”

Dave Waters

“This is nothing. In a few years, that bot will move
so fast you'll need a strobe light to see it.
Sweet dreams...”

Elon Musk

“Machine intelligence is the last invention
that humanity will ever need to make.”

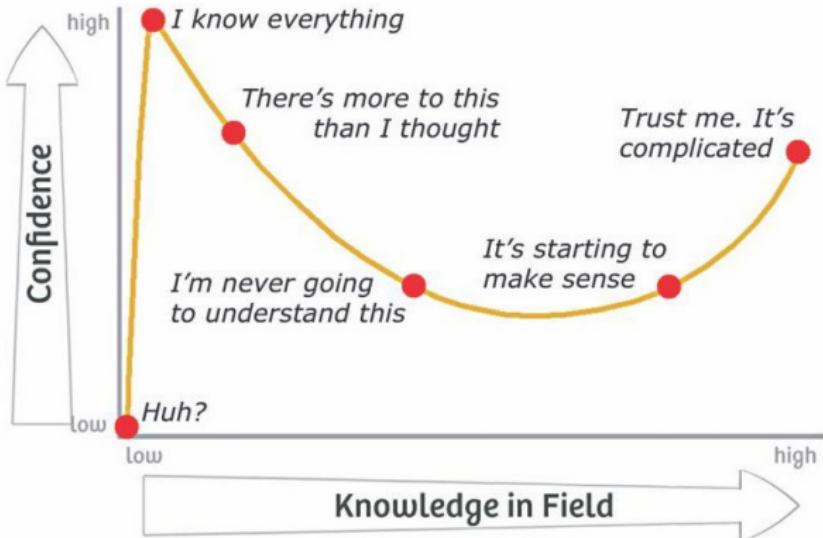
Nick Bostrom

¹Available @ <https://github.com/a-mhamdi/mlpy>

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Dunning-Kruger Effect

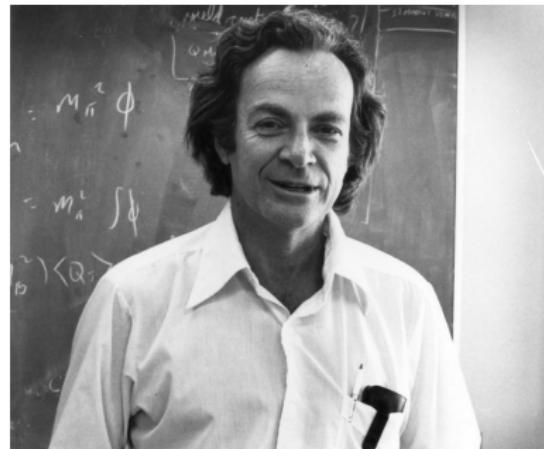


Kruger, J. and Dunning, D. (1999) *Unskilled and unaware of it: How difficulties in recognizing one's own incompetence lead to inflated self-assessments.* *J Pers Soc Psychol.* 77(6) pp. 1121–1134.

[doi:10.1037/0022-3514.77.6.1121](https://doi.org/10.1037/0022-3514.77.6.1121)

“Knowledge isn't free. You have to pay attention.”

Richard P. Feynman

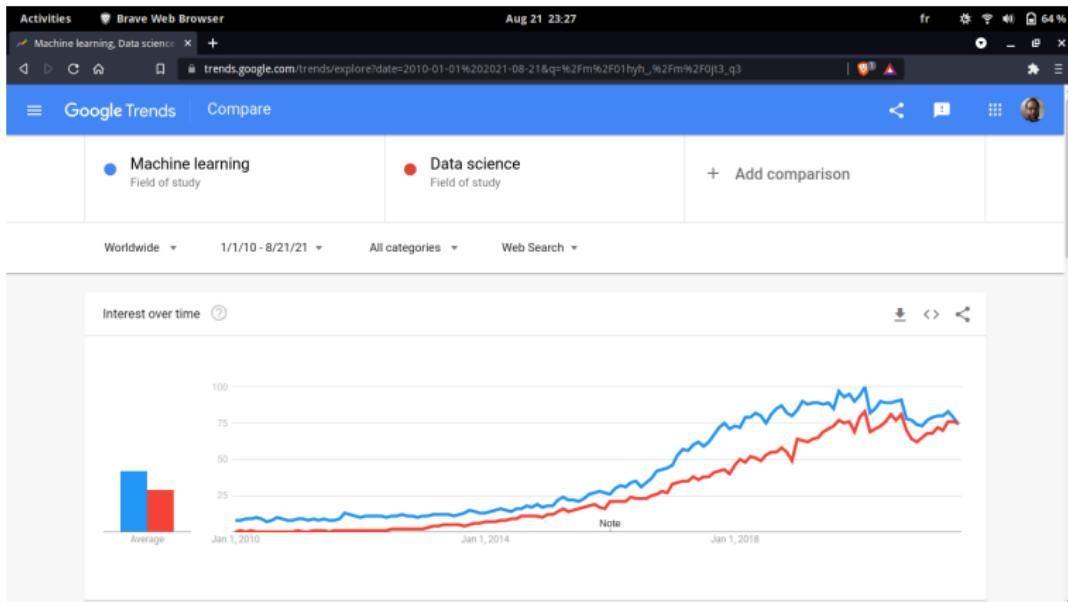


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- 2 Supervised Learning
- 3 Unsupervised Learning
- 4 Artificial Neural Network
- 5 Large Language Model
- 6 Complementary Lab. Project
- 7 ML Landscape through Quizzes

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Trends



"Numbers represent search interest relative to the highest point on the chart for the given region and time.

- A value of 100 is the peak popularity for the term;
- A value of 50 means that the term is half as popular;
- A score of 0 means there was not enough data for this term."

Global Data Traffic



Update on the internet in real time is available [here](#).

Top Uses



Literature Review (1/2)

“The field of machine learning is concerned with the question of how to construct computer programs that automatically improve with experience.”

Mitchell, T. (1997) *Machine Learning*. McGraw-Hill International Editions. McGraw-Hill.

Literature Review (2/2)

“Machine learning (ML) is a scientific discipline that concerns developing learning capabilities in computer systems. Machine learning is one of central areas of Artificial Intelligence (AI). It is an interdisciplinary area that combines results from statistics, logic, robotics, computer science, computational intelligence, pattern recognition, data mining, cognitive science, and more.”

Wojtusiak, J. (2012) [Machine learning](#). In *Encyclopedia of the Sciences of Learning*, pages 2082–2083. Springer US.

Debrief

Arthur Samuel (1959)

Machine Learning: Field of study that gives computers the ability to learn without being explicitly programmed.

Tom Mitchell (1998)

Well-posed Learning Problem: A computer is said to learn from experience \mathcal{E} with respect to some task \mathcal{T} and some performance measure \mathcal{P} , if its performance on \mathcal{T} , as measured by \mathcal{P} , improves with experience \mathcal{E} .

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Task #1

Suppose your email program watches which emails you do or do not mark as spam, and based on that learns how to better filter spam. What is the task \mathcal{T} in this setting?

- ① Classifying emails as spam or not spam;
- ② Watching you label emails as spam or not spam;
- ③ The number (or fraction) of emails correctly classified as spam/not spam;
- ④ None of the above-this not a machine learning problem.

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Task #1

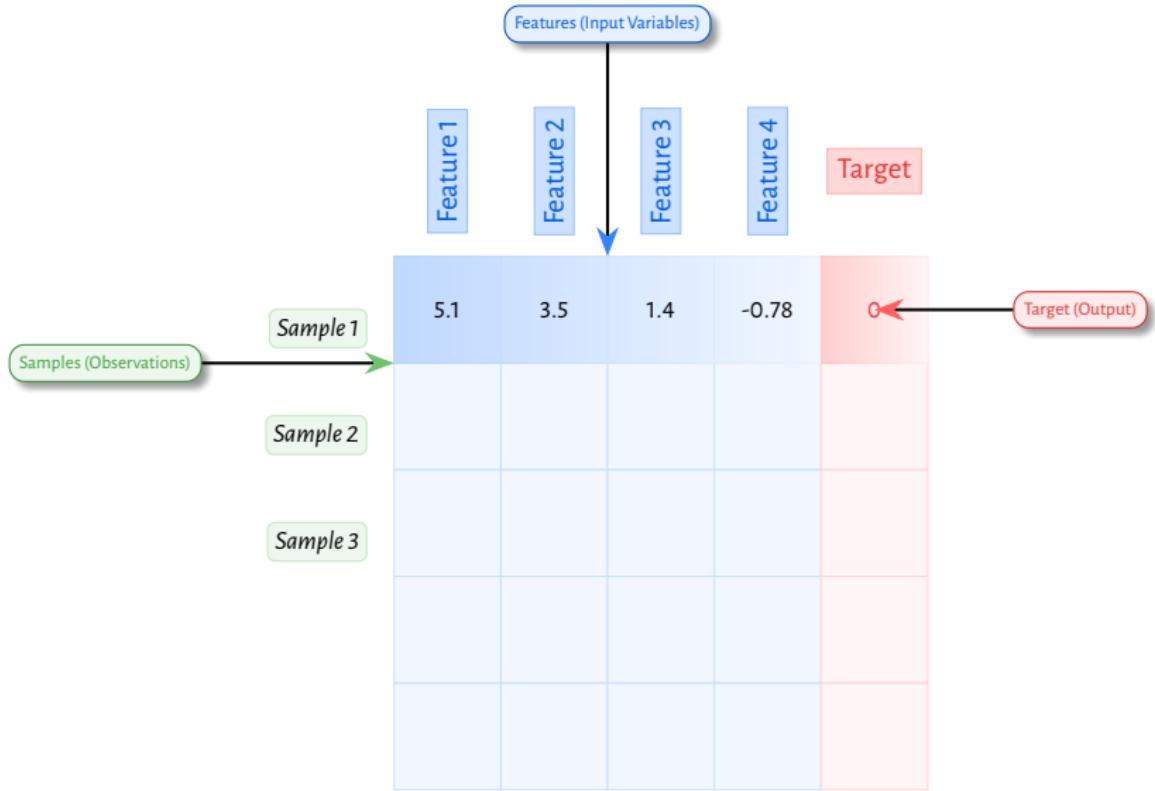
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Terminology (1/4)

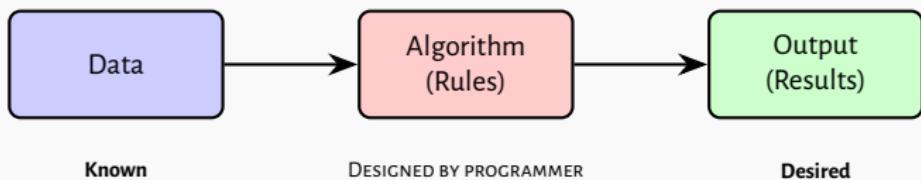
- ▶ Dataset is a structured collection of data organized for analysis or processing. Good datasets often contain diverse, representative examples with clear labels for the information they contain.
(e.g., census records, medical images, customer purchases.)
- ▶ Feature is an input variable or an attribute used to make predictions.
- ▶ Target is the output variable the model is trained to predict.
- ▶ Model is an algorithm that learns patterns from data to make predictions or decisions. Models transform inputs into outputs based on parameters that are optimized during training.
(e.g., neural networks, decision trees, regression.)

Terminology (2/4)



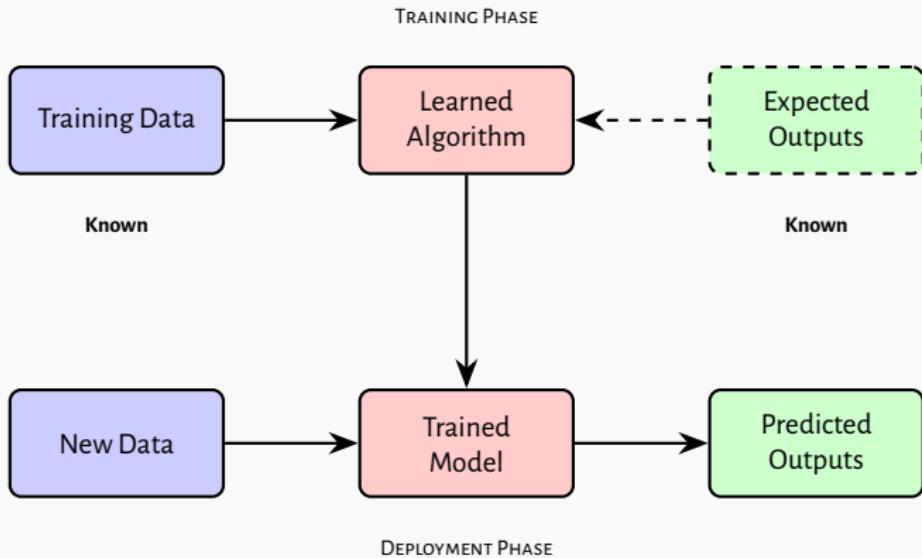
Terminology (3/4)

Classical Programming Paradigm



Terminology (4/4)

Machine Learning Paradigm



Learning Paradigms

- ▶ Supervised Learning is a machine learning approach where algorithms learn from labeled training data to predict outputs for new inputs. The algorithm is "supervised" by being shown correct answers during training, allowing it to learn the relationship between features and target variables.
(e.g., spam filtering, image classification, price prediction.)
- ▶ Unsupervised Learning is a machine learning approach where algorithms find patterns in data without explicit labels or guidance. These algorithms identify inherent structures in data, such as groupings, anomalies, or distribution characteristics.
(e.g., clustering, anomaly detection, dimensionality reduction.)

