Concepts and Techniques

— Chapter 2 —

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Chapter 2: Getting to Know Your Data



- Basic Statistical Descriptions of Data
- Data Visualization
- Measuring Data Similarity and Dissimilarity
- Summary

Types of Data Sets

- Record
 - Relational records
 - Data matrix, e.g., numerical matrix, crosstabs

 Document data: text documents: termfrequency vector

- Transaction data
- Graph and network
 - World Wide Web
 - Social or information networks
 - Molecular Structures
- Ordered
 - Video data: sequence of images
 - Temporal data: time-series
 - Sequential Data: transaction sequences
 - Genetic sequence data
- Spatial, image and multimedia:
 - Spatial data: maps
 - Image data:
 - Video data:

m-	team	coach	pla У	ball	score	game	n <u>V</u> .	lost	timeout	season
Document 1	3	0	5	0	2	6	0	2	0	2
Document 2	0	7	0	2	1	0	0	3	0	0
Document 3	0	1	0	0	1	2	2	0	3	0

TID	Items
1	Bread, Coke, Milk
2	Beer, Bread
3	Beer, Coke, Diaper, Milk
4	Beer, Bread, Diaper, Milk
5	Coke, Diaper, Milk

Important Characteristics of Structured Data

- Dimensionality
 - Curse of dimensionality
- Sparsity
 - Only presence counts
- Resolution
 - Patterns depend on the scale
- Distribution
 - Centrality and dispersion

Data Objects

- Data sets are made up of data objects.
- A data object represents an entity.
- Examples:
 - sales database: customers, store items, sales
 - medical database: patients, treatments
 - university database: students, professors, courses
- Also called samples, examples, instances, data points, objects, tuples.
- Data objects are described by attributes.
- Database rows -> data objects; columns ->attributes.

Attributes

- Attribute (or dimensions, features, variables): a data field, representing a characteristic or feature of a data object.
 - E.g., customer _ID, name, address
- Types:
 - Nominal
 - Binary
 - Numeric: quantitative
 - Interval-scaled
 - Ratio-scaled

Attribute Types

- Nominal: categories, states, or "names of things"
 - Hair_color = {auburn, black, blond, brown, grey, red, white}
 - marital status, occupation, ID numbers, zip codes

Binary

- Nominal attribute with only 2 states (0 and 1)
- Symmetric binary: both outcomes equally important
 - e.g., gender
- Asymmetric binary: outcomes not equally important.
 - e.g., medical test (positive vs. negative)
 - Convention: assign 1 to most important outcome (e.g., HIV positive)

Ordinal

- Values have a meaningful order (ranking) but magnitude between successive values is not known.
- Size = {small, medium, large}, grades, army rankings

Numeric Attribute Types

- Quantity (integer or real-valued)
- Interval
 - Measured on a scale of equal-sized units
 - Values have order
 - E.g., temperature in C°or F°, calendar dates
 - No true zero-point
- Ratio
 - Inherent zero-point
 - We can speak of values as being an order of magnitude larger than the unit of measurement (10 K° is twice as high as 5 K°).
 - e.g., temperature in Kelvin, length, counts, monetary quantities

Discrete vs. Continuous Attributes

Discrete Attribute

- Has only a finite or countably infinite set of values
 - E.g., zip codes, profession, or the set of words in a collection of documents
- Sometimes, represented as integer variables
- Note: Binary attributes are a special case of discrete attributes

Continuous Attribute

- Has real numbers as attribute values
 - E.g., temperature, height, or weight
- Practically, real values can only be measured and represented using a finite number of digits
- Continuous attributes are typically represented as floating-point variables

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Basic Statistical Descriptions of Data

- Motivation
 - To better understand the data: central tendency, variation and spread
- Data dispersion characteristics
 - median, max, min, quantiles, outliers, variance, etc.
- Numerical dimensions correspond to sorted intervals
 - Data dispersion: analyzed with multiple granularities of precision
 - Boxplot or quantile analysis on sorted intervals
- Dispersion analysis on computed measures
 - Folding measures into numerical dimensions
 - Boxplot or quantile analysis on the transformed cube

Measuring the Central Tendency

- Mean (algebraic measure) (sample vs. population): $\overline{X} = \frac{1}{n} \sum_{i=1}^{n} X_i$ $\mu = \frac{\sum_{i=1}^{N} X_i}{N}$ Note: *n* is sample size and *N* is population size.
 - Weighted arithmetic mean:
 - Trimmed mean: chopping extreme values $\bar{x} = \frac{i=1}{\sum_{i=1}^{n} w_i}$
- Median:
 - Middle value if odd number of values, or average of the middle two values otherwise
 - Estimated by interpolation (for *grouped data*):

$$median = L_1 + (\frac{n/2 - (\sum freq)l}{freq_{median}}) width$$

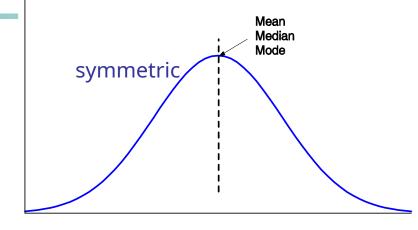
- Mode
 - Value that occurs most frequently in the data
 - Unimodal, bimodal, trimodal
 - Empirical formula: $mean mode = 3 \times (mean median)$

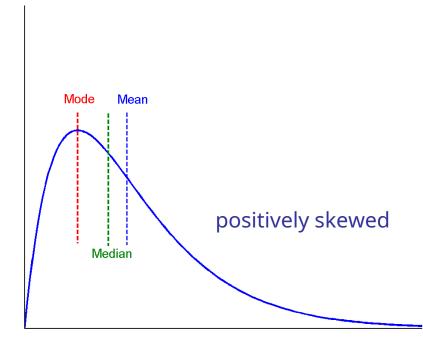
age	frequency
$\overline{1-5}$	200

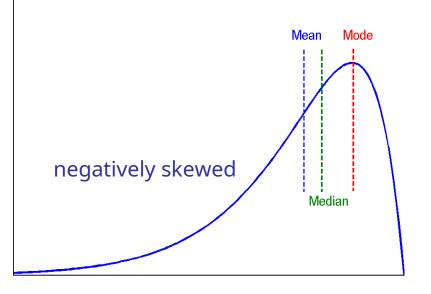
- 6-15450
- 16-20300
- 21 501500
- 51 80700
- 81 11044

