CS206 Data Structure

Homework #1

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0 About Programs

Program Language: C# 5.0 based on .NET Framework 4.5

Libraries: Standard library of .NET(ex: mscorlib.dll, System.Core.dll, System.Linq.dll)

Complier: C# Compiler in Visual Studio 2012 Update 4 (Any CPU)

Type of Executable File: .exe

Requirements: OS that supports .NET Framework 4.5(ex: Windows 7, 8, 8.1)

1 Program1

Executable File: Program1.exe

Source Files: Polynomial.cs, Term.cs, Program1.cs

Instruction: Program1.inst.txt

Sample Input, Output: Program1.sample.txt

$\mathbf{2}$ Program2

Executable File: Program2.exe

Source Files: Polynomial.cs, Term.cs, Program2.cs

Instruction: Program2.inst.txt

Sample Input, Output: Program2.sample.txt

3 Polynomial Calculus ADT

```
structure Polynomial
```

objects: a polynomial $\sum_{i=0}^{n} a_i x^i$ where $i \in \mathbb{N}_0 \wedge \forall_i a_i \in \mathbb{Z}$ functions: $(\forall poly1 (= \sum_{i=0}^{n_1} a_i x^i), poly2 (= \sum_{i=0}^{n_2} b_i x^i) \in Polynomial)$

 $Polynomial \ ADD(poly1, poly2)$

Let
$$\forall_{i>n_1} a_i = 0 \land \forall_{i>n_2} b_i = 0$$

return $\sum_{i=0}^{max\{n_1,n_2\}} (a_i + b_i) x^i$

return
$$\sum_{i=0}^{\max\{n_1,n_2\}} (a_i + b_i) x^i$$

Polynomial MULTIPLY(poly1, poly2)

return
$$\sum_{i=0}^{n_1} \sum_{j=0}^{n_2} (a_i \cdot b_j) x^{i+j}$$

Polynomial DIFFERENTIATE(poly1)

return
$$\sum_{i=1}^{n_1} i a_i v^{i-1}$$

4 New Operations of Polynomial Calculus ADT

Adding following additional operations will make polynomial calculus ADT useful. **structure** Polynomial

functions:
$$(\forall poly1 (= \sum_{i=0}^{n_1} a_i x^i), poly2 (= \sum_{i=0}^{n_2} b_i x^i) \in Polynomial, v \in \mathbb{R})$$

Polynomial **NEGATE**(poly1)
$$\triangleright$$
 Get a negated polynomial **return** $\sum_{i=0}^{n_1} (-a_i)x^i$

$$Polynomial \ \mathbf{SUBTRACT}(poly1,\ poly2) \qquad
ightharpoonup \ \mathrm{Subtract} \ \mathrm{two} \ \mathrm{polynomials} \ \mathbf{return} \ \mathrm{Add}(poly1,\ \mathrm{Negate}(poly2))$$

Polynomial INTEGRATE(poly1)
$$ightharpoonup$$
 Integrate a polynomial. $C=0$ return $\sum_{i=0}^{n_1} \frac{a_i}{i+1} x^{i+1}$

double SUBSTITUTE(poly1, v)
$$\triangleright$$
 Substitute x = v in a polynomial return $\sum_{i=0}^{n_1} a_i v^i$