Discrete Structures. CSCI-150. Fall 2013.

$$(a \land b) \equiv (b \land a) \qquad \text{commutativity of } \land \\ (a \lor b) \equiv (b \lor a) \qquad \text{commutativity of } \lor \\ ((a \land b) \land c) \equiv (a \land (b \land c)) \qquad \text{associativity of } \land \\ ((a \lor b) \lor c) \equiv (a \lor (b \lor c)) \qquad \text{associativity of } \lor \\ \neg (\neg a) \equiv a \qquad \text{double-negation elimination} \\ (a \rightarrow b) \equiv (\neg b \rightarrow \neg a) \qquad \text{contraposition} \\ (a \rightarrow b) \equiv (\neg a \lor b) \qquad \text{implication elimination} \\ (a \rightarrow b) \equiv (a \rightarrow b) \land (b \rightarrow a) \qquad \text{biconditional elimination} \\ \neg (a \land b) \equiv (\neg a \lor \neg b) \qquad \text{De Morgan's Law} \\ \neg (a \lor b) \equiv (\neg a \lor \neg b) \qquad \text{De Morgan's Law} \\ (a \land (b \lor c)) \equiv (a \land b) \lor (a \land c) \qquad \text{distributivity of } \land \text{ over } \lor \\ (a \lor (b \land c)) \equiv (a \lor b) \land (a \lor c) \qquad \text{distributivity of } \lor \text{ over } \land \\ \hline \frac{p}{p \lor q} \qquad \text{``} \land \text{-Introduction''} \qquad \qquad \frac{p \rightarrow q}{p} \qquad \text{``Modus Tollens''} \\ \hline \frac{p}{p \rightarrow q} \qquad \text{``} \land \text{-Elimination''} \qquad \qquad \frac{p \lor q}{p} \qquad \text{``} \land \text{-Elimination''} \\ \hline \frac{p}{p \rightarrow q} \qquad \text{``} \land \text{-Elimination''} \qquad \qquad \frac{p \lor q}{q} \qquad \text{``} \land \text{-Elimination''} \\ \hline \frac{p}{p \rightarrow q} \qquad \text{``} \land \text{-Elimination''} \qquad \qquad \frac{p \lor q}{q} \qquad \text{``} \land \text{-Elimination''} \\ \hline \frac{p}{q \rightarrow q} \qquad \text{``} \land \text{-Elimination''} \qquad \qquad \frac{p \lor q}{q} \qquad \text{``} \land \text{-Elimination''} \\ \hline \frac{p \lor q}{q} \qquad \text{``} \land \text{-Elimination''} \qquad \qquad \frac{p \lor q}{q} \qquad \text{``} \land \text{-Elimination''} \\ \hline \frac{p \lor q}{q} \qquad \text{``} \land \text{-Elimination''} \qquad \qquad \frac{p \lor q}{q} \qquad \text{``} \land \text{-Elimination''} \\ \hline \frac{p \lor q}{q} \qquad \text{``} \land \text{-Elimination''} \qquad \qquad \frac{p \lor q}{q} \qquad \text{``} \land \text{-Elimination''} \\ \hline \frac{p \lor q}{q} \qquad \text{``} \land \text{-Elimination''} \qquad \qquad \frac{p \lor q}{q} \qquad \text{``} \land \text{-Elimination''} \\ \hline \frac{p \lor q}{q} \qquad \text{``} \land \text{-Elimination''} \qquad \qquad \Rightarrow \text{-Introduction''} (\text{Deduction theorem})$$