Symmetric vs. Skewed Data

 Median, mean and mode of symmetric, positively and negatively skewed data







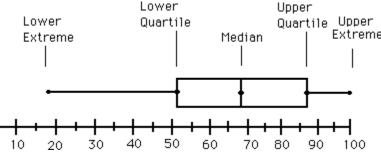
Measuring the Dispersion of Data

- Quartiles, outliers and boxplots
 - Quartiles: Q₁ (25th percentile), Q₃ (75th percentile)
 - Inter-quartile range: $IQR = Q_3 Q_1$
 - Five number summary: min, Q_1 , median, Q_3 , max
 - **Boxplot**: ends of the box are the quartiles; median is marked; add whiskers, and plot outliers individually
 - **Outlier**: usually, a value higher/lower than 1.5 x IQR
- Variance and standard deviation (sample: s, population: σ)

Variance: (algebraic, scalable computation)
$$s^{2} = \frac{1}{n-1} \sum_{i=1}^{n} (x_{i} - \bar{x})^{2} = \frac{1}{n-1} \left[\sum_{i=1}^{n} x_{i}^{2} - \frac{1}{n} (\sum_{i=1}^{n} x_{i})^{2} \right] \qquad \sigma^{2} = \frac{1}{N} \sum_{i=1}^{n} (x_{i} - \mu)^{2} = \frac{1}{N} \sum_{i=1}^{n} x_{i}^{2} - \mu^{2}$$

Standard deviation s (or σ) is the square root of variance s^2 (or σ^2)

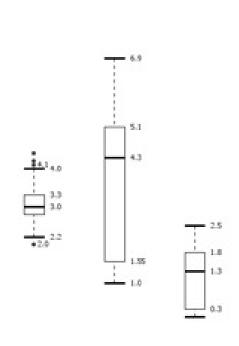
Boxplot Analysis



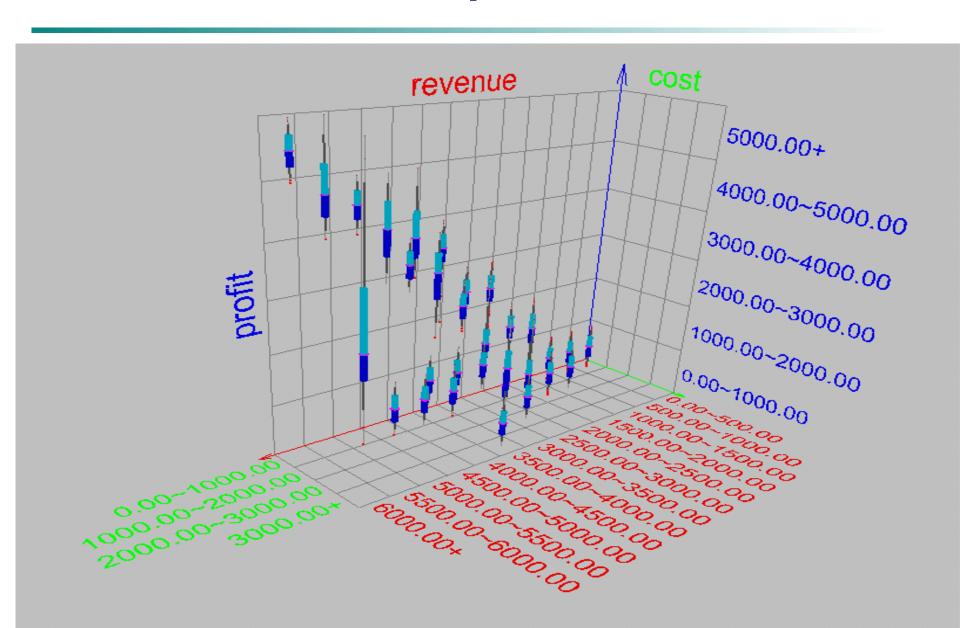
- Five-number summary of a distribution
 - Minimum, Q1, Median, Q3, Maximum

Boxplot

- Data is represented with a box
- The ends of the box are at the first and third quartiles, i.e., the height of the box is IQR
- The median is marked by a line within the box
- Whiskers: two lines outside the box extended to Minimum and Maximum
- Outliers: points beyond a specified outlier threshold, plotted individually

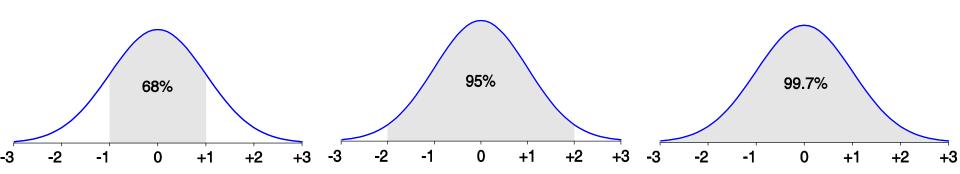


Visualization of Data Dispersion: 3-D Boxplots



Properties of Normal Distribution Curve

- The normal (distribution) curve
 - From μ-σ to μ+σ: contains about 68% of the measurements (μ: mean, σ: standard deviation)
 - From μ –2 σ to μ +2 σ : contains about 95% of it
 - From μ –3 σ to μ +3 σ : contains about 99.7% of it

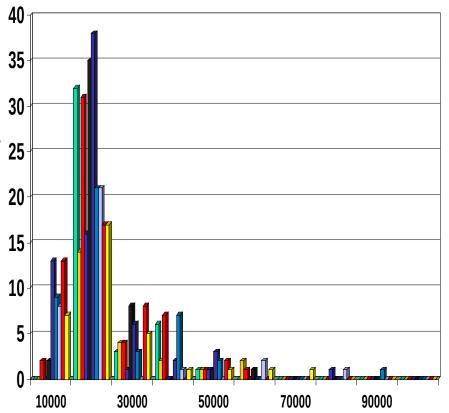


Graphic Displays of Basic Statistical Descriptions

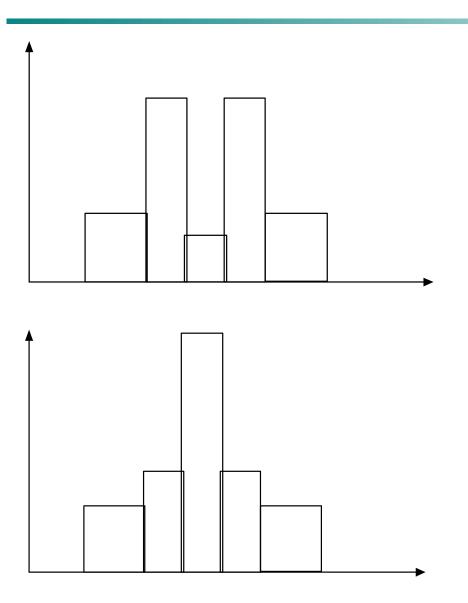
- Boxplot: graphic display of five-number summary
- Histogram: x-axis are values, y-axis repres. frequencies
- **Quantile plot**: each value x_i is paired with f_i indicating that approximately 100 f_i % of data are $\leq x_i$
- Quantile-quantile (q-q) plot: graphs the quantiles of one univariant distribution against the corresponding quantiles of another
- Scatter plot: each pair of values is a pair of coordinates and plotted as points in the plane

