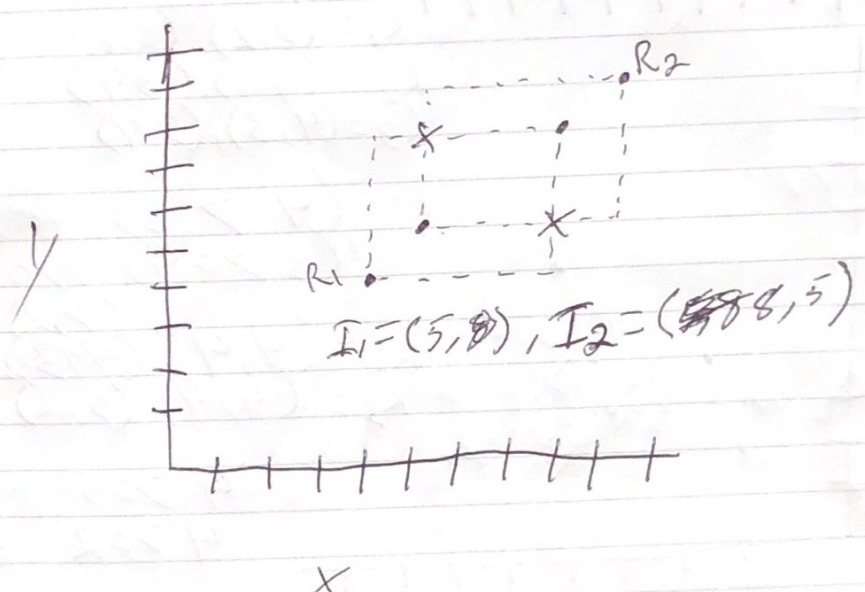


$(3, 4) = 14$
 $(4, 5) = 14$
 $(4, 6) = 14$
 $(5, 7) = 14$



$$R_1 = (x_1, y_1), (x_2, y_2) \quad R_2 = (x_3, y_3), (x_4, y_4)$$

$$\begin{aligned}
 x_5 &= 5 = \max(4, 5) \\
 y_5 &= 5 = \max(4, 5) \\
 x_6 &= 8 = \min(8, 9) \\
 y_6 &= 8 = \min(8, 9)
 \end{aligned}$$

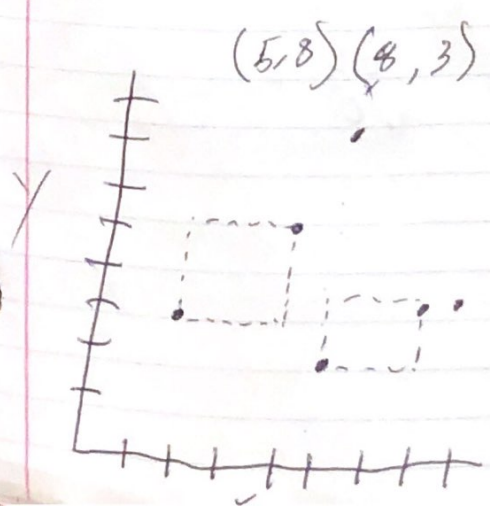
$$I_1 = x_5, y_5$$

$$R_3 = (x_5, y_5), (x_6, y_6)$$

$$\begin{aligned}
 I_1 &= (5, 8) \\
 I_2 &= (8, 5)
 \end{aligned}$$

Intersect

5 > 8 = No
5 > 8 = No



$$\begin{aligned}
 R_1 &= (2, 3), (4, 5) \\
 R_2 &= (5, 2), (7, 3) \\
 R_3 &= (5, 7), (2, 3)
 \end{aligned}$$

