Basic Approaches for Missing Values





Basic Approaches for Missing Values

We will now discuss a few simple approaches to deal with missing values

We will use partially synthetic data

- We will focus on specific (and mosly intact) sections of our series
- The we will remove values artificially
- ...And measure the accuracy of our filling approaches via the Root MSE

$$RMSE = \sqrt{\frac{1}{n} \sum_{i=0}^{n} (x_i - \hat{x}_i)^2}$$

Where x_i is a value from the filled series and \hat{x}_i the ground truth

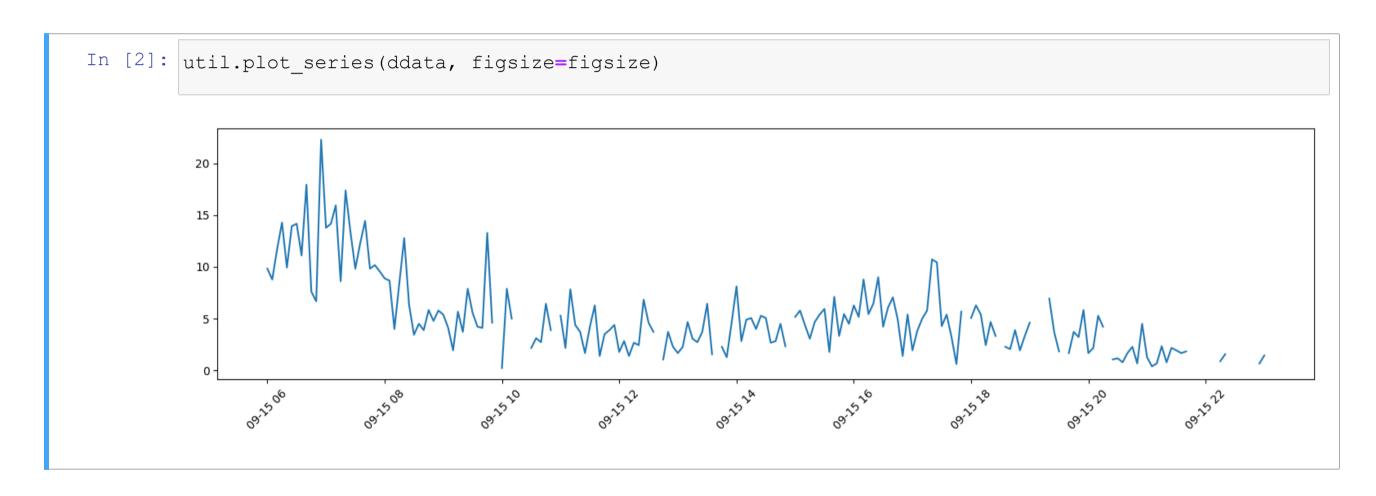
- $\mathbf{x}_i = \hat{x}_i$ if no value is missing
- Hence, any MSE difference is entirely due to missing values





The Benchmark Dataset

Our benchmark dataset will consist of this particular stretch from our traffic series



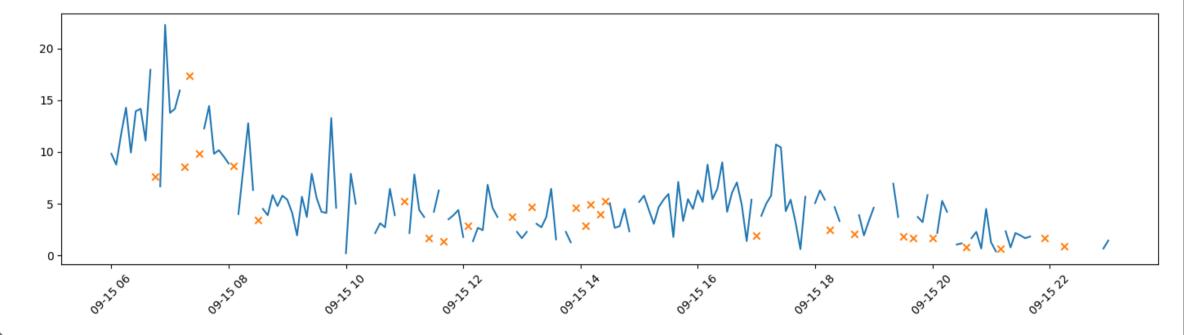
- There are (comparatively) few missing values
- Some of them are isolated, some for contiguous "holes"

The Benchmark Dataset

We now introduce some missing values

...By drawing them at random:

```
In [3]: np.random.seed(42) # seed (to get reproducible results)
    mv_idx = np.random.choice(range(len(ddata.index)), size=30, replace=False)
    ddata_mv = ddata.copy()
    ddata_mv.iloc[mv_idx] = np.NaN
    util.plot_series(ddata_mv, figsize=figsize)
    plt.scatter(ddata.index[mv_idx], ddata.iloc[mv_idx], color='tab:orange', marker='x');
```







Forward/Backward Filling

The easiest approach for missing values consists in replicating nearby observations

- Forward filling: propagate forward the last valid observation
- Backward filling: propagate backward the next valid observation

An important observation:

- When filling missing values, we have access to the whole series
- ...So we can reason both forward and backward

Forward/backward filling are simple methods, but they can work well

- Rationale: most time series have a certain "inertia"
- ...I.e.: a strong level of local correlation
- For this reason (e.g.) the last observation is often a good predictor for the next