Histogram Analysis

- Histogram: Graph display of tabulated frequencies, shown as bars
- It shows what proportion of cases 30fall into each of several categories 25-
- Differs from a bar chart in that it is the area of the bar that denotes the value, not the height as in bar charts, a crucial distinction when the categories are not of uniform width
- The categories are usually specified as non-overlapping intervals of some variable. The categories (bars) must be adiacent



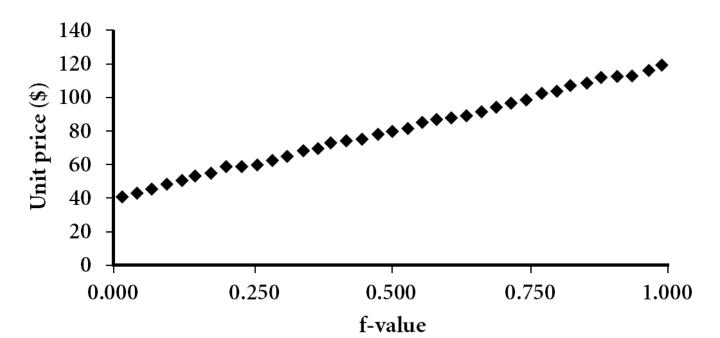
Histograms Often Tell More than Boxplots



- The two histograms shown in the left may have the same boxplot representation
 - The same values for: min, Q1, median, Q3, max
 - But they have rather different data distributions

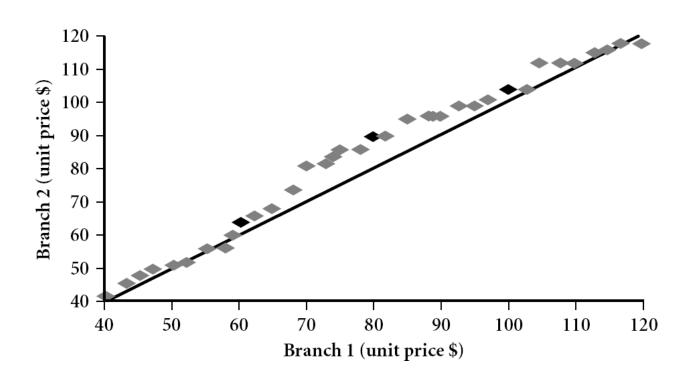
Quantile Plot

- Displays all of the data (allowing the user to assess both the overall behavior and unusual occurrences)
- Plots quantile information
 - For a data x_i data sorted in increasing order, f_i indicates that approximately 100 f_i % of the data are below or equal to the value x_i



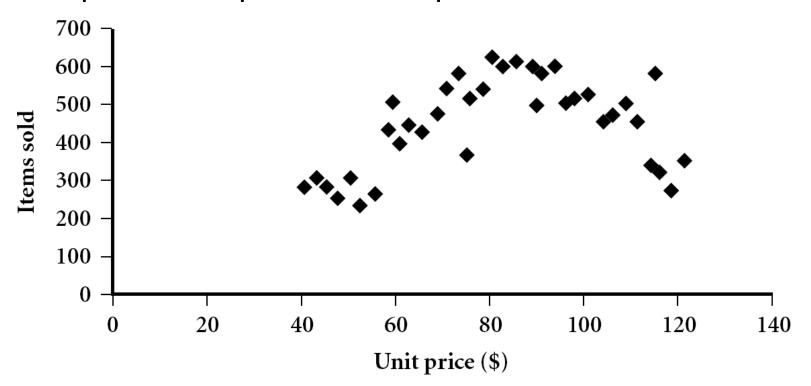
Quantile-Quantile (Q-Q) Plot

- Graphs the quantiles of one univariate distribution against the corresponding quantiles of another
- View: Is there is a shift in going from one distribution to another?
- Example shows unit price of items sold at Branch 1 vs. Branch 2 for each quantile. Unit prices of items sold at Branch 1 tend to be lower than those at Branch 2.

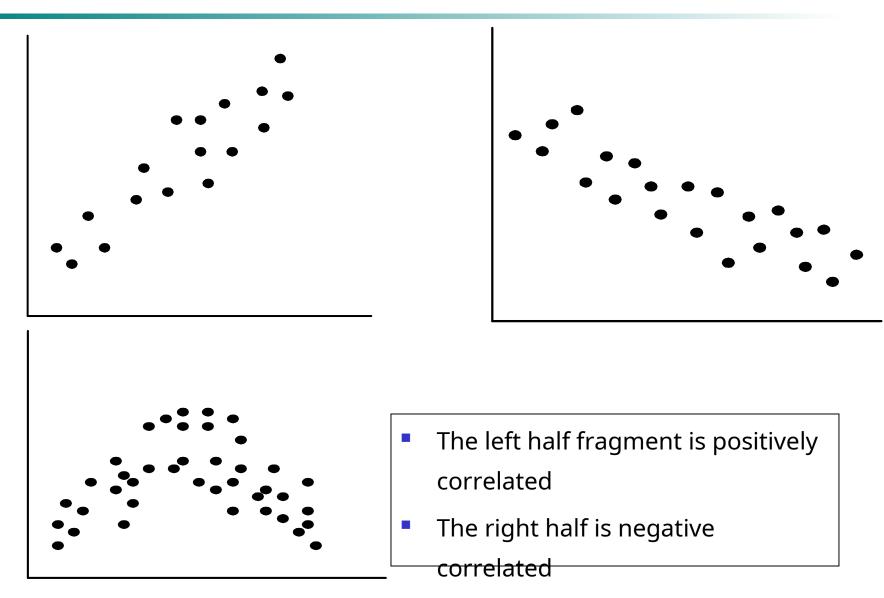


Scatter plot

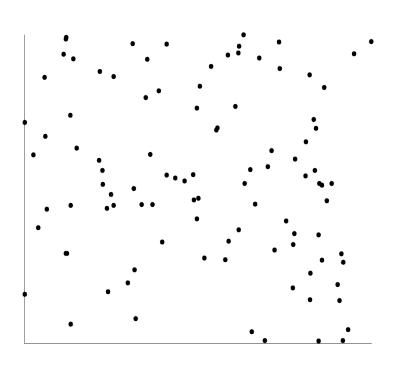
- Provides a first look at bivariate data to see clusters of points, outliers, etc
- Each pair of values is treated as a pair of coordinates and plotted as points in the plane