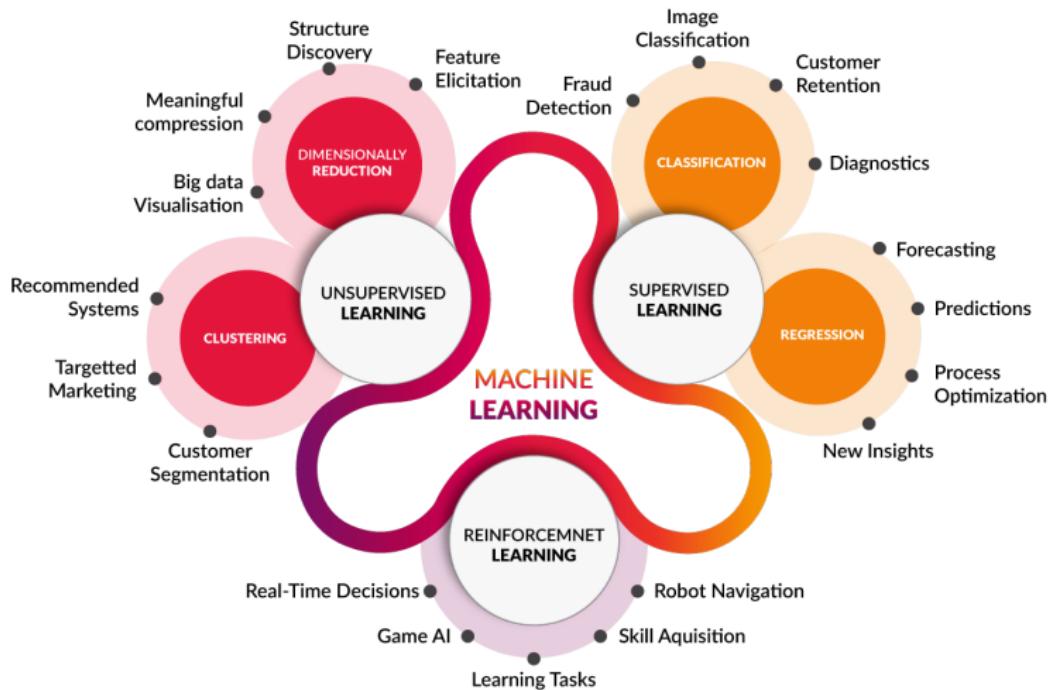
Learning Paradigms

COMMON TASKS

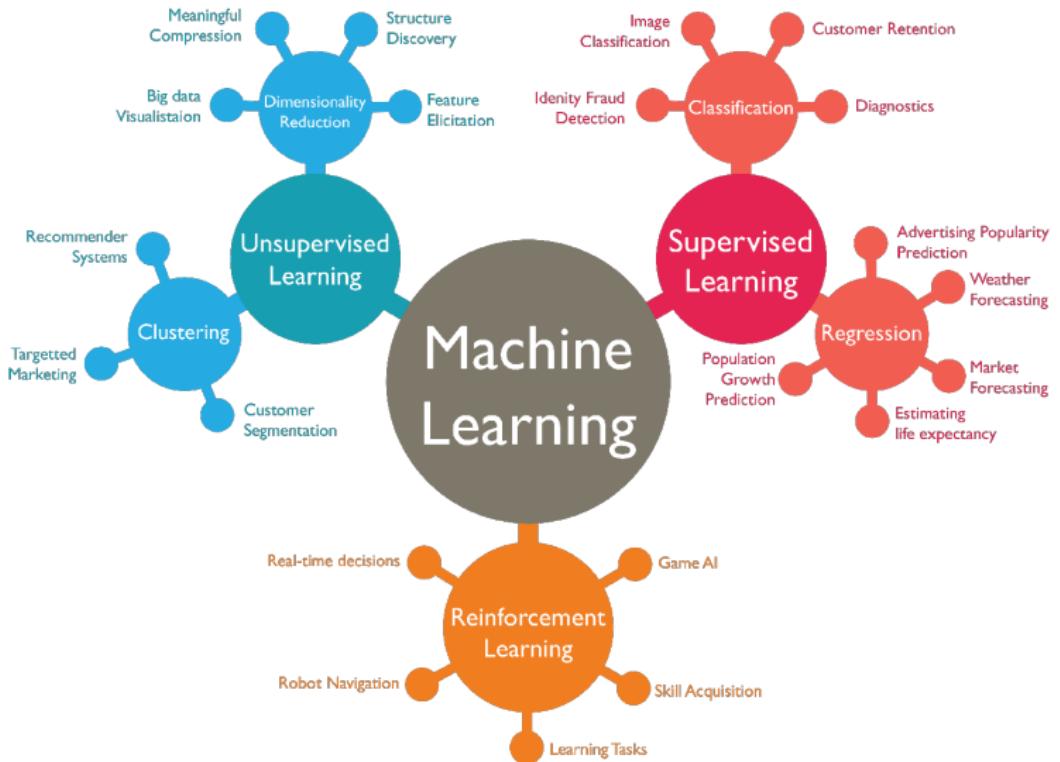
- ▶ Regression is a supervised learning technique that predicts continuous numerical values based on input features. It models relationships between dependent and independent variables by finding the best-fitting mathematical function.
(e.g., price forecasting, temperature prediction, sales modeling.)
- ▶ Classification is a supervised learning task where algorithms learn to assign input data to predefined categories or classes. The model identifies decision boundaries that separate different classes based on feature patterns.
(e.g., spam detection, sentiment analysis, disease diagnosis.)
- ▶ Clustering is an unsupervised learning technique that groups similar data points together based on their inherent characteristics. It identifies natural groupings without predefined labels by optimizing for high intra-cluster similarity and low inter-cluster similarity.
(e.g., customer segmentation, document grouping, image compression.)

Overall Methodology

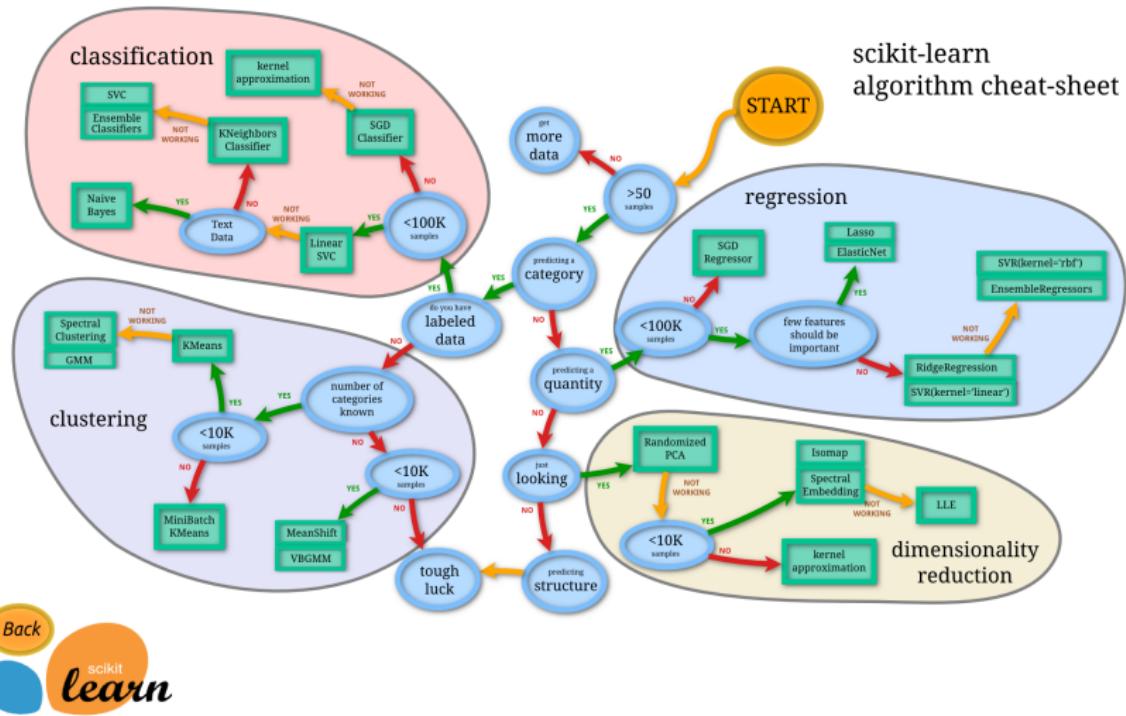
- ① Define the problem;
- ② Gather dataset;
- ③ Choose measure of success;
- ④ Decide evaluation protocol;
- ⑤ Prepare the data;
- ⑥ Develop a model;
- ⑦ Iterate models.



<https://www.cognub.com/index.php/cognitive-platform/>

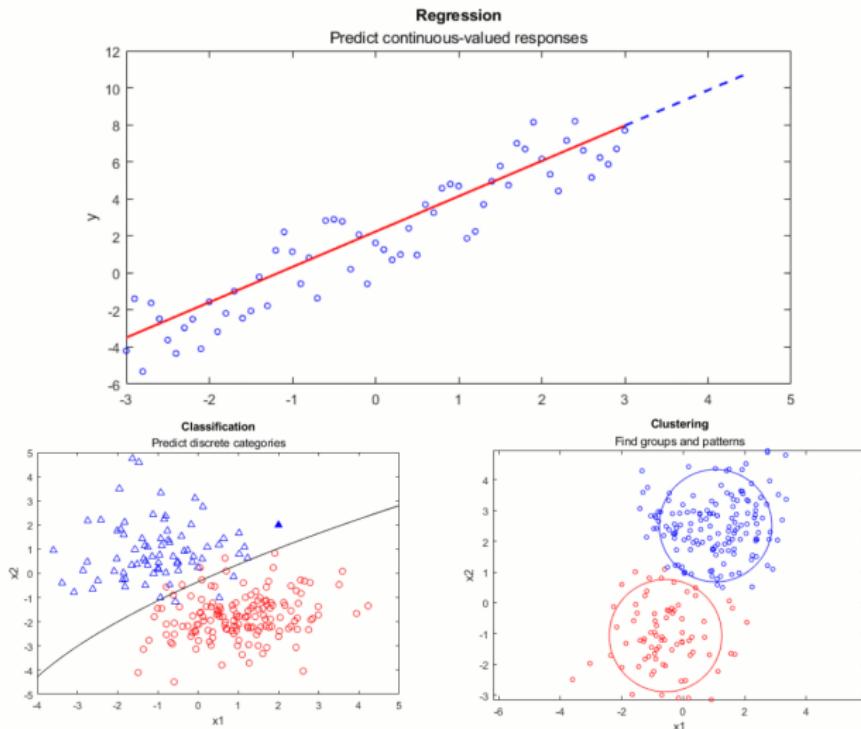


<https://vitalflux.com/great-mind-maps-for-learning-machine-learning/>



https://scikit-learn.org/stable/tutorial/machine_learning_map/index.html

Regression | Classification | Clustering



<https://github.com/MathWorks-Teaching-Resources/Machine-Learning-for-Regression>

Programming Language

A screenshot of a terminal window titled "python3". The window shows a command-line interface where the user has run the command "python3" followed by a few lines of Python code. The code prints "Hello, World!" to the console.

```
+ 13 python3
Python 3.10.6 (main, Aug 10 2022, 11:40:04) [GCC 11.3.0] on linux
Type "help", "copyright", "credits" or "license" for more information.
>>> print('Hello, World!')
Hello, World!
>>> |
```

Development Environments



▲ \$ docker compose up
▼ \$ docker compose down



Required Packages

Valid only for...



