

4 生产函数 $q = 10L^{0.5}K^{0.5}$ 且 $w=r=10$

$$(A) q = 10L^{0.5}K^{0.5} \Rightarrow L^* = \frac{q^2}{10K}$$

$$STC = 10L^* + 10K = \frac{q^2}{10K} + 10K$$

$$AC = \frac{q}{10K} + \frac{10K}{q}, MC = \frac{q}{5K}$$

$$(B) \frac{dSTC}{dK} = \frac{-q^2}{10K^2} + 10 = 0 \Rightarrow K^2 = \frac{q}{10} \text{ 即 } STC$$

$$TC = STC(K = \sqrt{\frac{q}{10}}) = \frac{q^2}{10 \times \frac{q}{10}} + 10K = q + q = 2q$$

$$7. TC = q^3 - 12q^2 + q + 50$$

$$(A) AFC = \frac{FC}{q} = \frac{50}{10} = 5$$

$$(B) AVC = q^2 - 12q + 1 \Rightarrow \frac{dAVC}{dq} = 2q - 12 = 0 \quad q = 6$$

(C) 根据生产反成本的对偶性 $AVC \uparrow \quad AFC \downarrow \quad q \geq 6$

$$(D) MC = 3q^2 - 24q + 1 \Rightarrow \frac{dMC}{dq} = 6q - 24 = 0 \Rightarrow q = 4 \quad MC$$