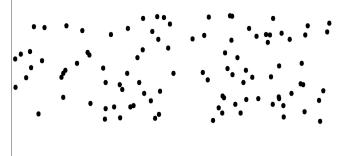


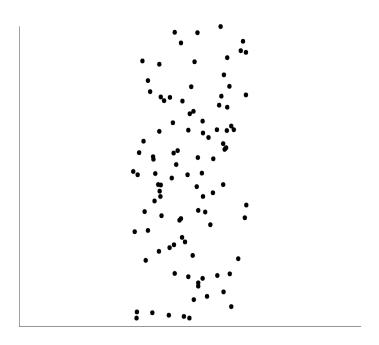
Positively and Negatively Correlated Data



Uncorrelated Data







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- Data Visualization



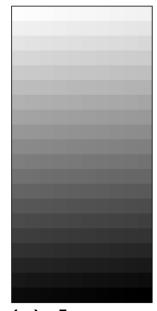
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Data Visualization

- Why data visualization?
 - Gain insight into an information space by mapping data onto graphical primitives
 - Provide qualitative overview of large data sets
 - Search for patterns, trends, structure, irregularities, relationships among data
 - Help find interesting regions and suitable parameters for further quantitative analysis
 - Provide a visual proof of computer representations derived
- Categorization of visualization methods:
 - Pixel-oriented visualization techniques
 - Geometric projection visualization techniques
 - Icon-based visualization techniques
 - Hierarchical visualization techniques
 - Visualizing complex data and relations

Pixel-Oriented Visualization Techniques

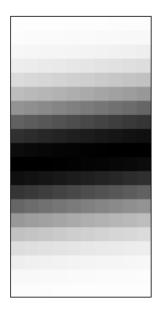
- For a data set of m dimensions, create m windows on the screen, one for each dimension
- The m dimension values of a record are mapped to m pixels at the corresponding positions in the windows
- The colors of the pixels reflect the corresponding values



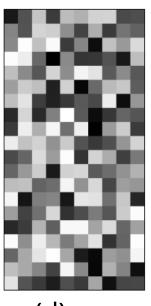
(a) Income



(b) Credit Limit



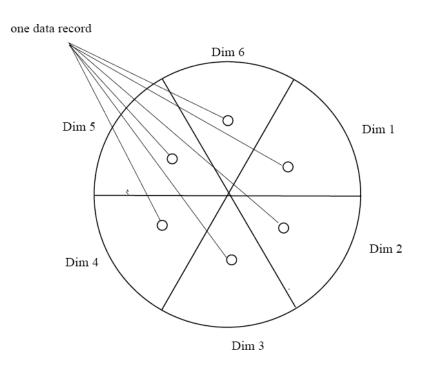
(c) transaction volume



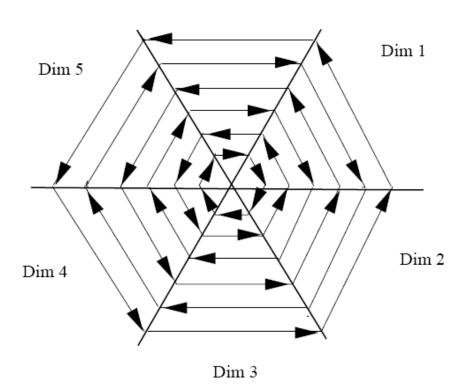
(d) age

Laying Out Pixels in Circle Segments

 To save space and show the connections among multiple dimensions, space filling is often done in a circle segment



(a) Representing a data record in circle segment



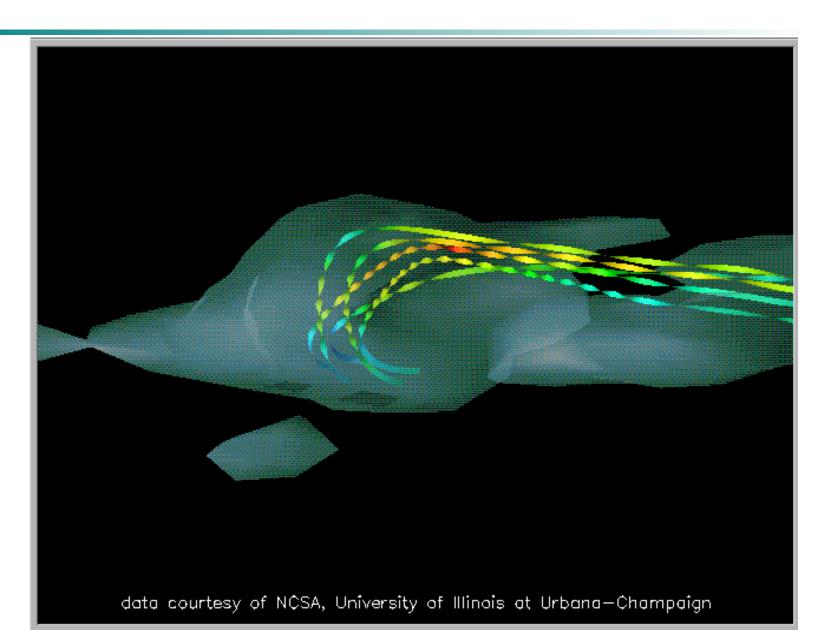
Dim 6

(b) Laying out pixels in circle segment

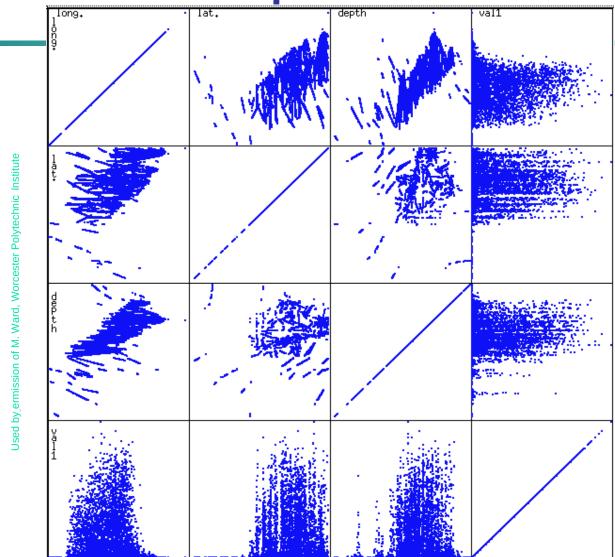
Geometric Projection Visualization Techniques