- A full list is available @ <https://pypi.org/>

Numpy



Matplotlib



Pandas



Scikit – learn



Keras



```
$ pip install virtualenv
$ virtualenv -version
$ virtualenv «virtualenv_name»
$ source «virtualenv_name»/bin/activate # ACTIVATE
$ deactivate # DEACTIVATE
```

```
> pip install virtualenv
> virtualenv -version
> virtualenv «virtualenv_name»
> «virtualenv_name»\Scripts\activate %= ACTIVATE =%
> deactivate %= DEACTIVATE =%
```





Source Control Management (SCM)

The screenshot shows a GitHub repository page for 'a-mhamdi / mlpy' (Public). The 'Code' tab is selected, displaying a list of recent commits:

Commit Message	Date
a-mhamdi fix some typos	9f2e8e2 4 minutes ago
.github/workflows Update docker-image.yml	2 months ago
Codes gradient descent code	yesterday
Docker change working dir in Dockerfile	last month
Exams reorganize mlpy folder	2 months ago
Slides-Labs fix some typos	4 minutes ago
.gitignore ignore vscode dotfiles	yesterday
LICENSE Initial commit	6 months ago
README.md change link to remote repo and add yml file	last month

Below the commits, there is a section for 'README.md' and the repository title 'Machine Learning with Python'. To the right, there is an 'About' section with repository details:

- Machine Learning with Python
- Tags: machine-learning, docker-image, sklearn, python3, keras-tensorflow
- Readme
- MIT license
- 0 stars
- 1 watching
- 0 forks

Under 'Languages', it shows 99.3% Jupyter Notebook and 0.7% Other.

<https://github.com/a-mhamdi/mlpy>





Docker Image

The screenshot shows a browser window displaying the Docker Hub interface for the repository `abmhamdi/mlpy`. The page includes a navigation bar with links for Explore, Repositories, Organizations, Help, Upgrade, and a user profile. The main content area shows the repository details for `abmhamdi / mlpy`, which is described as "Machine Learning Labs @ ISETBZ". It shows a push history from 18 minutes ago and a table of tags. A "Docker commands" section provides a command to push a new tag. Another section for automated builds is also visible.

https://hub.docker.com/r/abmhamdi/mlpy

Tag	OS	Type	Pulled	Pushed
latest		Image	--	18 minutes ago



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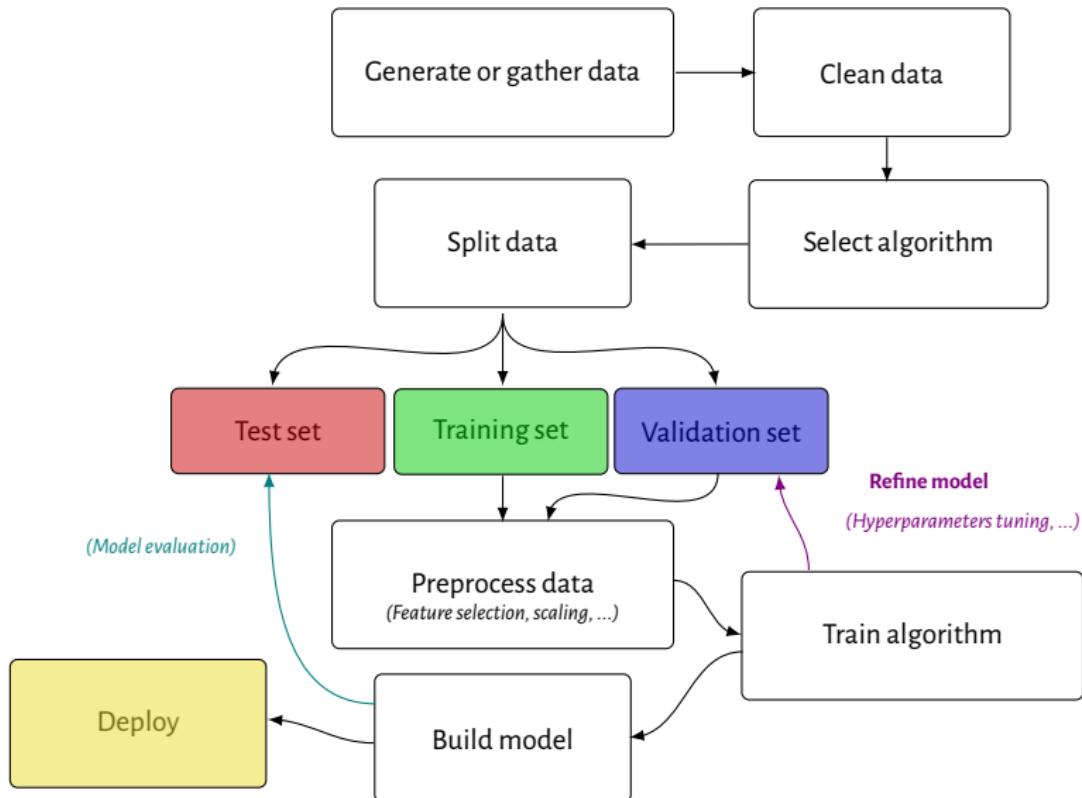
4 Artificial Neural Network

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Workflow in Machine Learning



Data Preprocessing

How?

Cleaning Identifying and correcting or removing inaccuracies and inconsistencies.

Transformation Converting data from one format or structure to another.

Normalization Scaling the data so that it fits within a specific range.

Data Preprocessing

Why?

- ▶ Raw data is often messy and may need to be cleaned and formatted before it can be used for machine learning.
(This may involve removing missing or invalid data, handling outliers, and encoding categorical variables.)
- ▶ Normalizing the data can help to scale the features so that they are on the same scale.
(This can be important for algorithms that use distance measures, as features on different scales can dominate the distance measure.)
- ▶ Preprocessing techniques such as feature selection and feature extraction can help to reduce the dimensionality of the data.
(This may improve the performance of the model and reduce the risk of overfitting.)
- ▶ Preprocessing techniques such as feature selection can help to identify the most important features in the data.
(This can make the model more interpretable and easier to understand.)

Data Preprocessing

Feature Scaling

Normalization (*MinMaxScaler*)

$$X \triangleq \frac{X - X.\min()}{X.\max() - X.\min()}$$

- ▲ No assumption on data distribution

Standardization (*StandardScaler*)

$$X \triangleq \frac{X - \mu}{\sigma}$$

- ▲ More recommended when following normal distribution

Data Preprocessing Template



The code is available at <https://github.com/a-mhamdi/mlpy> → *Codes* → *Python*

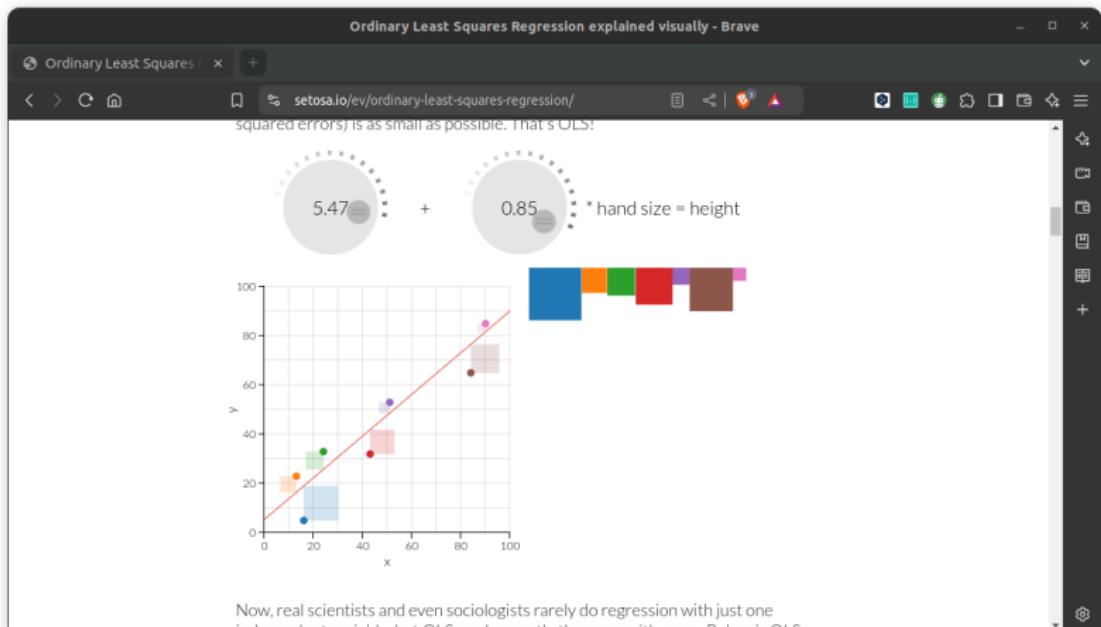
→ Marimo → *data-processing.py*



→ Jupyter → *data-processing.ipynb*



This kind of supervised learning deals with labelled data. A subset of this data is used later to predict in continuous form. Regression problems involve tasks where the outputs form generally a set of real numbers. They often follow linear formats.



Consider the example of a spring. Our main goal is to determine the stiffness k of this spring, given some experimental data. The mathematical model (*Hooke's law*):

$$F = kx \quad (1)$$

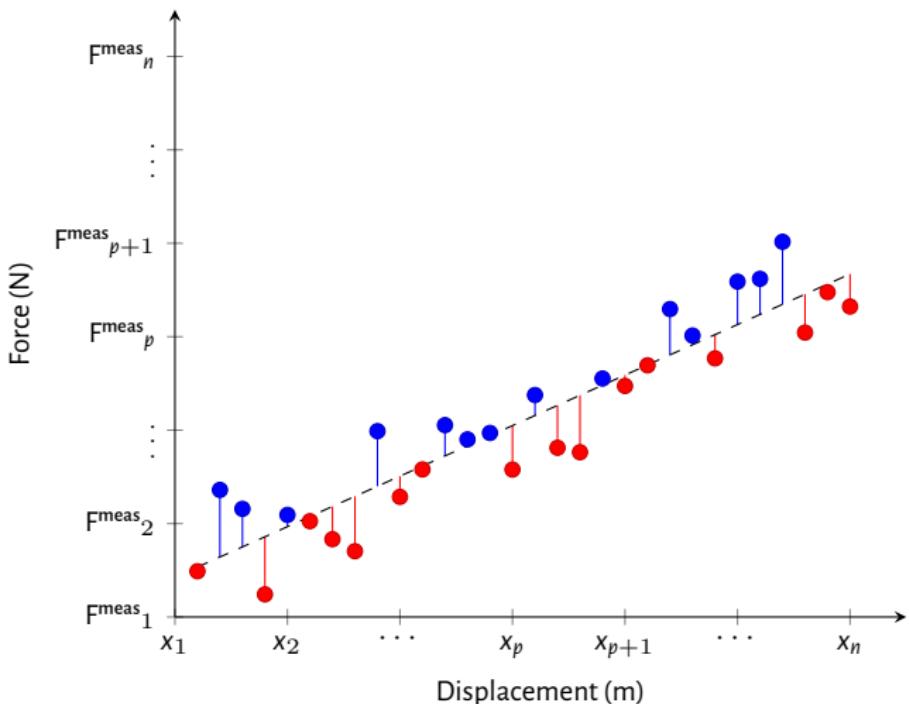
Restoring force is proportional to displacement.

Table: Measurements of couple (x_i, F^{meas}_i)

x_i	x_0	\dots	x_p	\dots	x_{n-1}
F^{meas}_i	F^{meas}_0	\dots	F^{meas}_p	\dots	F^{meas}_{n-1}

$$\begin{aligned} F^{\text{meas}}_i &= F_i + \varepsilon_i \\ &= kx_i + \varepsilon_i, \end{aligned} \quad (2)$$

where F_i denotes the unknown real value of the force applied to the spring.



