Discrete Structures. CSCI-150. Summer 2014.

## Homework 8.

Due Thr. Jul 3, 2014.

#### Problem 1

Decide whether each of these integers is congruent to 3 modulo 7.

- (a) 37
- (b) 66
- (c) -17
- (d) -67

# Problem 2 (Graded)

Prove that

$$24^{31} \equiv 23^{32} \pmod{19}$$
.

# Problem 3 (Graded)

Given two numbers,

$$a_0 = 172, \quad a_1 = 61,$$

write out the execution of the extended Euclidean algorithm. Find  $a_k = \gcd(a_0, a_1)$  and Bezout's coefficients  $x_k$  and  $y_k$ , i.e. the numbers such that the following equation is satisfied:

$$a_k = \gcd(a_0, a_1) = x_k a_0 + y_k a_1$$

If it's possible, find the multiplicative inverse of  $a_1$  modulo  $a_0$ .

### Problem 4 (Graded)

Repeat the task from the problem 3 for numbers

$$a_0 = 800, \quad a_1 = 33.$$

#### Problem 5

Verify that  $p=17,\ q=13,\ e=5,$  and d=77 are valid parameters for RSA encryption and decryption.

Encrypt the following two-blocks message M = (115, 209).

The encrypted message should be equal to C = (098, 014). Decrypt it back.