- Visualization of geometric transformations and projections of the data
- Methods
 - Direct visualization
 - Scatterplot and scatterplot matrices
 - Landscapes
 - Projection pursuit technique: Help users find meaningful projections of multidimensional data
 - Prosection views
 - Hyperslice
 - Parallel coordinates

Direct Data Visualization

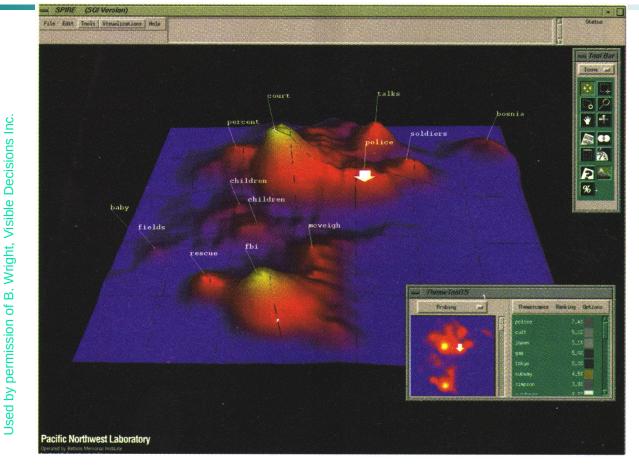


Scatterplot Matrices



Matrix of scatterplots (x-y-diagrams) of the k-dim. data [total of (k2/2-k) scatterplots]

Landscapes



news articles visualized as a landscape

- Visualization of the data as perspective landscape
- The data needs to be transformed into a (possibly artificial) 2D spatial representation which preserves the characteristics of the data

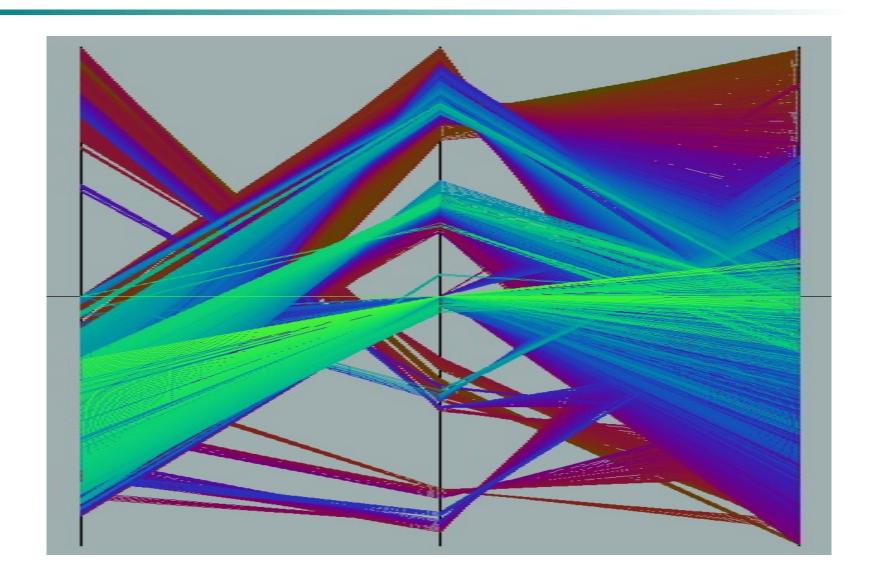
Parallel Coordinates

- n equidistant axes which are parallel to one of the screen axes and correspond to the attributes
- The axes are scaled to the [minimum, maximum]: range of the corresponding attribute
- Every data item corresponds to a polygonal line which intersects each of the axes at the point which corresponds to the value for the attribute

• • •

Attr. 1 Attr. 2 Attr. 3 Attr. k

Parallel Coordinates of a Data Set



Icon-Based Visualization Techniques

- Visualization of the data values as features of icons
- Typical visualization methods
 - Chernoff Faces
 - Stick Figures
- General techniques
 - Shape coding: Use shape to represent certain information encoding
 - Color icons: Use color icons to encode more information
 - Tile bars: Use small icons to represent the relevant feature vectors in document retrieval

Chernoff Faces

- A way to display variables on a two-dimensional surface, e.g., let x be eyebrow slant, y be eye size, z be nose length, etc.
- The figure shows faces produced using 10 characteristics--head eccentricity, eye size, eye spacing, eye eccentricity, pupil size, eyebrow slant, nose size, mouth shape, mouth size, and mouth opening): Each assigned one of 10 possible values, generated using Mathematica (S. Dickson)
- REFERENCE: Gonick, L. and Smith, W. <u>The Cartoon Guide to Statistics.</u> New York: Harper Perennial, p. 212, 1993
- Weisstein, Eric W. "Chernoff Face." From *MathWorld--*A Wolfram Web Resource. <u>mathworld.wolfram.com/ChernoffFace.ht</u>















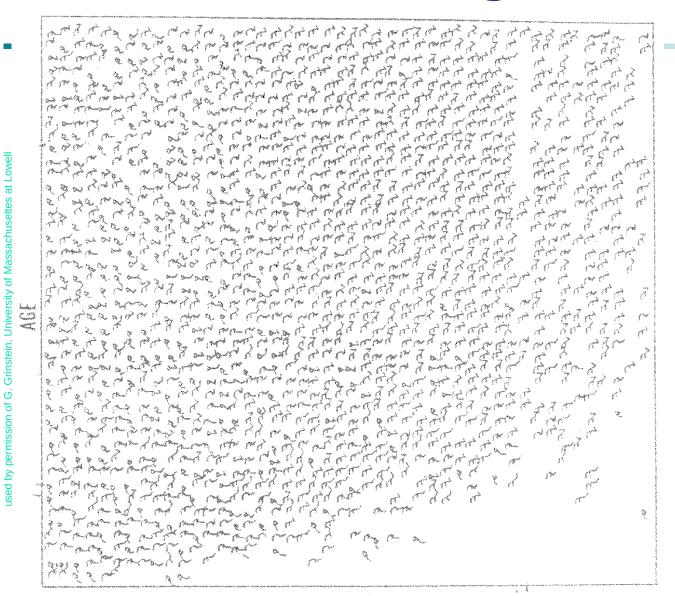








Stick Figure



A census data figure showing age, income, gender, education, etc.