In order to estimate the stiffness value k , we can consider the quadratic criterion:

$$\begin{aligned}
 \mathcal{J} &= \sum_{i=0}^{n-1} \varepsilon_i^2 \\
 &= \sum_{i=0}^{n-1} (F^{\text{meas}}_i - kx_i)^2 \\
 \frac{\partial \mathcal{J}}{\partial k} &= 0
 \end{aligned} \tag{3}$$

$$\begin{aligned}
 2 \sum_{i=0}^{n-1} (F^{\text{meas}}_i - kx_i) \sum_{i=0}^{n-1} \frac{\partial (F^{\text{meas}}_i - kx_i)}{\partial k} &= 0 \\
 \sum_{i=0}^{n-1} (F^{\text{meas}}_i - kx_i) \sum_{i=0}^{n-1} x_i &= 0
 \end{aligned}$$

$$\sum_{i=0}^{n-1} F^{\text{meas}}_i x_i = k \sum_{i=0}^{n-1} x_i^2 \iff \hat{k} = \frac{\sum_{i=0}^{n-1} F^{\text{meas}}_i x_i}{\sum_{i=0}^{n-1} x_i^2}$$

Simple Linear Regression



The code is available at <https://github.com/a-mhamdi/mlpy> → *Codes* → *Python*

→ *Marimo* → *simple-linear-regression.py*



→ *Jupyter* → *simple-linear-regression.ipynb*



Multiple Linear Regression



The code is available at <https://github.com/a-mhamdi/mlpy> → *Codes* → *Python*

→ Marimo → *multiple-linear-regression.py*



→ Jupyter → *multiple-linear-regression.ipynb*



Consider the following multivariable equation:

$$y = \theta_0 x_0 + \theta_1 x_1 + \cdots + \theta_{m-1} x_{m-1} \quad (4)$$

For a particular single measurement, eq. (4) can be updated as

$$y_k = \theta_0 x_{(0, k)} + \theta_1 x_{(1, k)} + \cdots + \theta_{m-1} x_{(m-1, k)} + \varepsilon_k \quad (5)$$

We denote hereafter by θ the vector $\begin{bmatrix} \theta_0 \\ \theta_1 \\ \vdots \\ \theta_{m-1} \end{bmatrix}$. The function y_k becomes:

$$y_k = \underbrace{\left[x_{(0, k)}, x_{(1, k)}, \dots, x_{(m-1, k)} \right]}_{x_k^T} \theta + \varepsilon_k \quad (6)$$

We assume that we have n measurements for y . Then we can transform the previous equation into

$$y = X\theta + \varepsilon, \quad (7)$$

where $y^T = [y_0, y_1, \dots, y_{n-1}]$, $X = \begin{bmatrix} x_0^T \\ x_1^T \\ \vdots \\ x_{n-1}^T \end{bmatrix}$ and $\varepsilon^T = [\varepsilon_0, \varepsilon_1, \dots, \varepsilon_{n-1}]$.

An estimate of $\hat{\theta}$ is given by

$$\hat{\theta} = (X^T X)^{-1} X^T y$$



$X^T X$ is not invertible (singular/degenerate)

▼ Redundant Features

Some features are linearly dependent, i.e., \exists some $x_p \propto$ some x_l .

▼ Too many features

Fewer observations compared to the number of features, i.e., $m > n$.

- ▲ Delete some features
- ▲ Add extra observations

Gradient Descent

The linear regression is given by:

$$y_k = \underbrace{\underbrace{[x_{(0,k)}, x_{(1,k)}, \dots, x_{(m-1,k)}]}_{x_k^T} \theta}_{h_\theta(x_k)} + \varepsilon_k \quad (8)$$

$$\theta_0 \triangleq \theta_0 + \alpha \frac{1}{n} \sum_{k=0}^{n-1} (y_k - h_\theta(x_k)) x_{(0,k)}$$

$$\theta_1 \triangleq \theta_1 + \alpha \frac{1}{n} \sum_{k=0}^{n-1} (y_k - h_\theta(x_k)) x_{(1,k)}$$

⋮

$$\theta_{m-1} \triangleq \theta_{m-1} + \alpha \frac{1}{n} \sum_{k=0}^{n-1} (y_k - h_\theta(x_k)) x_{(m-1,k)}$$

The hyperparameter α is the learning rate.

Polynomial Regression



The code is available at <https://github.com/a-mhamdi/mlpy> → *Codes* → *Python*

→ *Marimo* → *polynomial-regression.py*



→ *Jupyter* → *polynomial-regression.ipynb*



Task #2

The yield y of a chemical process is a random variable whose value is considered to be a linear function of the temperature x . The following data of corresponding values of x and y is found:

Temperature in °C (x)	0	25	50	75	100
Yield in grams (y)	14	38	54	76	95

The linear regression model $y = \theta_0 + \theta_1 x$ is used. Determine the values of θ_0 and θ_1 .

$$y = \begin{bmatrix} 14 \\ 38 \\ 54 \\ 76 \\ 95 \end{bmatrix} \quad x = \begin{bmatrix} 1 & 0 \\ 1 & 25 \\ 1 & 50 \\ 1 & 75 \\ 1 & 100 \end{bmatrix} \quad x^T x = \begin{bmatrix} 5 & 250 \\ 250 & 18750 \end{bmatrix}$$

$$(x^T x)^{-1} = \frac{1}{31250} \begin{bmatrix} 18750 & -250 \\ -250 & 5 \end{bmatrix} \quad x^T y = \begin{bmatrix} 277 \\ 18850 \end{bmatrix}$$

$$\therefore \begin{bmatrix} \hat{\theta}_0 \\ \hat{\theta}_1 \end{bmatrix} = \begin{bmatrix} 15.4 \\ 0.8 \end{bmatrix} \quad \text{with: } \begin{cases} \text{mae} = \langle |y - \hat{y}| \rangle \approx 1.28 \\ \text{mape} = \langle \left| \frac{\hat{y} - y}{y} \right| \rangle \approx 0.04 \\ \text{mse} = \langle (y - \hat{y})^2 \rangle = 2.24 \end{cases}$$

Code implementation



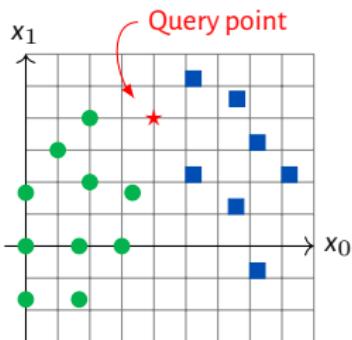
```

1 import numpy as np
2 import matplotlib.pyplot as plt
3
4 X = np.array([[1, 0], [1, 25], [1, 50], [1, 75], [1, 100]])
5 y = np.array([14, 38, 54, 76, 95])
6
7 # NORMAL EQUATION
8 theta_ne = np.linalg.inv(X.T @ X) @ X.T @ y
9
10 # GRADIENT DESCENT
11 theta_gd = np.zeros(shape=(2, 1001))
12 theta_gd[:, 0] = np.array([10, .5])
13 cost = []
14 for k in range(1000):
15     eps = y - (X @ theta_gd[:, k])
16     cost.append(1/10*(eps @ eps))
17     theta_gd[:, k+1] = theta_gd[:, k] + .003/5*(eps @ X)
18
19 plt.plot(theta_gd[0, :], label=r'$\hat{\theta}_0$')
20 plt.plot(theta_gd[1, :], label=r'$\hat{\theta}_1$')
21 plt.legend(); plt.grid(); plt.show()
22
23 plt.plot(cost); plt.grid(); plt.show()

```

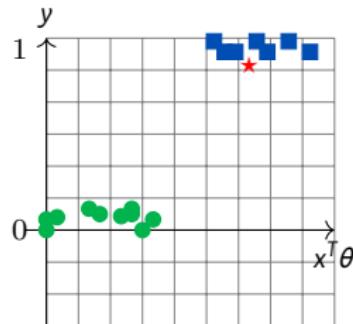
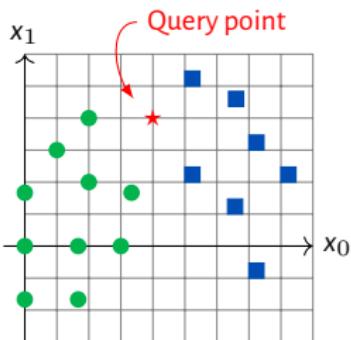
Introduction

Classification is a type of supervised machine learning algorithm. A model is trained on a set of *labeled data*, where each data point is associated with a known class or category. The goal of the algorithm is to learn the relationship between the *input features x* and the corresponding *output classes y*, so that it can accurately predict the class of **new, unseen query points**.



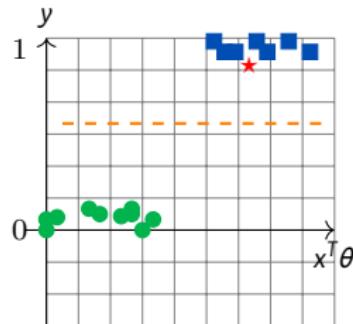
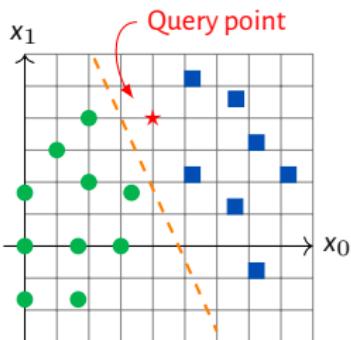
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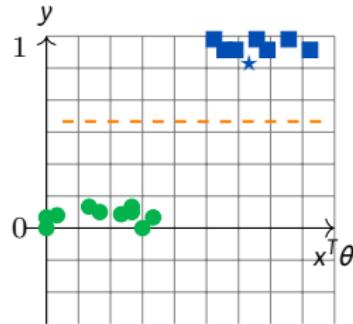
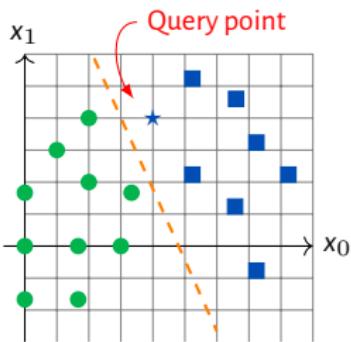
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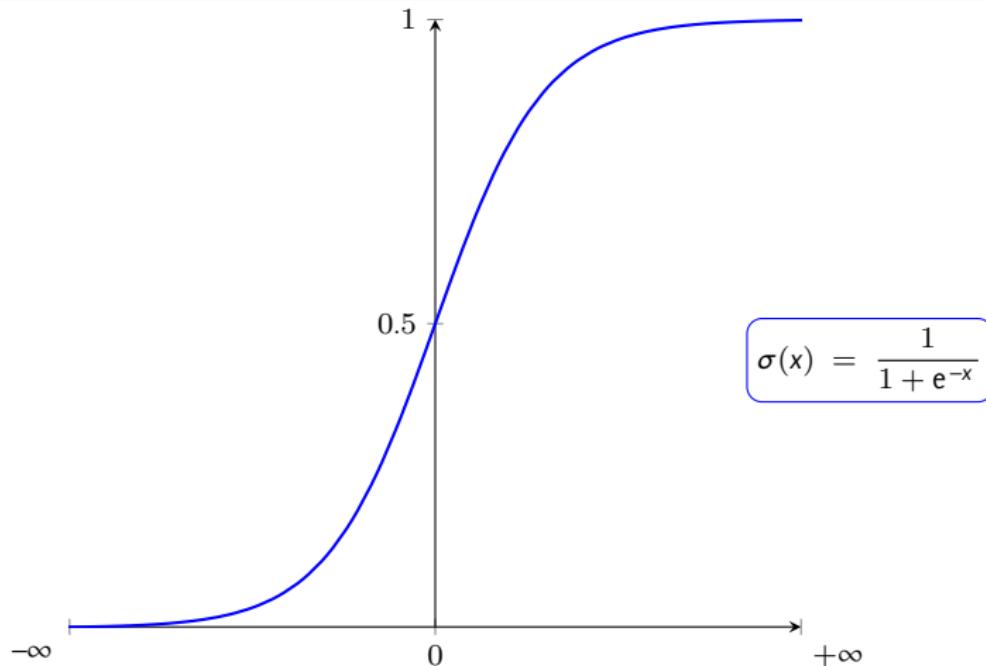


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Logistic or S-shaped function σ



- ▲ σ squashes range of distance from $]-\infty, +\infty[$ to $[0, 1]$
- ▲ σ is differentiable and easy to compute: $\dot{\sigma} = \sigma \times (1 - \sigma)$

Decision boundary

$$y = \sigma(\theta_0 x_0 + \theta_1 x_1 + \cdots + \theta_{m-1} x_{m-1})$$

$$y = \frac{1}{1 + e^{-x^T \theta}}$$

Hypothesis

Considering $h_\theta(x) = \frac{1}{1 + e^{-x^T \theta}}$ yields $h_\theta(x_k) = \frac{1}{1 + e^{-x_k^T \theta}}$



⋮

$$\theta_{m-1} \triangleq \theta_{m-1} + \alpha \frac{1}{n} \sum_{k=0}^{n-1} (y_k - h_\theta(x_k)) x_{(m-1, k)}$$