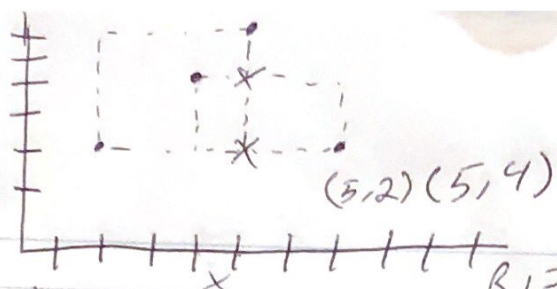
$$\begin{aligned}
 x_1 &= 5 \\
 y_1 &= 3 \\
 x_2 &= 4
 \end{aligned}$$

$$\begin{aligned}
 5 &= \max(2, 5) \\
 7 &= \max(4, 7) \\
 2 &= \min(3, 2) \\
 3 &= \min(5, 3)
 \end{aligned}$$

5 > 2 = Yes
7 > 3 = Yes

No Intersect

y



$$R_1 = (2,2), (5,6)$$

$$R_2 = (4,4), (7,2)$$

$$R_3 = (4,4), (5,2)$$

$$R_1 = (2,2), (5,6)$$

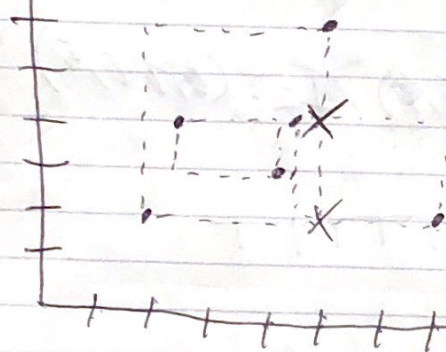
$$R_2 = (4,3), (3,4)$$

$$R_3 = (4,3), (3,4)$$