A 5-piece stick figure (1 body and 4 limbs w. different angle/length)

INCOME

Hierarchical Visualization Techniques

- Visualization of the data using a hierarchical partitioning into subspaces
- Methods
 - Dimensional Stacking
 - Worlds-within-Worlds
 - Tree-Map
 - Cone Trees
 - InfoCube

Dimensional Stacking

attribute 4

attribute 2

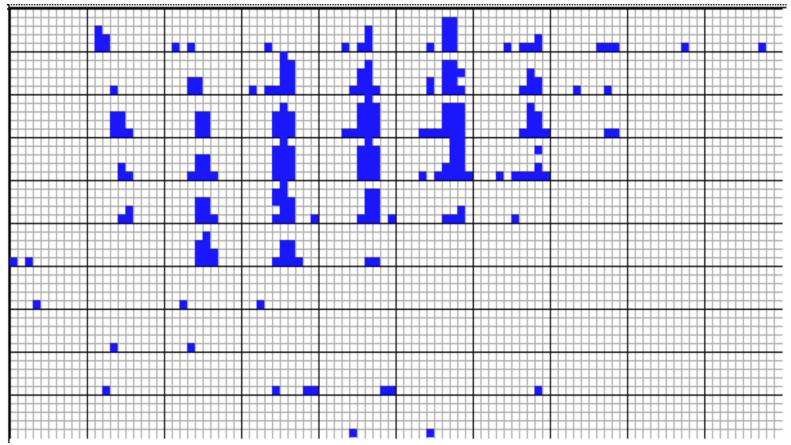
attribute 3

attribute 1

- Partitioning of the n-dimensional attribute space in 2-D subspaces, which are 'stacked' into each other
- Partitioning of the attribute value ranges into classes.
 The important attributes should be used on the outer levels.
- Adequate for data with ordinal attributes of low cardinality
- But, difficult to display more than nine dimensions

Dimensional Stacking

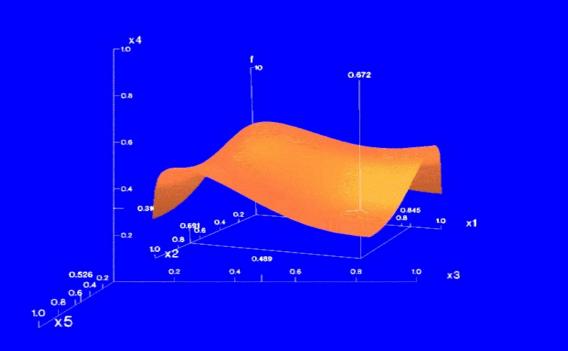




Visualization of oil mining data with longitude and latitude mapped to the outer x-, y-axes and ore grade and depth mapped to the inner x-, y-axes

Worlds-within-Worlds

- Assign the function and two most important parameters to innermost world
- Fix all other parameters at constant values draw other (1 or 2 or 3 dimensional worlds choosing these as the axes)
- Software that uses this paradigm
 - N-vision: Dynamic interaction through data glove and stereo displays, including rotation, scaling (inner) and translation (inner/outer)
 - Auto Visual: Static interaction by means of queries



Tree-Map

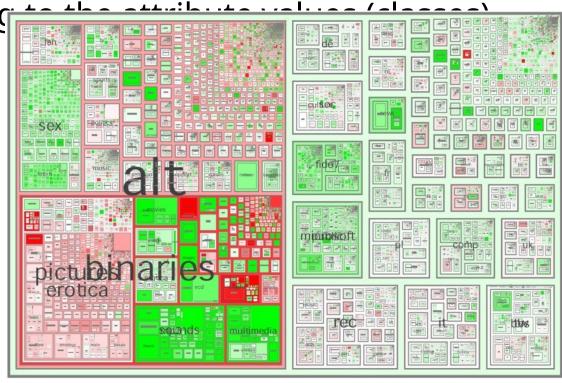
 Screen-filling method which uses a hierarchical partitioning of the screen into regions depending on the attribute values

The x- and y-dimension of the screen are partitioned

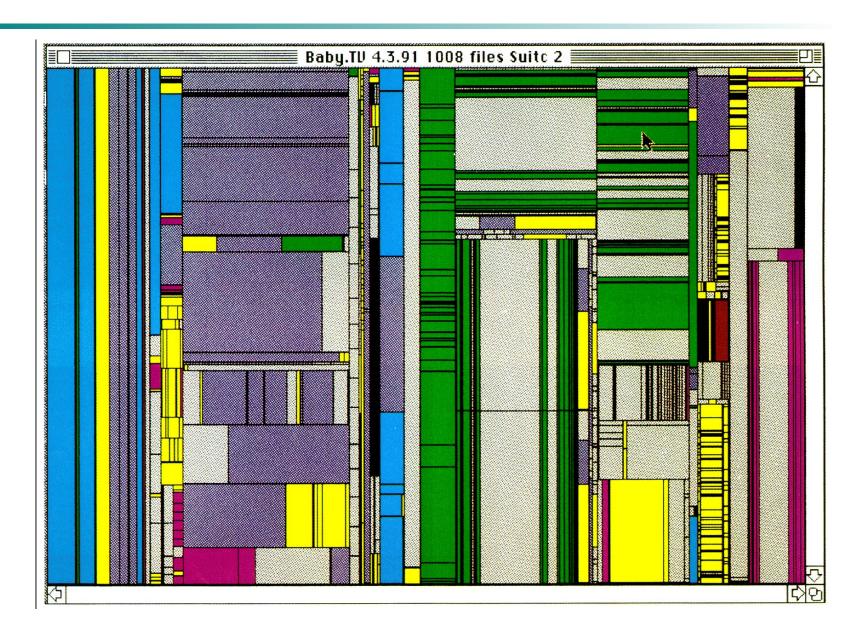
Ack.:

alternately according

MSR Netscan Image



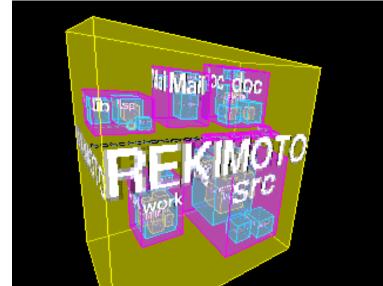
Tree-Map of a File System (Schneiderman)