Logistic Regression



The code is available at <https://github.com/a-mhamdi/mlpy> → *Codes* → *Python*

→ Marimo → *logistic-regression.py*



→ Jupyter → *logistic-regression.ipynb*



Evaluation metrics

Accuracy

Precision

Recall

f1-score

Accuracy denotes the ratio of how many we got right over all cases:

$$\text{Accuracy} = \frac{\text{TP} + \text{TN}}{\text{TP} + \text{FP} + \text{TN} + \text{FN}}$$

Precision designates how many positives do we get right over all positive predictions:

$$\text{Precision} = \frac{\text{TP}}{\text{TP} + \text{FP}}$$

Recall is the ratio of how many positives we got right over all actual positive cases:

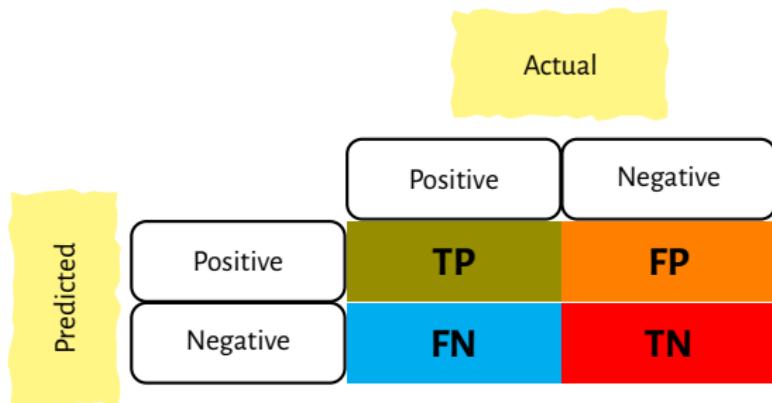
$$\text{Recall} = \frac{\text{TP}}{\text{TP} + \text{FN}}$$

f1-score denotes the Harmonic Mean of *Precision & Recall*:

$$\text{f1-score} = \frac{2}{\frac{1}{\text{Precision}} + \frac{1}{\text{Recall}}}$$

Evaluation metrics

Confusion Matrix



$$\text{Accuracy} = \frac{\text{TP} + \text{TN}}{\text{TP} + \text{FP} + \text{TN} + \text{FN}}$$

$$\text{Precision} = \frac{\text{TP}}{\text{TP} + \text{FP}}$$

$$\text{Recall} = \frac{\text{TP}}{\text{TP} + \text{FN}}$$

$$f1-score = \frac{2}{\frac{1}{\text{Precision}} + \frac{1}{\text{Recall}}}$$

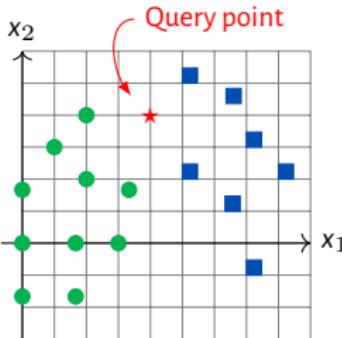
183	141
13	663

$$\begin{aligned}\text{Accuracy} &= 0.846 \\ \text{Precision} &= 0.565 \\ \text{Recall} &= 0.934 \\ f1-score &= 0.704\end{aligned}$$

320	20
43	538

$$\begin{aligned}\text{Accuracy} &= 0.932 \\ \text{Precision} &= 0.941 \\ \text{Recall} &= 0.882 \\ f1-score &= 0.910\end{aligned}$$

k-Nearest Neighbors (1/5)



► Evelyn Fix and Joseph Hodges, 1951

► Thomas Cover, 1966

Algorithm Summary Construction

1: **procedure** How DOES *k*-NN work? (Finding Nearest Neighbors)

Input: A query point;

Output: Assign a class label to that point.

2: Define how many neighbors will be checked to classify the specific query point;

3: Compute the distance $d(x; y)$ of the query point to other data points;

4: Count the number of the data points in each category;

5: Assign the query point to the class with most frequent neighbors.

6: **end procedure**

k-Nearest Neighbors (2/5)

Minkowski distance

$$d(x; y) = \left(\sum_{i=0}^{n-1} |y_i - x_i|^p \right)^{1/p}$$

Manhattan distance (p=1)

$$d(x; y) = \sum_{i=0}^{n-1} |y_i - x_i|$$

Euclidean distance (p=2)

$$d(x; y) = \sqrt{\sum_{i=0}^{n-1} (y_i - x_i)^2}$$

Task #3

Let be the following coordinate points:

A(1, 6); B(2, 6); C(3, 1); D(4, 2); E(6, 0); F(7, 5); G(7, 3); H(10, 3); I(-4, -1)

Using the Euclidean distance, what are the two closest neighbors of point P(5, 5)?

$$d(A; P) = \sqrt{17} \approx 4.12 \quad d(B; P) = \sqrt{10} \approx 3.16 \quad d(C; P) = \sqrt{20} \approx 4.47$$

$$d(D; P) = \sqrt{10} \approx 3.16 \quad d(E; P) = \sqrt{26} \approx 5.1 \quad d(F; P) = \sqrt{4} = 2$$

$$d(G; P) = \sqrt{8} \approx 2.83 \quad d(H; P) = \sqrt{29} \approx 5.38 \quad d(I; P) = \sqrt{117} \approx 10.82$$

k-Nearest Neighbors (3/5)

```
from math import sqrt
def dds(a, b): # `a` and `b` are coordinates of some point
    d_squared = (a-5)**2+(b-5)**2
    return (d_squared, sqrt(d_squared))

dds(1, 6) # Point `A`
dds(2, 6) # Point `B`
```

k-Nearest Neighbors (4/5)

Task #4^a

^aFrom Prof. Winston's book

We try to predict the color of a fruit according to its width (w) and height (h). The following training data is available:

Fruit	F_1	F_2	F_3	F_4	F_5	F_6	F_7	F_8
w	2	5	2	6	1	4	2	6
h	6	6	5	5	2	2	1	1
Color	Red	Yellow	Orange	Purple	Red	Blue	Violet	Green

The goal here is to study the influence of neighbors on the color property of a fruit. Let U be the new fruit of width $w = 1$ and height $h = 4$

- ① What is its color if we consider 1 neighbor?
- ② What is its color if we consider 3 neighbors?
- ③ Rather than majority voting, we would like to consider the vote of neighbors weighted by the distance. Each neighbor votes according to a weight inversely proportional to the square of its distance: $\frac{1}{d^2}$. We take 3 neighbors, what is the color of U ? Compare your results to those in question 2.

k-Nearest Neighbors (5/5)

$$d(U; F_1) = \sqrt{5} \approx 2.24 \quad d(U; F_2) = \sqrt{20} \approx 4.47 \quad d(U; F_3) = \sqrt{2} \approx 1.41$$

$$d(U; F_4) = \sqrt{26} \approx 5.1 \quad d(U; F_5) = \sqrt{4} = 2 \quad d(U; F_6) = \sqrt{13} \approx 3.6$$

$$d(U; F_7) = \sqrt{10} \approx 3.16 \quad d(U; F_8) = \sqrt{34} \approx 5.83$$

- ① Color of U is Orange because $d(U; F_3)$ is the smallest.
- ② Color of U is Red: F_1 and F_5 (+2 to Red class), F_3 (+1 to Orange class)
- ③ Color of U is Orange

$$S(\text{Red}) = \frac{1}{d^2(U; F_1)} + \frac{1}{d^2(U; F_5)} = 0.45$$

$$S(\text{Orange}) = \frac{1}{d^2(U; F_3)} = 0.5$$

```
from math import sqrt
def dds(w, h): # `w` and `h` are width and height of some fruit
    d_squared = (w-1)**2+(h-4)**2
    return (d_squared, sqrt(d_squared))

dds(2, 6) # Fruit `F_1`
dds(5, 6) # Fruit `F_2`
```

k-NN



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→ *Marimo* → *k-nearest-neighbors.py*



→ *Jupyter* → *k-nearest-neighbors.ipynb*



Rule of Thumb to Choose k

k is even if the number of classes is odd

k is odd if the number of classes is even

k is an important hyperparameter that can affect the performance of the model.

- ➊ Larger values of k will result in a smoother decision boundary, which can lead to a more generalized model.
- ➋ Smaller values of k will result in a more complex decision boundary, which can lead to a model that is more prone to overfitting.
- ➌ The optimal value of k may depend on the specific dataset and the characteristics of the data.

Outroduction

Method	Pros	Cons
<i>Logistic Regression</i>	▲ Probabilistic	▼ Almost linearly separable data
K-NN	▲ Simple	▼ Number of neighbors k
	▲ Fast	▼ Detecting outliers ²
	▲ Efficient	

²Points that differ significantly from the rest of the data points.

[Next...](#)

- 1 An overview
- 2 Supervised Learning
- 3 Unsupervised Learning**
- 4 Artificial Neural Network
- 5 Large Language Model
- 6 Complementary Lab. Project
- 7 ML Landscape through Quizzes

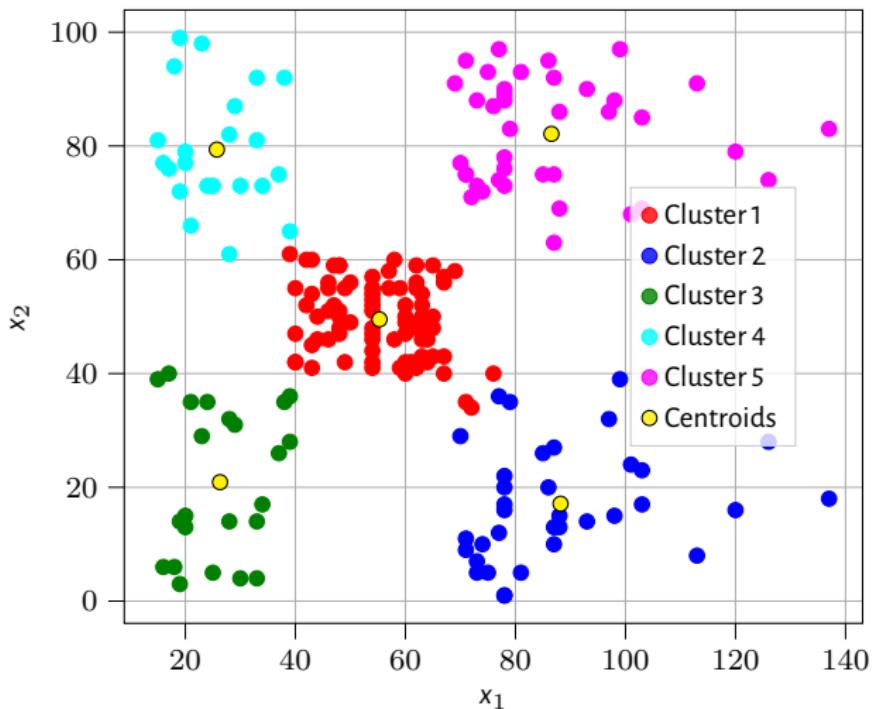
K-Means Clustering (1/3)

The algorithm **K-Means** allows to display regularities or patterns in unlabeled data.

- ▶ The term 'means' refers to averaging the data when computing each centroid;
- ▶ A centroid is the arithmetic mean of all the data points belonging to a particular cluster.

This technique identifies a certain number of centroids within a data set. The algorithm then allocates every data point to the nearest cluster as it attempts to keep the clusters as small as possible. At the same time, K-Means attempts to keep the other clusters as different as possible.

K-Means Clustering (2/3)



K-Means Clustering (3/3)

Algorithm Summary Construction

- 1: **procedure** How DOES K-MEANS WORK? (Discovering similarities)
Input: Unlabeled data sets;
Output: Grouping into clusters.
 - 2: Define how many clusters will be used to group the data sets;
 - 3: Initialize all the coordinates of the k cluster centers
 - 4: **repeat**
 - 5: Assign each point to its nearest cluster;
 - 6: Update the centroids coordinates;
 - 7: **until** No changes to the centers of the clusters
 - 8: Assign new cases to one of the clusters
 - 9: **end procedure**
-

Task #5^a

"From 'Machine Learning' course on 'Coursera'

Of the following examples, which would you address using an unsupervised learning algorithms? (*Check all that apply.*)

- ① Given email labeled as spam/not spam, learn a spam filter
- ② Given a set of news articles found on the web, group them into set of articles about the same story
- ③ Given a database of customer data, automatically discover market segments and group customers into different market segments
- ④ Given a dataset of patients diagnosed as either having diabetes or not, learn to classify new patients as having diabetes or not.