$$(4 > 3) \text{ yes}$$

$$!(3 > 4) \text{ no}$$

y



$$R_2 = (4,4), (7,2)$$

$$R_3 = (4,4), (5,2)$$

$$4 > 5 \text{ N}$$

$$4 > 2 \text{ Y}$$

$$R_1 = (2,2), (5,6) \quad x$$

$$R_2 = (3,4), (4,3)$$

$$R_3 = (3,4), (4,3)$$

$$\max(2,3) = 3$$

$$\max(2,4) = 4$$

$$\min(5,4) = 4$$

$$\min(6,3) = 3$$

$$3 > 4 = \text{No}$$

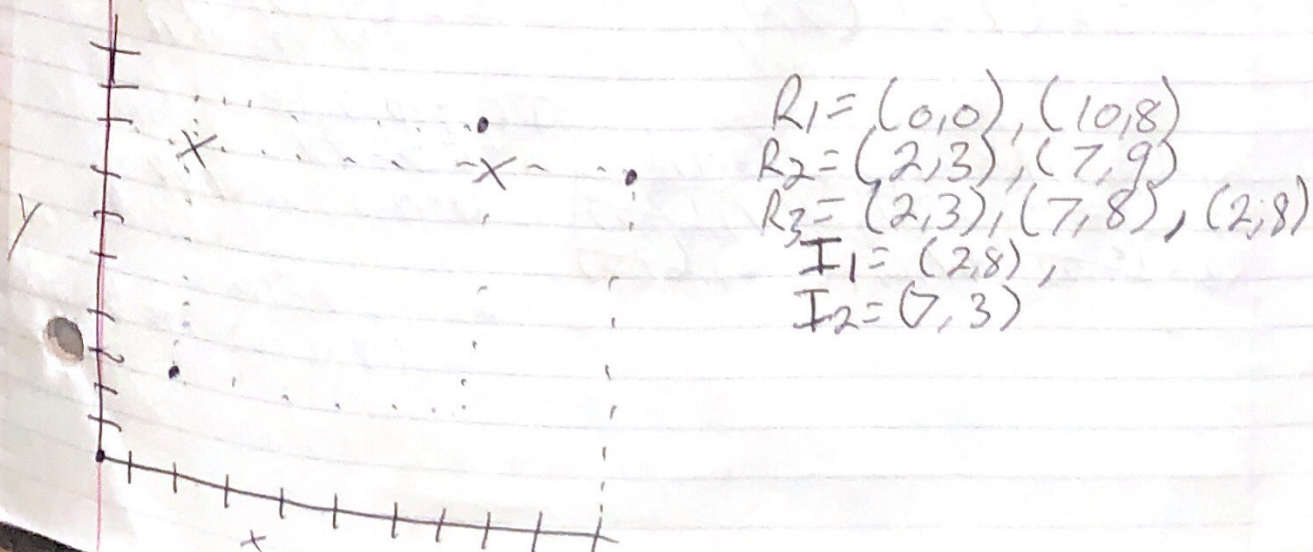
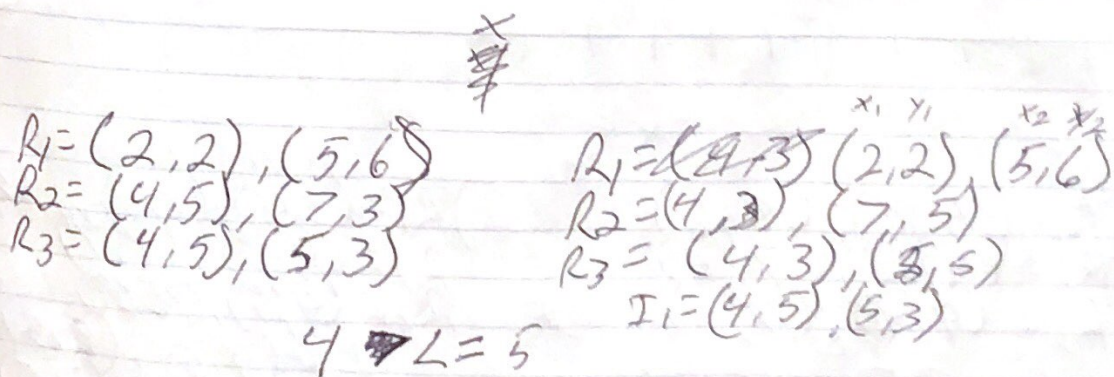
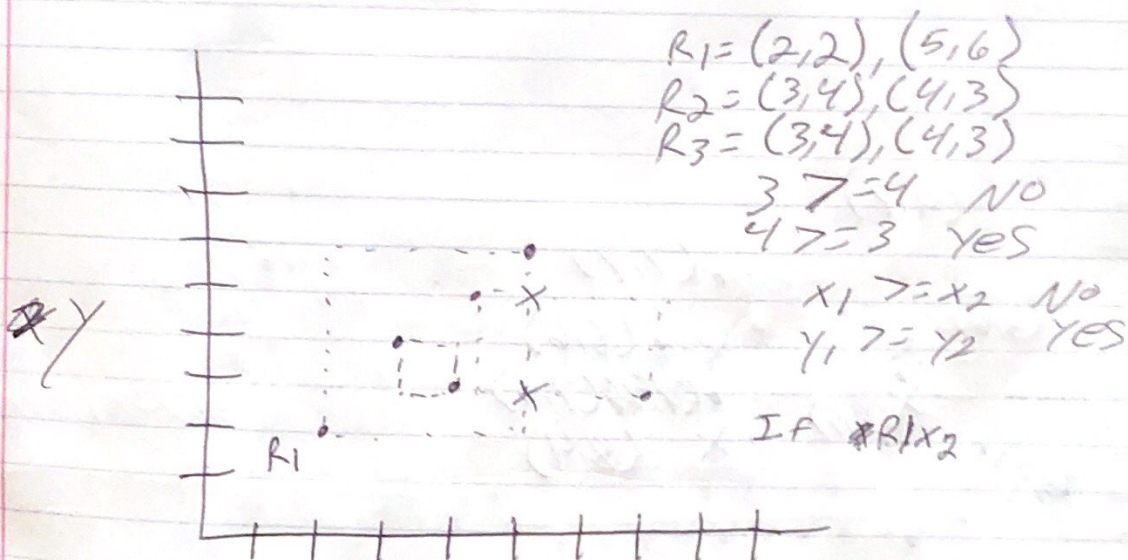
$$4 > 3 = \text{Yes}$$

