

4. $q = 10L^{0.5}K^{0.5}$, 且 $w=r=10$. 但設 K 固定 K_0 .

(A) 求短期成本, 變動成本, 邊際成本函數:

TC

$$\frac{K}{L} \cdot \frac{10}{10} \quad MC = 2$$

$$\frac{5L^{-0.5}K^{0.5}}{5L^{0.5}K^{-0.5}} = \frac{K}{L}$$

$$|MRTS| = \frac{MPL}{MPK} = \frac{L}{K} = \frac{w}{r} = 1$$

$$\Rightarrow L^* = K^* = 0.1q$$

$$q = 10L^{0.5}K^{0.5} = 10 \cdot (100)^{0.5} = 100 \quad q = 10L^{0.5}K^{0.5} \rightarrow L^* = q^2/100K$$

$$TC = rK^* + wL^*$$

$$\hookrightarrow TC = 10L^* + 10K = (q^2/10K) + 10K$$

$$= 10 \cdot 0.1q + 10 \cdot 0.1q = 2q$$

$$AC = (q/10K) + (10K/q)$$

$$MC = 2$$

$$MC = q/5K$$

(B) 由(A)反推總成本函數

$$\frac{\partial \hookrightarrow TC}{\partial K} = \frac{-q^2}{10K^2} + 10 = 0 \Rightarrow \bar{K} = \frac{q}{10}$$

$$TC = \hookrightarrow TC(K = \bar{K}) = \frac{q^2}{10 \times (q/10)} + 10 \frac{q}{10} = q + q = 2q$$

HW

1. 短期成本函數 $TC = q^3 - 12q^2 + q + 50$, 且短期下的變動要素為勞動

(A) $q = 10$ 之 AFC .

$$AFC = \frac{FC}{q} = \frac{50}{10} = 5$$

(B) 產量多少時, $AVC = MC$

$$AVC = q^2 - 12q + 1$$

$$\rightarrow dAVC/dq = 2q - 12 = 0, q = 6$$

(C) 產量超過多少時, APL start 遞減

根據生產和成本的對偶性, 知道當 AVC 遞增時, APL 遞減

$$q \geq 6$$

(D) 產量超過多少時, MP_L start 遞減

$$MC = 3q^2 - 24q + 1 \quad dMC/dq = 6q - 24 = 0, q = 4$$

根據生產和成本的對偶性, 知道 MC 遞增時, MP_L 遞減

$$q \geq 4$$