Task #5^a

"From 'Machine Learning' course on 'Coursera'

Of the following examples, which would you address using an unsupervised learning algorithms? (*Check all that apply.*)

- ① Given email labeled as spam/not spam, learn a spam filter
- ② Given a set of news articles found on the web, group them into set of articles about the same story
- ③ Given a database of customer data, automatically discover market segments and group customers into different market segments
- ④ Given a dataset of patients diagnosed as either having diabetes or not, learn to classify new patients as having diabetes or not.

Task #6^a

^aCredit: Shokoufeh Mirzaei, PhD

Use K-Means algorithm to cluster the following eight points into three clusters:

A(2, 10); B(2, 5); C(8, 4); D(5, 8); E(7, 5); F(6, 4); G(1, 2) and H(4, 9).

- ▶ Initial cluster centers are: $\alpha(2, 10)$; $\beta(5, 8)$ and $\gamma(1, 2)$
- ▶ The distance between two points: $M(x_m, y_m)$ and $N(x_n, y_n)$ is defined as

$$d(M; N) = |x_m - x_n| + |y_m - y_n|$$

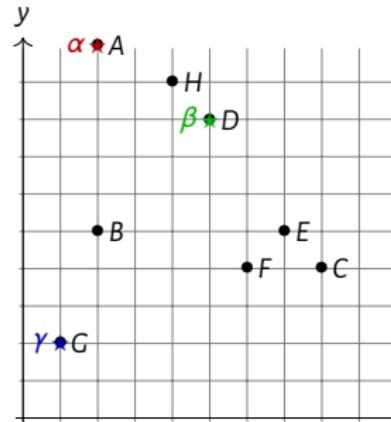
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Task #6^a^aCredit: Shokoufeh Mirzaei, PhD

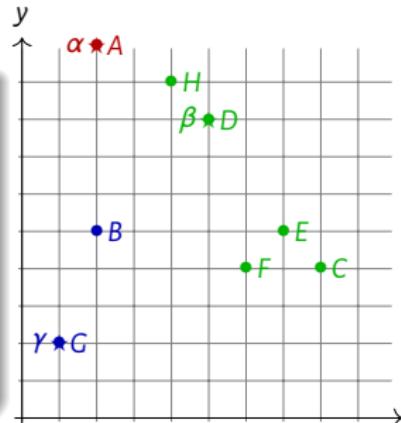
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$$d(M; N) = |x_m - x_n| + |y_m - y_n|$$

Point	$\alpha(2, 10)$	$\beta(5, 8)$	$\gamma(1, 2)$	#
A(2, 10)	0	5	9	1
B(2, 5)	5	6	4	3
C(8, 4)	12	7	9	2
D(5, 8)	5	0	10	2
E(7, 5)	10	5	9	2
F(6, 4)	10	5	7	2
G(1, 2)	9	10	0	3
H(4, 9)	3	2	10	2



Task #6^a^aCredit: Shokoufeh Mirzaei, PhD

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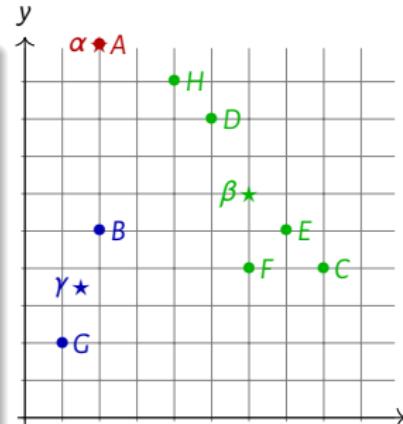
$$d(M; N) = |x_m - x_n| + |y_m - y_n|$$

Point	$\alpha(2, 10)$	$\beta(5, 8)$	$\gamma(1, 2)$	#
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D(5, 8)	5	0	10	2
E(7, 5)	10	5	9	2
F(6, 4)	10	5	7	2
G(1, 2)	9	10	0	3
H(4, 9)	3	2	10	2

$\alpha(2, 10)$

$\beta(6, 6)$

$\gamma(1.5, 3.5)$



Task #6^a^aCredit: Shokoufeh Mirzaei, PhD

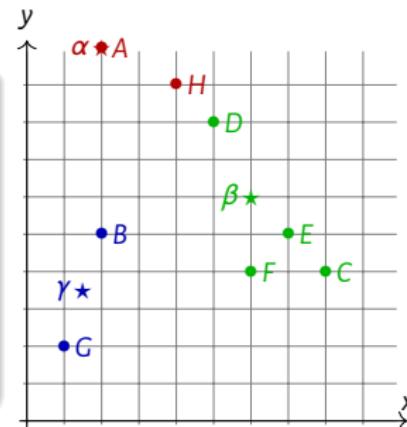
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G(1, 2)	9	9	2	3
H(4, 9)	3	5	8	1



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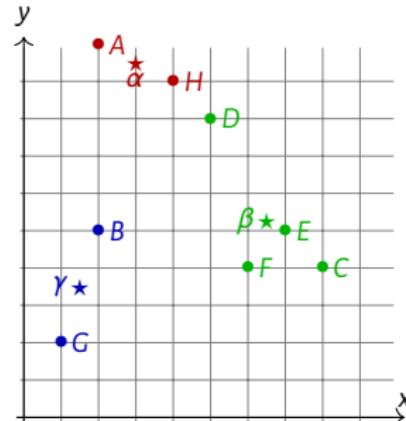
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Point	$\alpha(2, 10)$	$\beta(6, 6)$	$\gamma(1.5, 3.5)$	#
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F(6, 4)	10	2	5	2
G(1, 2)	9	9	2	3
H(4, 9)	3	5	8	1

 $\alpha(3, 9.5)$ $\beta(6.5, 5.25)$ $\gamma(1.5, 3.5)$ 

Task #6^a^aCredit: Shokoufeh Mirzaei, PhD

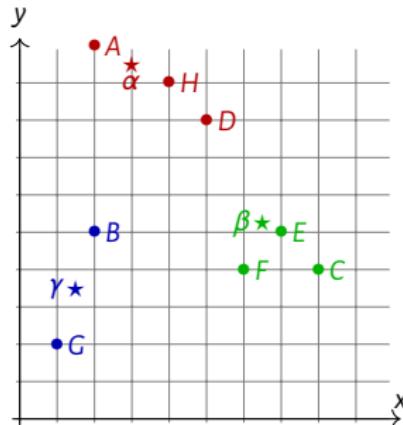
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Point	$\alpha(3, 9.5)$	$\beta(6.5, 5.25)$	$\gamma(1.5, 3.5)$	#
A(2, 10)	1.5	9.25	7	1
B(2, 5)	5.5	4.75	2	3
C(8, 4)	10.5	2.75	7	2
D(5, 8)	3.5	4.25	8	1
E(7, 5)	8.5	0.75	7	2
F(6, 4)	8.5	1.75	5	2
G(1, 2)	9.5	8.75	2	3
H(4, 9)	1.5	6.25	8	1



Task #6^a^aCredit: Shokoufeh Mirzaei, PhD

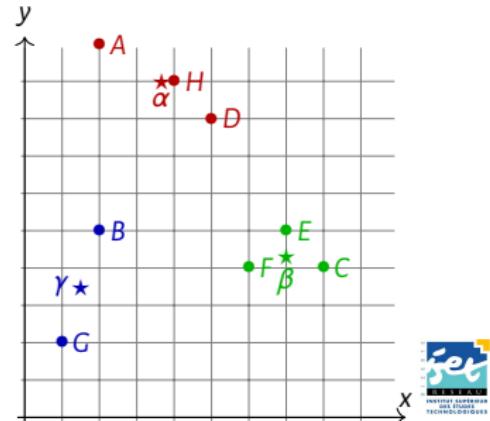
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H(4, 9)	1.5	6.25	8	1

 $\alpha(3.67, 9)$ $\beta(7, 4.3)$ $\gamma(1.5, 3.5)$ 

Task #6^a^aCredit: Shokoufeh Mirzaei, PhD

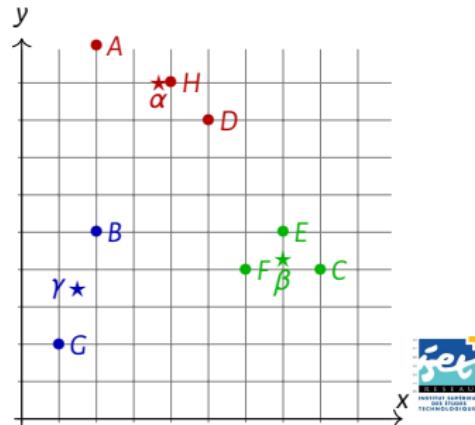
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$$d(M; N) = |x_m - x_n| + |y_m - y_n|$$

Point	$\alpha(3.67, 9)$	$\beta(7, 4.3)$	$\gamma(1.5, 3.5)$	#
A(2, 10)	2.67	10.7	7	1
B(2, 5)	5.67	5.7	2	3
C(8, 4)	9.33	1.3	7	2
D(5, 8)	2.33	5.7	8	1
E(7, 5)	7.33	0.7	7	2
F(6, 4)	7.33	1.3	5	2
G(1, 2)	9.67	8.3	2	3
H(4, 9)	0.33	7.7	8	1



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Use K-Means algorithm to cluster the following eight points into three clusters:

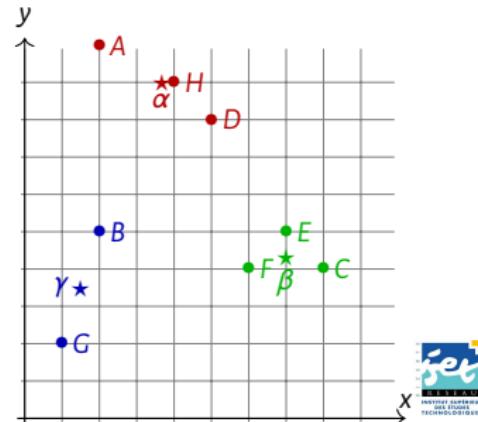
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Point	$\alpha(3.67, 9)$	$\beta(7, 4.3)$	$\gamma(1.5, 3.5)$	#
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$\alpha(3.67, 9)$ $\beta(7, 4.3)$ $\gamma(1.5, 3.5)$



K-Means



The code is available at <https://github.com/a-mhamdi/mlpy> → *Codes* → *Python*

→ *Marimo* → *K-means-clustering.py*



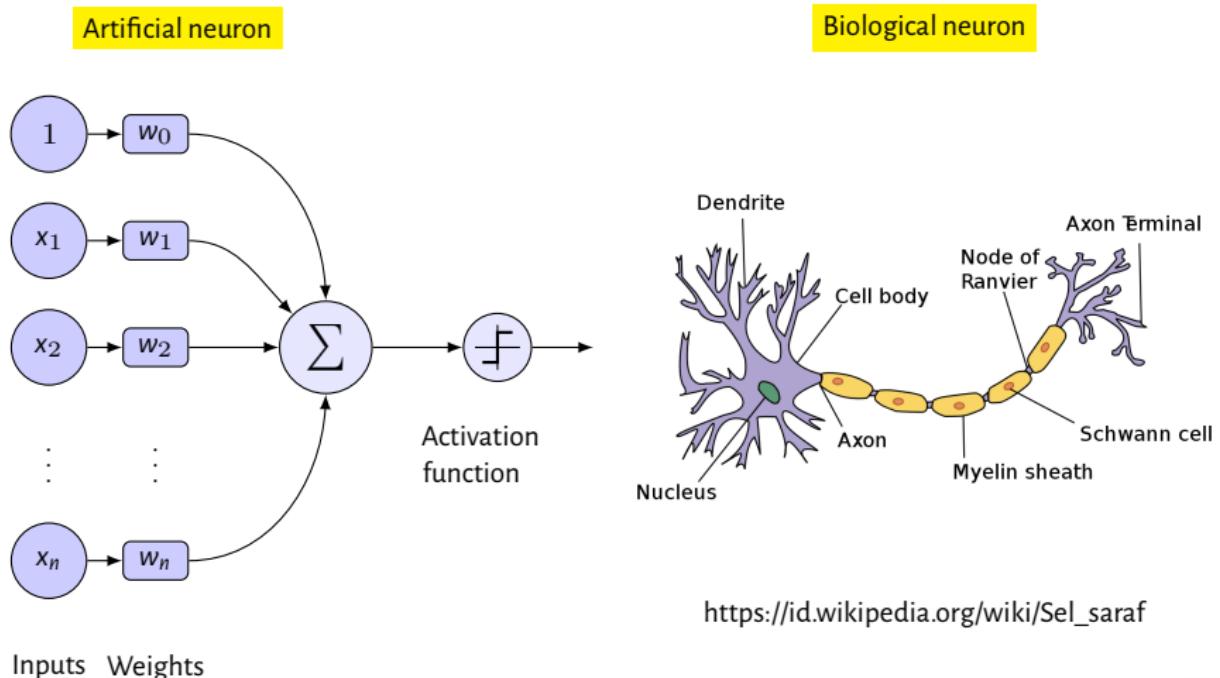
→ *Jupyter* → *K-means-clustering.ipynb*