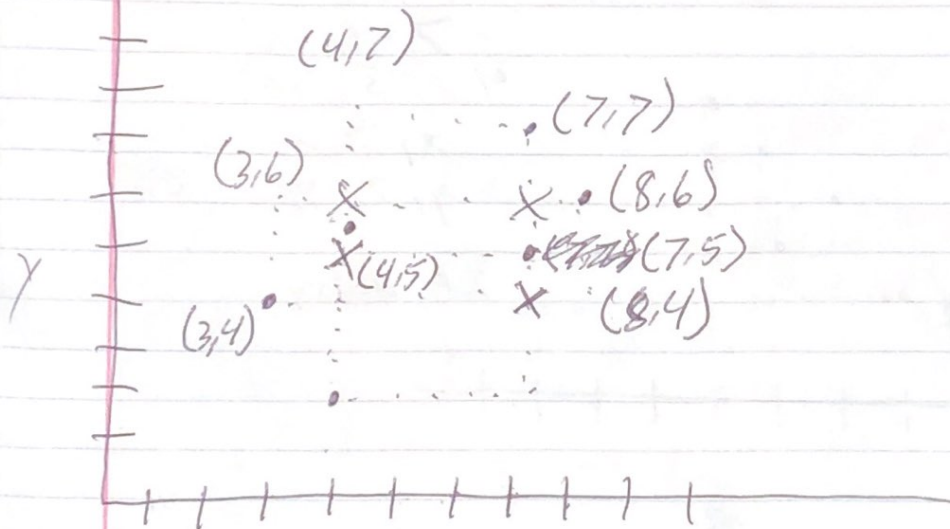
$$!(x_5 \geq x_6) \text{ containment}$$

$$!(y_5 \geq y_6)$$

$$4 > 3 \text{ yes}$$

$$3 > 4 \text{ no}$$





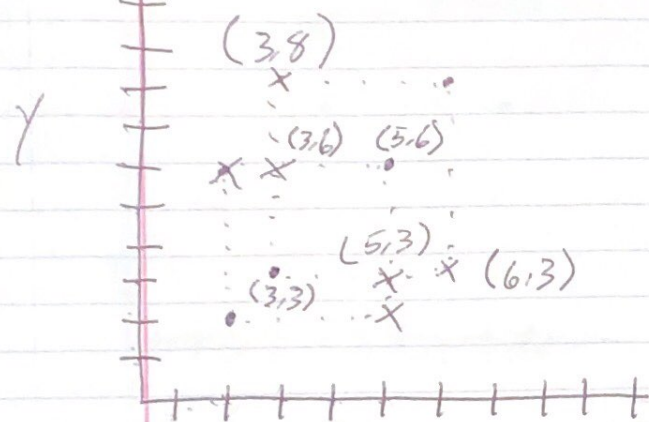
$$\begin{aligned}
 1) \quad R_1 &= (3,4), (8,6) \\
 R_2 &= (4,2), (7,5) \\
 R_3 &= (4,4), (7,5) \\
 I &= (4,5), (7,4)
 \end{aligned}$$

$$\begin{aligned}
 2) \quad R_1 &= (x_1, y_1), (x_2, y_2) = (3,4), (8,6) \\
 R_2 &= (x_3, y_3), (x_4, y_4) = (4,2), (7,5) \\
 R_3 &= (x_5, y_5), (x_6, y_6) = (4,5), (7,5) \\
 I &= (x_7, y_7), (x_8, y_8) = (4,5), (7,4)
 \end{aligned}$$

$$\begin{aligned}
 R_1 &= (3,4), (8,6), (3,6), (8,4) \\
 R_2 &= (4,5), (7,7), (4,7), (7,5) \\
 R_3 &= (4,5), (7,6), (4,6), (7,5)
 \end{aligned}$$