InfoCube

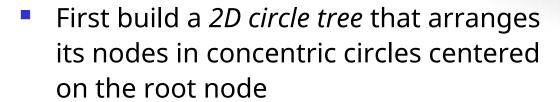
- A 3-D visualization technique where hierarchical information is displayed as nested semitransparent cubes
- The outermost cubes correspond to the top level data, while the subnodes or the lower level data are represented as smaller cubes inside the

outermost cubes, and so on



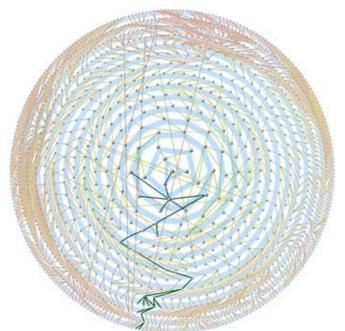
Three-D Cone Trees

 3D cone tree visualization technique works well for up to a thousand nodes or so



- Cannot avoid overlaps when projected to 2D
- G. Robertson, J. Mackinlay, S. Card.
 "Cone Trees: Animated 3D Visualizations of Hierarchical Information", ACM SIGCHI'91
- Graph from Nadeau Software
 Consulting website: Visualize a social
 network data set that models the: w确以Andeausoftware.com/articles/visualization

infection spreads from one person to



Visualizing Complex Data and Relations

- Visualizing non-numerical data: text and social networks
- Tag cloud: visualizing user-generated tags
 - The importance of tag is represented by font size/color
- Besides text data, there are also methods to visualize relationships, such as visualizing social networks



Newsmap: Google News Stories in

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Similarity and Dissimilarity

Similarity

- Numerical measure of how alike two data objects are
- Value is higher when objects are more alike
- Often falls in the range [0,1]
- Dissimilarity (e.g., distance)
 - Numerical measure of how different two data objects are
 - Lower when objects are more alike
 - Minimum dissimilarity is often 0
 - Upper limit varies
- Proximity refers to a similarity or dissimilarity

Data Matrix and Dissimilarity Matrix

Data matrix

- n data points with p dimensions
- Two modes

$$\begin{bmatrix} x_{11} & \cdots & x_{1f} & \cdots & x_{1p} \\ \cdots & \cdots & \cdots & \cdots & \cdots \\ x_{i1} & \cdots & x_{if} & \cdots & x_{ip} \\ \cdots & \cdots & \cdots & \cdots & \cdots \\ x_{n1} & \cdots & x_{nf} & \cdots & x_{np} \end{bmatrix}$$

Dissimilarity matrix

- n data points, but registers only the distance
- A triangular matrix
- Single mode

$$\begin{bmatrix} 0 \\ d(2,1) & 0 \\ d(3,1) & d(3,2) & 0 \\ \vdots & \vdots & \vdots \\ d(n,1) & d(n,2) & \dots & \dots & 0 \end{bmatrix}$$

Proximity Measure for Nominal Attributes

- Can take 2 or more states, e.g., red, yellow, blue, green (generalization of a binary attribute)
- Method 1: Simple matching
 - m: # of matches, jp: $toPaI_p$ # of variables
- Method 2: Use a large number of binary attributes
 - creating a new binary attribute for each of

Proximity Measure for Binary Attributes

A contingency table for binary data

- Distance measure for symmetric $d(i,j) = \frac{r+s}{q+r+s+t}$ binary variables:
- Distance measure for asymmetric $d(i, j) = \frac{r+s}{q+r+s}$ binary variables:
- Worle | 466 and coefficient is the same as "coherence":

$$coherence(i,j) = \frac{sup(i,j)}{sup(i) + sup(j) - sup(i,j)} = \frac{q}{(q+r) + (q+s) - q}$$

Dissimilarity between Binary Variables

Example

Name	Gender	Fever	Cough	Test-1	Test-2	Test-3	Test-4
Jack	M	Y	N	P	N	N	N
Mary	F	Y	N	P	N	P	N
Jim	M	Y	P	N	N	N	N

- Gender is a symmetric attribute
- The remaining attributes are asymmetric binary
- Let the values Y and P be 1, and the value N 0

$$d(jack, mary) = \frac{0+1}{2+0+1} = 0.33$$

$$d(jack, jim) = \frac{1+1}{1+1+1} = 0.67$$

$$d(jim, mary) = \frac{1+2}{1+1+2} = 0.75$$

Standardizing Numeric Data

- Z-score: $z = \frac{x \mu}{\sigma}$
 - X: raw score to be standardized, μ: mean of the population, σ: standard deviation
 - the distance between the raw score and the population mean in units of the standard deviation
 - negative when the raw score is below the mean, "+" when above
- An alternative way: $\mathcal{L}_{h}^{1}(\mathbf{q}_{\mathbf{q}})$ An alternative way: $\mathcal{L}_{h}^{1}(\mathbf{q}_{\mathbf{q}})$

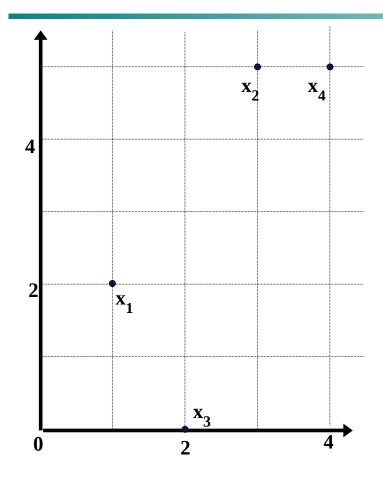
where

$$m_{f} = \frac{1}{n} (x_{1f} + x_{2f} + \dots + x_{nf})$$

$$z_{if} = \frac{x_{if} - m_{f}}{s_{f}}$$

- standardized measure (z-score):
- Using mean absolute deviation is more robust than using standard deviation

Example: Data Matrix and Dissimilarity Matrix



Data Matrix

point	attribute1	attribute2
x1	1	2
<i>x</i> 2	3	5
х3	2	0
x4	4	5

Dissimilarity Matrix

(with Euclidean Distance)

	x1	<i>x</i> 2	<i>x</i> 3	x4
x1	0			
<i>x</i> 2	3.61	0		
х3	5.1	5.1	0	
x4	4.24	1	5.39	0