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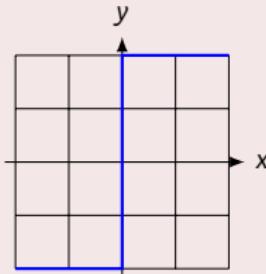
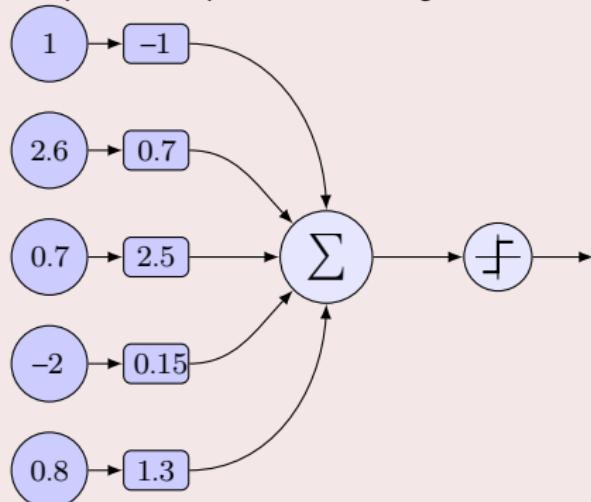
Fundamental unit of a neural network (1/2)



Fundamental unit of a neural network (2/2)

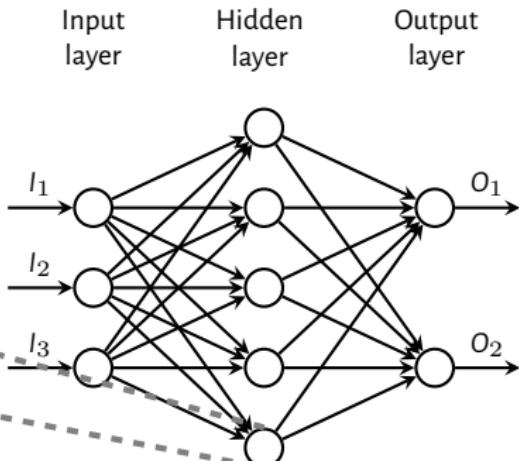
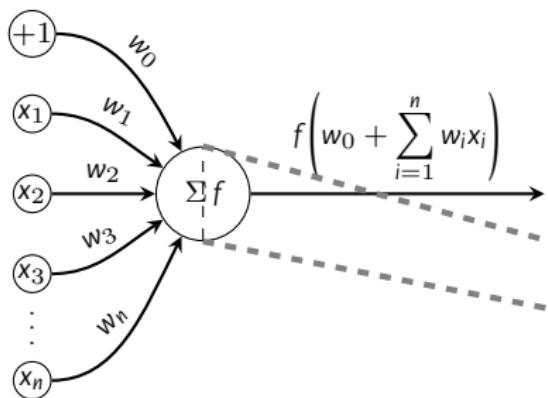
Task #7

Compute the output of the following neuron.



$$y = \text{sign}(1 \times -1 + 2.6 \times 0.7 + 0.7 \times 2.5 - 2 \times 0.15 + 0.8 \times 1.3) = 1$$

Multilayer Perceptron (MLP) (1/4)

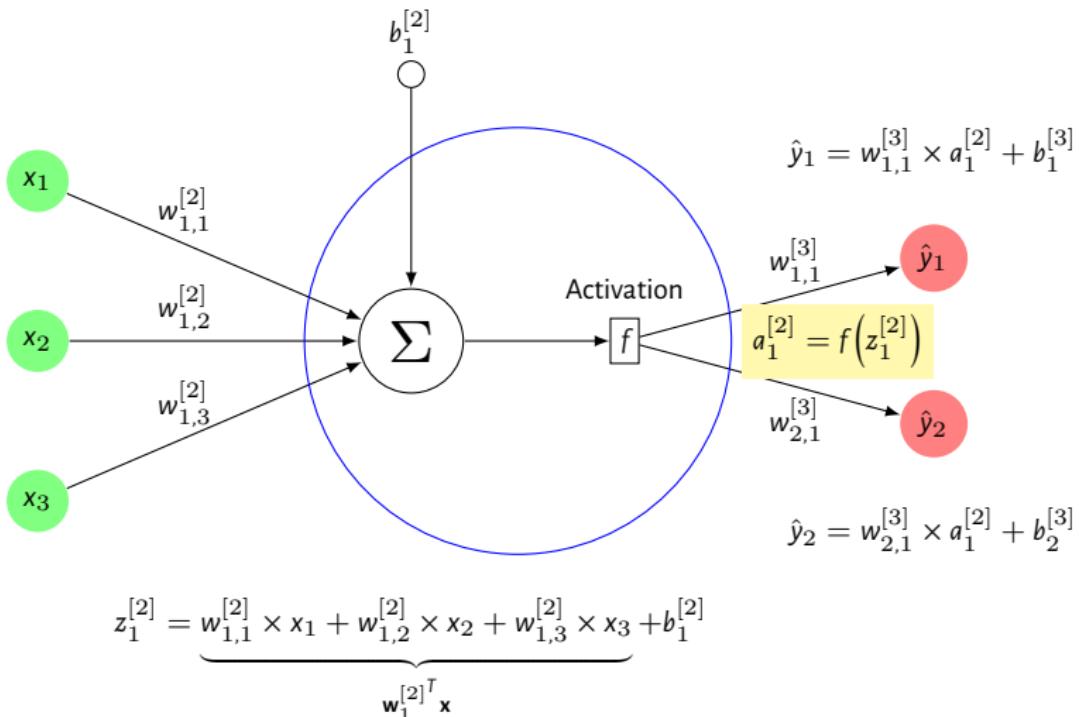


Task #8

For the above structure, determine how many parameters are to be adjusted.

$$\# \text{ params} = 5 \times 3 + 5 + 2 \times 5 + 2 = 32$$

Multilayer Perceptron (MLP) (2/4)



Multilayer Perceptron (MLP) (3/4)

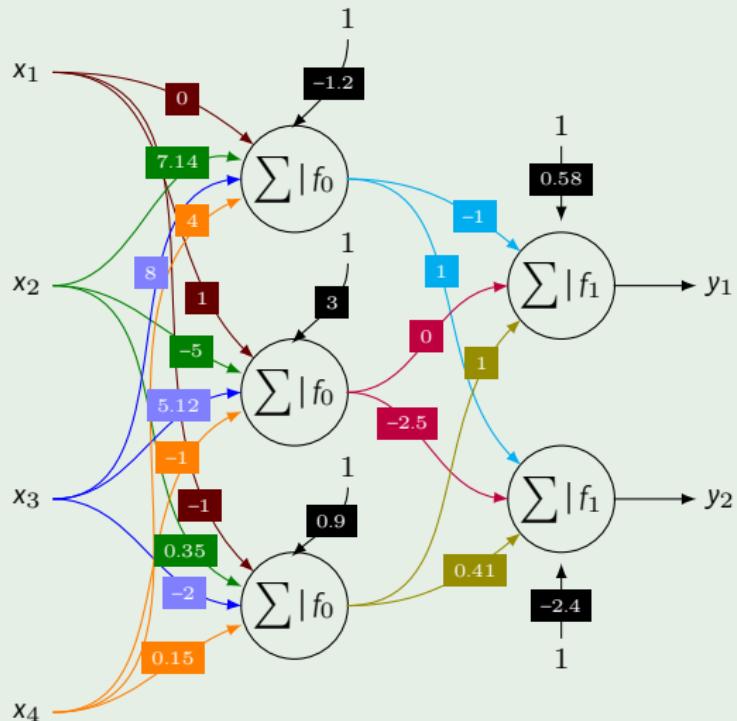
Task #9

Given the following weight matrices and biases vectors. Draw the corresponding neural network architecture. (*Place the values of the synaptic weights and biases on the arrows.*)

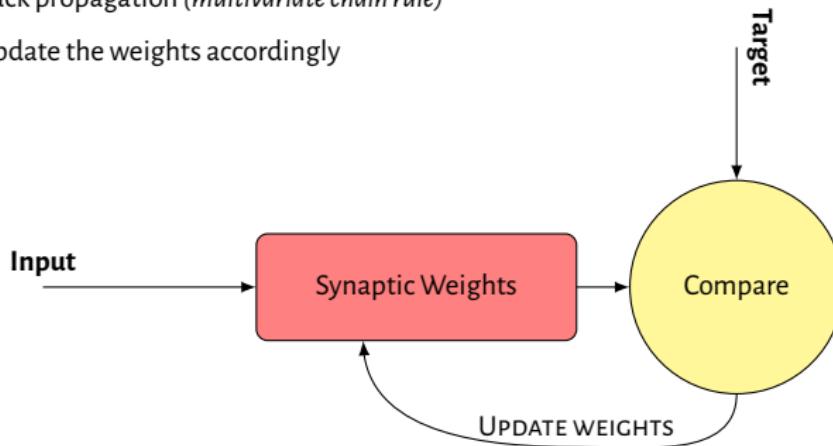
$$\mathbf{W}^{[0]} = \begin{bmatrix} 0 & 7.14 & 8 & 4 \\ 1 & -5 & 5.12 & -1 \\ -1 & 0.35 & -2 & 0.15 \end{bmatrix} \quad \text{and} \quad \mathbf{b}^{[0]} = \begin{bmatrix} -1.2 \\ 3 \\ 0.9 \end{bmatrix}$$

$$\mathbf{W}^{[1]} = \begin{bmatrix} -1 & 0 & 1 \\ 1 & -2.5 & 0.41 \end{bmatrix} \quad \text{and} \quad \mathbf{b}^{[1]} = \begin{bmatrix} 0.58 \\ -2.4 \end{bmatrix}$$

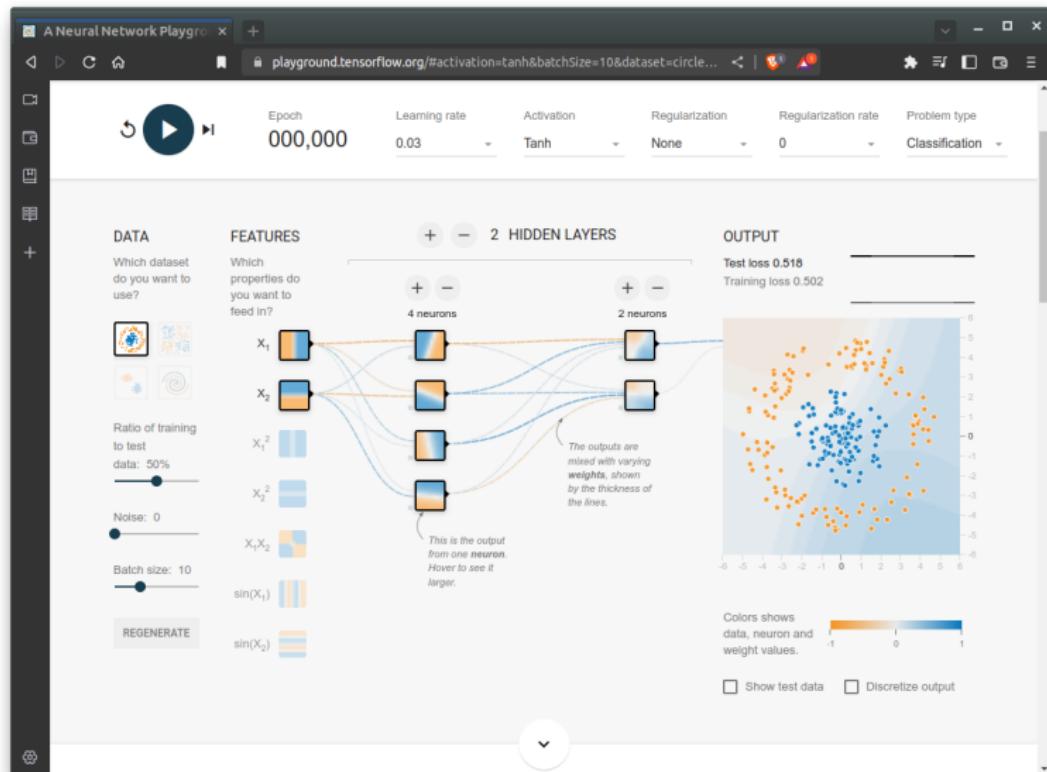
Multilayer Perceptron (MLP) (4/4)