If top side
 $y_5 \geq y_7$
 (x_5, y_5) else (x_7, y_7)

$x_6 \geq x_8$
 (x_6, y_6) else (x_8, y_8)

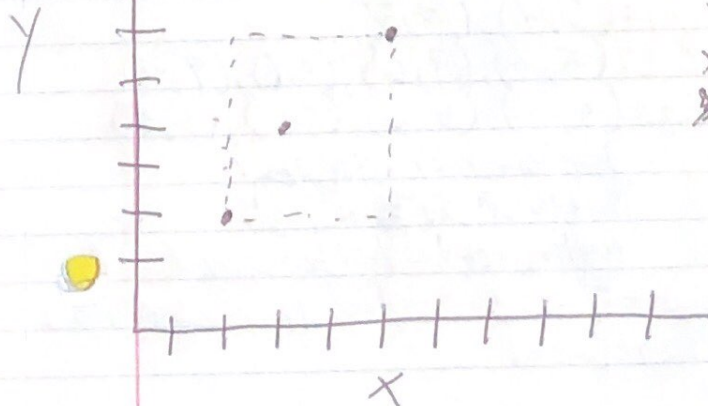


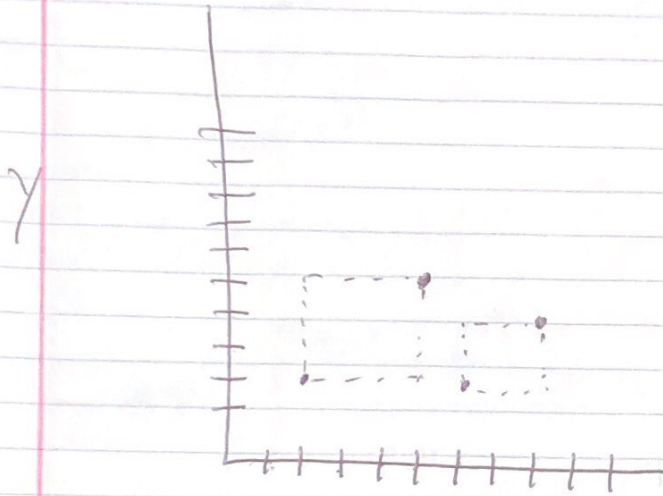
$$\begin{aligned}
 R_1 &= (2,2), (5,6), \boxed{(2,6), (5,2)} \\
 R_2 &= (3,3), (6,8), (3,8), (6,3) \\
 R_3 &= (3,3), (5,6), (3,6), (5,3) \\
 I &= (3,6), (5,3)
 \end{aligned}$$

$$\begin{aligned}
 R_1 &= \overset{p_1 p_1}{(2,2)}, \overset{p_2 p_2}{(5,6)}, \overset{p_2 p_1}{(2,6)}, \overset{p_1 p_2}{(5,2)} \\
 R_2 &= (3,4), (4,3), (3,3),
 \end{aligned}$$