Distance on Numeric Data: Minkowski Distance

Minkowski distance: A popular distance measure

$$d(i,j) = \sqrt[h]{|x_{i1} - x_{j1}|^h + |x_{i2} - x_{j2}|^h + \dots + |x_{ip} - x_{jp}|^h}$$

where $i = (x_{i1}, x_{i2}, ..., x_{ip})$ and $j = (x_{j1}, x_{j2}, ..., x_{jp})$ are two pdimensional data objects, and h is the order (the
distance so defined is also called L-h norm)

- Properties
 - d(i, j) > 0 if $i \neq j$, and d(i, i) = 0 (Positive definiteness)
 - d(i, j) = d(j, i) (Symmetry)
 - $d(i, j) \le d(i, k) + d(k, j)$ (Triangle Inequality)
- A distance that satisfies these properties is a metric

Special Cases of Minkowski Distance

- h = 1: Manhattan (city block, L₁ norm) distance
 - E.g., the Hamming distance: the number of bits that are different between two binary vectors

$$d(i,j) = x_{i_1} - x_{j_1} | + |x_{i_2} - x_{j_2}| + ... + |x_{i_p} - x_{j_p}|$$

• h = 2: (L₂ norm) Euclidean distance

$$d(i,j) = \sqrt{(|x_{i1} - x_{j1}|^2 + |x_{i2} - x_{j2}|^2 + ... + |x_{ip} - x_{jp}|^2)}$$

- $h \to \infty$. "supremum" (L_{max} norm, L_{∞} norm) distance.
 - This is the maximum difference between any component (attribute) of the vectors

$$d(i,j) = \lim_{h \to \infty} \left(\sum_{f=1}^{p} |x_{if} - x_{jf}|^h \right)^{\frac{1}{h}} = \max_{f} |x_{if} - x_{jf}|$$

Example: Minkowski Distance

Dissimilarity Matrices

point	attribute 1	attribute 2		
x1	1	2		
x 2	3	5		
x 3	2	0		
x4	4	5		

1					
			x ₂	x ₄	
2	x ₁				
		X ₂			
0		2		4	•

Manhattan (L₁)

L	x1	x2	х3	x4
x1	0			
x2	5	0		
x 3	3	6	0	
x4	6	1	7	0

Euclidean (L₂)

L2	x1	x 2	х3	x4
x1	0			
x2	3.61	0		
x 3	2.24	5.1	0	
x4	4.24	1	5.39	0

Supremum

L∞	x1	x 2	х3	x4
x1	0			
x 2	3	0		
х3	2	5	0	
x4	3	1	5	0

Ordinal Variables

- An ordinal variable can be discrete or continuous
- Order is important, e.g., rank
- Can be treated like interval-scaled
 - replace x_{if} by their rank $r_{if} \in \{1,...,M_f\}$
 - map the range of each variable onto [0, 1] by replacing i-th object in the f-th variable by

$$z_{if} = \frac{r_{if} - 1}{M_f - 1}$$

 compute the dissimilarity using methods for interval-scaled variables

Attributes of Mixed Type

- A database may contain all attribute types
 - Nominal, symmetric binary, asymmetric binary, numeric, ordinal
- One may use a weighted formula to combine their effects $\sum_{p} S(f) A(f)$

$$d(i,j) = \frac{\sum_{f=1}^{p} \delta_{ij}^{(f)} d_{ij}^{(f)}}{\sum_{f=1}^{p} \delta_{ij}^{(f)}}$$

f is binary or nominal:

$$d_{ij}^{(f)} = 0$$
 if $x_{if} = x_{if}$, or $d_{ij}^{(f)} = 1$ otherwise

- f is numeric: use the normalized distance
- f is ordinal
 - Compute ranks r_{if} and

$$Z_{if} = \frac{r_{if} - 1}{M_{f} - 1}$$

Treat z_s as interval-scaled

Cosine Similarity

 A document can be represented by thousands of attributes, each recording the frequency of a particular word (such as keywords) or phrase in the document.

Document	team	coach	hockey	baseball	soccer	penalty	score	win	loss	season
Document1	5	0	3	0	2	0	0	2	0	0
Document2	3	0	2	0	1	1	0	1	0	1
Document3	0	7	0	2	1	0	0	3	0	0
Document4	0	1	0	0	1	2	2	0	3	0

- Other vector objects: gene features in micro-arrays, ...
- Applications: information retrieval, biologic taxonomy, gene feature mapping, ...
- Cosine measure: If d_1 and d_2 are two vectors (e.g., term-frequency vectors), then

$$cos(d_1, d_2) = (d_1 \cdot d_2) / ||d_1|| ||d_2||,$$

where \bullet indicates vector dot product, ||d||: the length of vector d

Example: Cosine Similarity

- cos $(d_1, d_2) = (d_1 \cdot d_2) / ||d_1|| ||d_2||$, where \cdot indicates vector dot product, ||d|: the length of vector d
- Ex: Find the similarity between documents 1 and 2.

 $d_1 = (5, 0, 3, 0, 2, 0, 0, 2, 0, 0)$

$$\begin{aligned} d_2 &= (3, 0, 2, 0, 1, 1, 0, 1, 0, 1) \\ d_1 &\bullet d_2 &= 5*3 + 0*0 + 3*2 + 0*0 + 2*1 + 0*1 + 0*1 + 2*1 + 0*0 + 0*1 = 25 \\ &||d_1|| &= (5*5 + 0*0 + 3*3 + 0*0 + 2*2 + 0*0 + 0*0 + 2*2 + 0*0 + 0*0)^{0.5} = (42)^{0.5} = 6.481 \\ &||d_2|| &= (3*3 + 0*0 + 2*2 + 0*0 + 1*1 + 1*1 + 0*0 + 1*1 + 0*0 + 1*1)^{0.5} = (17)^{0.5} = 4.12 \\ &\cos(d_1, d_2) &= 0.94 \end{aligned}$$

Chapter 2: Getting to Know Your Data

- Data Objects and Attribute Types
- Basic Statistical Descriptions of Data
- Data Visualization
- Measuring Data Similarity and Dissimilarity
- Summary



Summary

- Data attribute types: nominal, binary, ordinal, interval-scaled, ratioscaled
- Many types of data sets, e.g., numerical, text, graph, Web, image.
- Gain insight into the data by:
 - Basic statistical data description: central tendency, dispersion, graphical displays
 - Data visualization: map data onto graphical primitives
 - Measure data similarity
- Above steps are the beginning of data preprocessing.
- Many methods have been developed but still an active area of research.

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