- ✓ Design a structure
- ✓ Specify a loss function to minimize
- ✓ Optimize using gradient descent
 - ① Feedforward propagation (*matrix multiplication and point-wise activation*)
 - ② Back propagation (*multivariate chain rule*)
 - ③ Update the weights accordingly



Tinker with a neural network



<https://playground.tensorflow.org/>

ANN



The code is available at <https://github.com/a-mhamdi/mlpy> → *Codes* → *Python*

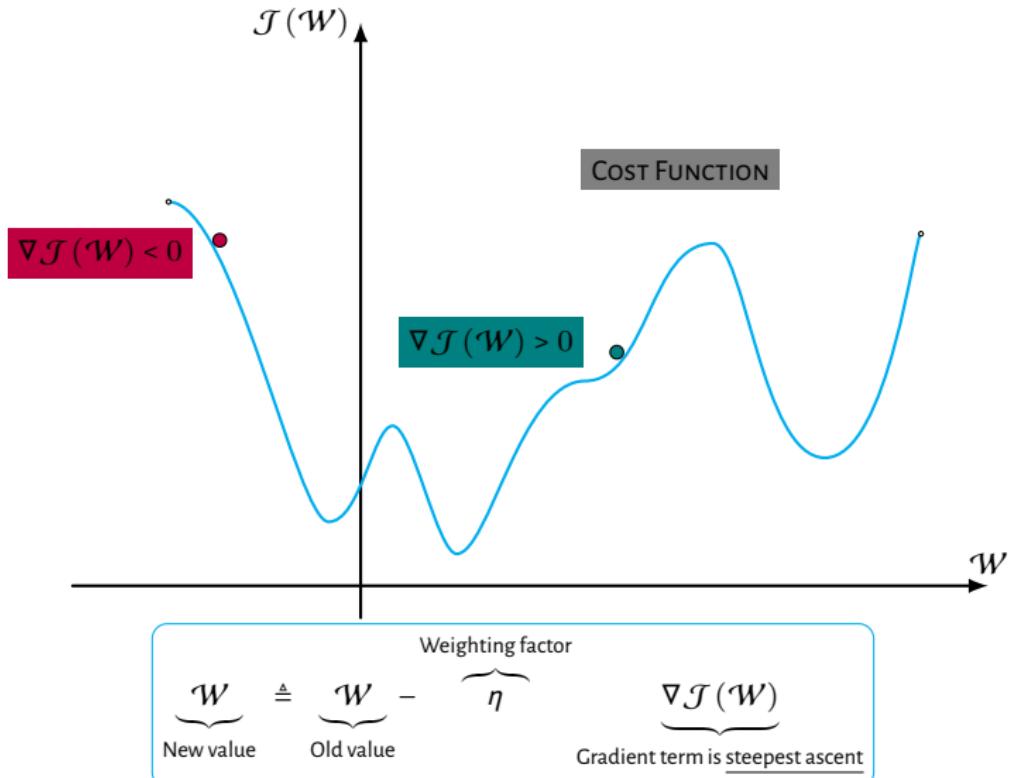
→ Marimo → *artificial-neural-network.py*



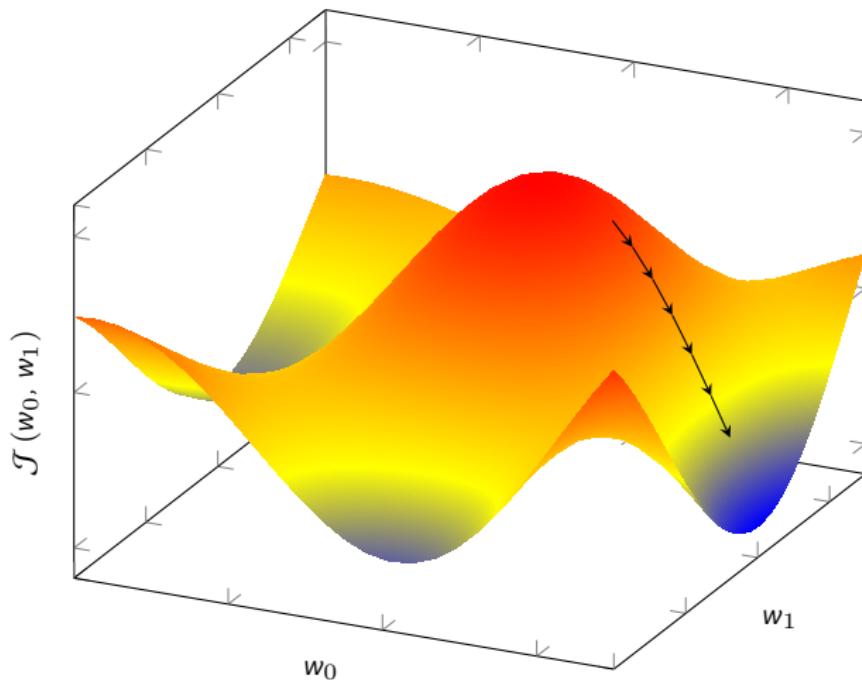
→ Jupyter → *artificial-neural-network.ipynb*



Gradient Descent (1/2)



Gradient Descent (2/2)



- ① Start with some random values of w_0 and w_1
- ② Keep changing w_0 and w_1 to reduce $\mathcal{J}(w_0, w_1)$ until we hopefully end up at minimum

List of available optimizers

Here is a list of some common optimizers for artificial neural networks:

$$\Delta \hat{W} \triangleq \mathcal{F} \left(\nabla \underbrace{\mathcal{J}(\hat{W})}_{\text{Loss Function}} \right) \equiv \hat{W} \triangleq \hat{W} + \mathcal{F} \left(\nabla \mathcal{J}(\hat{W}) \right) \quad \nabla \mathcal{J}(\hat{W}) = \begin{bmatrix} \frac{\partial \mathcal{J}}{\partial \hat{w}_0} \\ \vdots \\ \frac{\partial \mathcal{J}}{\partial \hat{w}_n} \end{bmatrix}$$

SGD
SGD+MOMENTUM
ADAGRAD

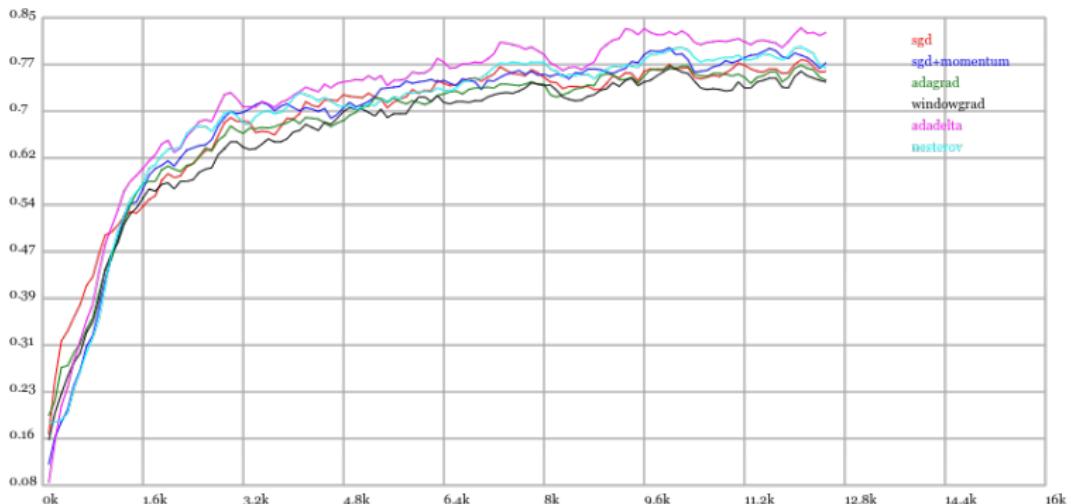
WINDOWGRAD
ADADELTA
NESTEROV

Effect of optimizer on loss values



<https://cs.stanford.edu/people/karpathy/convnetjs/demo/trainers.html>

Effect of optimizer on testing accuracy values



<https://cs.stanford.edu/people/karpathy/convnetjs/demo/trainers.html>

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ChatGPT Prompt Engineering for Developers (1/3)

Prompting Principles



WRITE CLEAR AND SPECIFIC INSTRUCTIONS

- Tactic ① Use delimiters to indicate distinct parts of the input (*e.g.*, ", ", < >);
- Tactic ② Ask for a structured output;
- Tactic ③ Ask the model to check whether conditions are satisfied;
- Tactic ④ “Few-shot” prompting.

GIVE THE MODEL TIME TO “THINK”

- Tactic ① Specify the steps required to complete a task;
- Tactic ② Instruct the model to work out its own solution before rushing to a conclusion.



ChatGPT Prompt Engineering for Developers (2/3)

Prompting Principles



Load the API key and relevant Python libraries

```
[ ]: import openai
import os

from dotenv import load_dotenv, find_dotenv
_ = load_dotenv(find_dotenv())

openai.api_key = os.getenv('OPENAI_API_KEY')
```

Helper function

```
[ ]: def get_completion(prompt, model="gpt-3.5-turbo"):
    messages = [{"role": "user", "content": prompt}]
    response = openai.ChatCompletion.create(
        model=model,
        messages=messages,
        temperature=0,
    )
    return response.choices[0].message["content"]
```



ChatGPT Prompt Engineering for Developers (3/3)

Prompting Principles



```
[ ]: text = """  
Some long text!  
"""  
prompt = f"""  
Summarize the text delimited by triple backticks \  
into a single sentence.  
```{text}```  
"""
response = get_completion(prompt)
print(response)
```



### CREDIT ATTRIBUTION

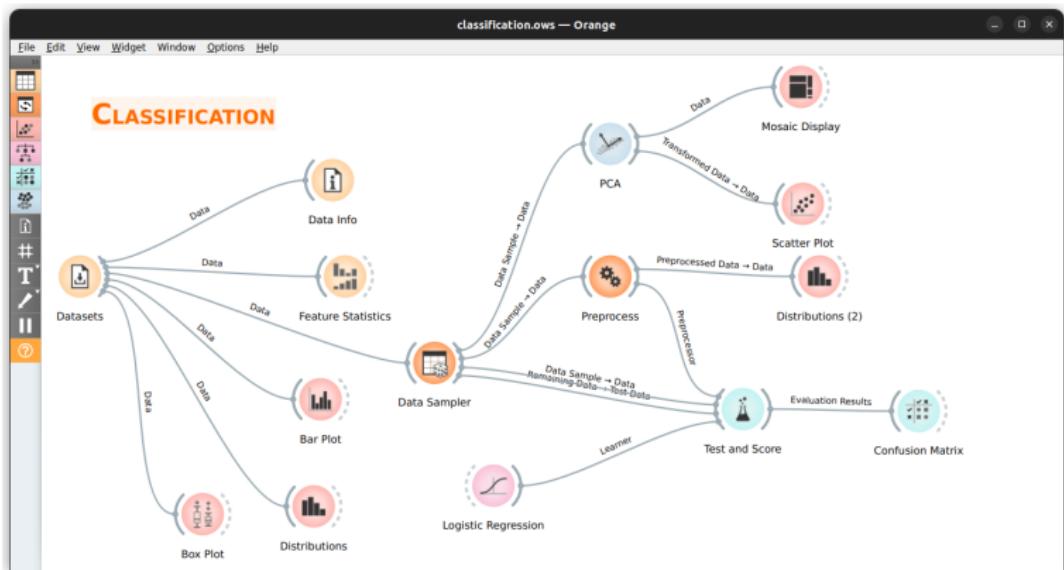
<https://learn.deeplearning.ai/> → ChatGPT Prompt Engineering for Developers → Guidelines



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On the day of assignment, you will be informed about the **dataset to consider, specific features to keep, and name of machine learning model to build**. You will be asked to conduct the experiment successfully (*pipeline, featurization, split, etc.*)



<https://github.com/a-mhamdi/dm-orange>

ORANGE DATA MINING

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# Knowledge Check



1

Go to [wooclap.com](https://app.wooclap.com/MLPY)

2

Enter the event code in the top banner

Event code  
**MLPY**

<https://app.wooclap.com/MLPY>

## Further Reading (1/2)

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## Further Reading (2/2)

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