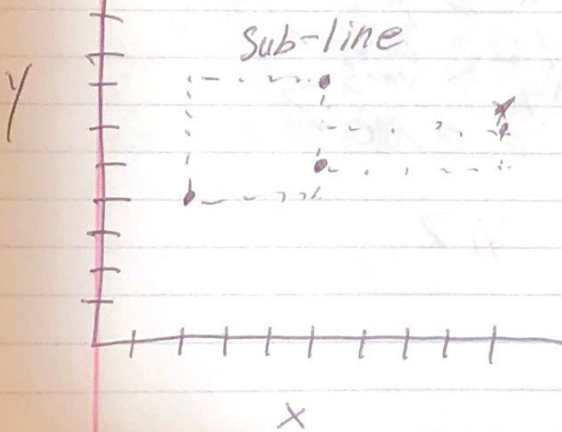
$$\begin{aligned}
 &\overset{p_3 p_3}{x_1} < \overset{p_4 p_4}{x_2} \rightarrow \text{yes} > \text{yes} \\
 &\overset{p_3 p_3}{y_1} < \overset{p_4 p_4}{y_2} \rightarrow \text{yes} > \text{yes} \\
 &\overset{p_3 p_3}{x_3} < \overset{p_4 p_4}{x_4} \rightarrow \text{yes} > \text{yes} \\
 &\overset{p_3 p_3}{y_3} < \overset{p_4 p_4}{y_4} \rightarrow \text{NO} >
 \end{aligned}$$

7.7.





$$\begin{array}{lcl}
 & p_1 & p_2^x \\
 R_1 = & (2, 2), (5, 5) & p_{1y} < p_{4y} \\
 R_2 = & (6, 2), (8, 4) & \\
 R_3 = & (6, 2), (5, 4) & \\
 & 6 > 5 & x_5 > x_6 \\
 & 2 < 4 & y_5 < y_6
 \end{array}$$



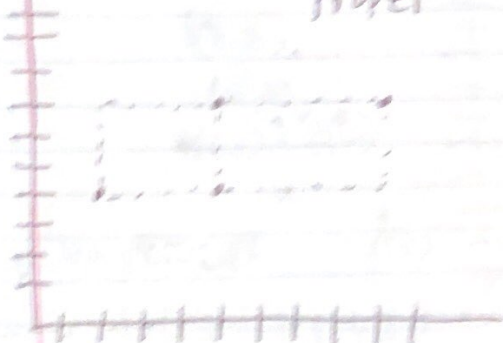
$$\begin{array}{l}
 R_1 = (2, 4), (5, 7) \\
 R_2 = (5, 5), (9, 6), (5, 8), (9, 5) \\
 R_3 = (5, 6), (5, 6), (5, 6), (5, 6)
 \end{array}$$

$$\begin{array}{l}
 \text{bottom-left} = \text{top-left} \\
 \text{bottom-right} = \text{top-right} \\
 \text{bottom-left} = \text{bottom-right}
 \end{array}$$

$$\begin{array}{l}
 R_1 = 7 - 4 = 3 \quad \text{top-left} = \text{top-right} \\
 R_2 = 6 - 5 = 1
 \end{array}$$

