$$\begin{split} G &= \{x^i | 0 \leq i \leq 342, x^{342} = 1\} \\ &\gcd(11, 343) = 1, x^{11} generates the Group. \end{split}$$

$$p \coloneqq 7; e \coloneqq 3; g \coloneqq x^{11}; h \coloneqq x^{41};$$

$$p := 7$$

$$e := 3$$

$$g := x^{11}$$

$$h := x^{41}$$
(1)

Step1:

 $x\theta \coloneqq 0;$ 

$$x\theta \coloneqq 0 \tag{2}$$

 $s\coloneqq x^{11\cdot 49\mod 343};\ h\theta\coloneqq x^{41\cdot 49\mod 343};$ 

$$s := x^{196}$$

$$h\theta := x^{294}$$
(3)

Searching  $for d\theta$ ;  $d\theta = 5 satisfies s^{d\theta} = h\theta$ 

 $d\theta \coloneqq 5;$ 

$$d0 \coloneqq 5 \tag{4}$$

 $x^{196.5 \mod 343}$ ;

$$x^{294}$$
 (5)

 $x1 \coloneqq x\theta + p^0 \cdot d\theta;$ 

$$x1 := 5 \tag{6}$$

Step 2:

 $h1 := x^{(-55+41)\cdot 7 \mod 343};$ 

$$h1 := x^{245} \tag{7}$$

Searching for d1;  $d1 = 3satisfies s^{d1} = h1$ 

d1 := 3;

$$d1 := 3 \tag{8}$$

 $x^{196\cdot 3 \mod 343}$ ;

$$x^{245}$$
 (9)

 $x2 := x1 + p^1 \cdot d1;$ 

$$x2 \coloneqq 26 \tag{10}$$

Step 3:

 $h2 := x^{-286+41 \mod 343};$ 

$$h2 \coloneqq x^{98} \tag{11}$$

Searching for d2; d2 = 4 satisfies  $s^{d2} = h2$ 

 $d2 \coloneqq 4;$ 

$$d2 := 4 \tag{12}$$

 $x^{196\cdot 4 \mod 343};$ 

$$x^{98}$$
 (13)

 $x3 \coloneqq x2 + p^2 \cdot d2;$ 

$$x3 \coloneqq 222 \tag{14}$$

 $x 3 \, is \, our \, logar ithm$