

If the space provided for an answer is not sufficient, please continue on the back or attach an additional sheet.

Name:

Term: Subject: System Modeling & Control

Teacher: A. Mhamdi



Do not write in this table.

Question:	1	Total
Points:	1	1
Score:		

1. (1 point) ***

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$$\frac{d^2y}{dt^2} + 2 \times m \times \omega_0 \frac{dy}{dt} + \omega_0^2 y(t) = k \omega_0^2 u(t), \quad \text{where: } y(0) = 0 \text{ \& } \dot{y}(0) = 0$$

```
[1]: #####  
k, m, o = 1, 1, 1.5 # SIMULATION'S SETTINGS #  
#####
```

```
[2]: import numpy as np  
import matplotlib.pyplot as plt  
  
from scipy.signal import step
```

Numeric Integration: ODE

```
[3]: def mySys(x, t):  
    u = 1  
    dotx = [x[1], -o**2*x[0]-2*m*o*x[1] + k*o**2*u]  
    return dotx
```

```
[4]: from scipy.integrate import odeint
```

```
[5]: tspan = np.linspace(0.0, 10.0, 100)  
vect = odeint(mySys, [0, 0], tspan)  
y1 = vect[:, 0]
```

Transfer Function

```
[6]: from scipy.signal import TransferFunction as tf
```

```
[7]: hTF = tf([k*o**2], [1, 2*m*o, o**2])  
_, y2 = step(hTF, T=tspan)
```

State Space

```
[8]: from scipy.signal import StateSpace as ss
```

```
[9]: A = np.array([[0, 1], [-o**2, -2*m*o]])  
B = np.array([[0], [k*o**2]])  
C = np.array([[1, 0]])  
D = np.array([[0]])  
  
hSS = ss(A, B, C, D)  
_, y3 = step(hSS, T=tspan)
```

```
[10]: plt.plot(tspan, y1, 'r--', linewidth=2, label='ODE')  
plt.plot(tspan, y2, 'g--', linewidth=2, label='TF')  
plt.plot(tspan, y3, 'b--', linewidth=2, label='SS')  
  
plt.title('Step response of 2nd order LTI plant')  
plt.xlabel('t (sec)')  
plt.ylabel('y(t)')  
plt.grid()  
plt.legend(loc='best')  
plt.show()
```