y

proper



x

$$R_1 = (2,4), (5,7), (2,7), (5,4)$$

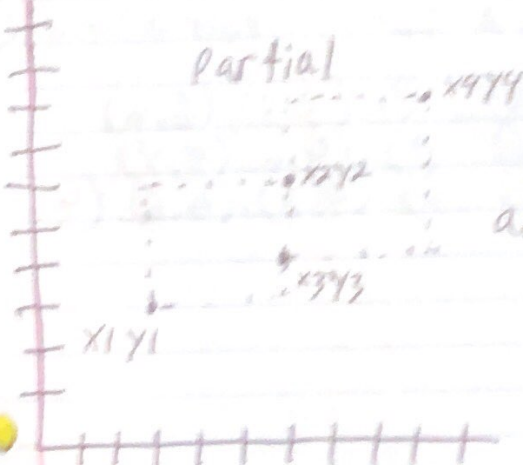
$$R_2 = (5,4), (9,7), (5,7), (9,4)$$

$$R_3 = (5,4), (5,7), (5,7), (5,4)$$

~~bottom-left = top-left~~ \rightarrow adjacent
~~bottom-right = top-right~~

y

partial



x

$$R_1 = (3,3), (6,6), (3,6), (6,3)$$

$$R_2 = (6,4), (9,8), (6,8), (9,4)$$

$$R_3 = (6,4), (6,6), (6,6), (6,4)$$

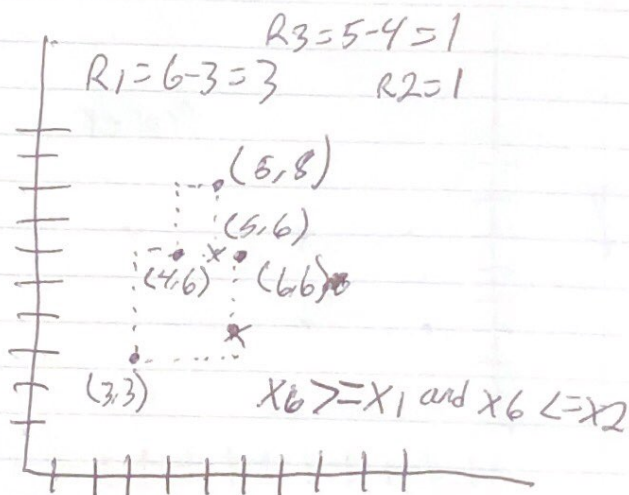
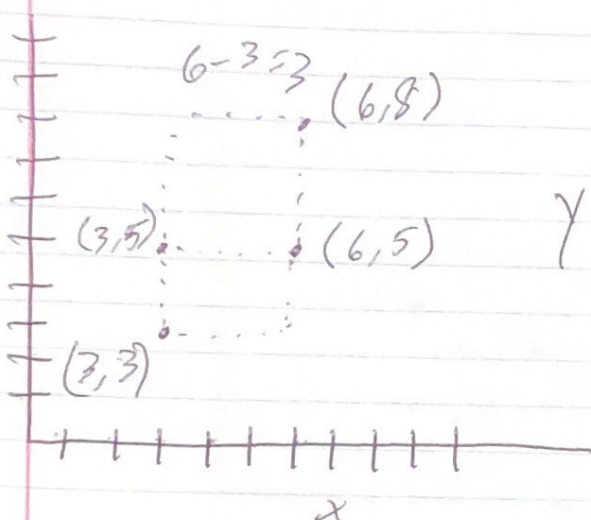
adjacent \angle ~~bottom-left = top-left~~
~~bottom-right = top-right~~

$$R_1 = 6-3 = 3$$

$$R_2 = 8-4 = 4$$

$$R_3 = 6-4 = 2$$

$$\boxed{y_4 > y_2 \wedge y_2 > y_3 \wedge y_3 > y_1}$$



$R_1 = (3,3), (6,5), (3,5), (6,3)$
 $R_2 = (3,5), (6,8), (3,8), (6,5)$
 $R_3 = (3,5), (6,5), (3,5), (6,5)$

$x_3 \geq x_1$ and $x_4 \leq x_2$

$\text{bottom_left} = \text{bottom_right}$ $\text{bottom_left} = \text{top_left}$
 $\text{top_left} = \text{top_right}$ $\text{bottom_right} = \text{top_right}$

$x_6 - x_5 = x_4 - x_3 = x_2 - x_1 = \text{proper} \rightarrow \text{Top} \leftrightarrow \text{Bottom}$
 $y_6 - y_5 = y_4 - y_3 = y_2 - y_1 = \text{proper} \rightarrow \text{left} \leftrightarrow \text{right}$

~~$R_1 = (3,3), (6,6), (3,6), (6,3)$~~
 ~~$R_2 = (4,6), (7,8), (4,8), (8,6)$~~
 ~~$R_3 = (4,6), (6,6), (4,6), (6,6)$~~

$R_1 = (3,3), (6,6)$
 $R_2 = (4,6), (5,8)$
 $R_3 = (4,6), (5,6), (4,6), (5,6)$

y



x

$$\begin{aligned} R_1 &= (2, 3), (5, 6) \\ R_2 &= (4, 3), (6, 4) \\ R_3 &= (4, 3), (5, 4) \end{aligned}$$