Forward/Backward Filling

Forward and backward filling are pre-implemented in pandas

They are available through the fillna method:

```
DataFrame.fillna(..., method=None, ...)
```

- fillna replaces NaN Values in a DataFrame Or Series
- The method parameter can take the values:
 - "pad" or "ffill": these correspond to forward filling
 - "backfill" or "bfill": these correspond to backward filling

They are generally applied to datasets with a dense index

■ Remember that our benchmark dataset already has a dense index





Forward/Backward Filling on the Benchmark

We can finally test forward/backward filling

```
In [4]: nan_mask = ddata['value'].isnull()
    ffseries = ddata_mv.fillna(method='ffill')
    ffseries[nan_mask] = np.NaN # We empty the values that were originally empty
    bfseries = ddata_mv.fillna(method='bfill')
    bfseries[nan_mask] = np.NaN # We empty the values that were originally empty
```

We can check the corresponding RMSE:

```
In [6]: rmse_ff = np.sqrt(mean_squared_error(ddata[~nan_mask], ffseries[~nan_mask]))
    rmse_bf = np.sqrt(mean_squared_error(ddata[~nan_mask], bfseries[~nan_mask]))
    print(f'RMSE for forwad filling: {rmse_ff:.2f}, for backward filling {rmse_bf:.2f}')
RMSE for forwad filling: 1.33, for backward filling 0.87
```

- In this case backward filling seems to work better
- The results are of course application-dependent





Forward/Backward Filling on the Benchmark

Let's have a close look at the results for forward filling

```
In [16]: util.plot series(ffseries, figsize=figsize)
         plt.scatter(ddata.index[mv idx], ddata.iloc[mv idx], color='tab:orange', marker='x');
         plt.scatter(ddata.index[mv_idx], ffseries.iloc[mv_idx], color='tab:red', marker='x');
          20
          15
          10
```

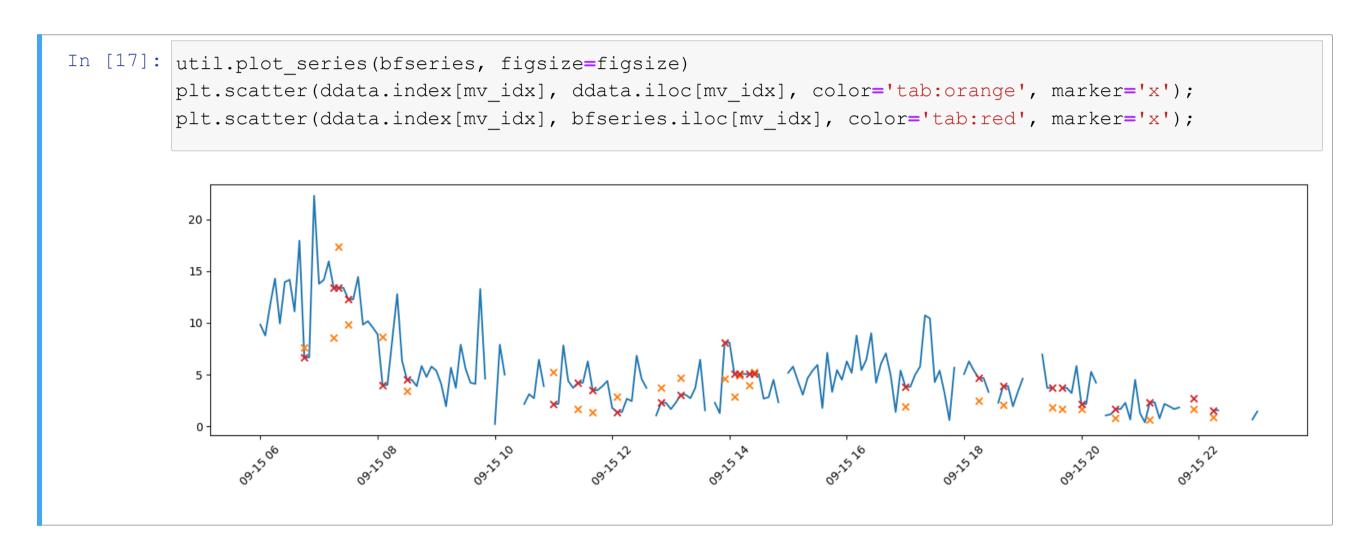
■ The red marks represent the values that have been filled





Forward/Backward Filling on the Benchmark

Let's have a close look at the results for backward filling



- Forward/backward filling tend to work well for low variance sections
- ...And conversely work worse for high variance sections

(Geometric) Interpolation

A few more options are available via the interpolate method

```
DataFrame/Series.interpolate(method='linear', ...)
```

The method parameter determines how NaNs are filled:

- "linear" uses a linear interpolation, assuming uniformly spaced samples
- "time" uses a linear interpolation, but supports non-uniformly spaced samples
- "nearest" uses the closest value
- "polynomial" uses a polynomial interpolation
- Even "ffill" and "bfill" are available

Both "polynomial" and "spline" require to specify the additional parameter order

■ E.g. df.interpolate(method='polynomial', order='3')





(Geometric) Interpolation

Let us check the performance of some approaches

- "linear" and "time" are equivalent (we have uniformly-spaced samples)
- "polynomial" is the most complex, and in this case also the worst

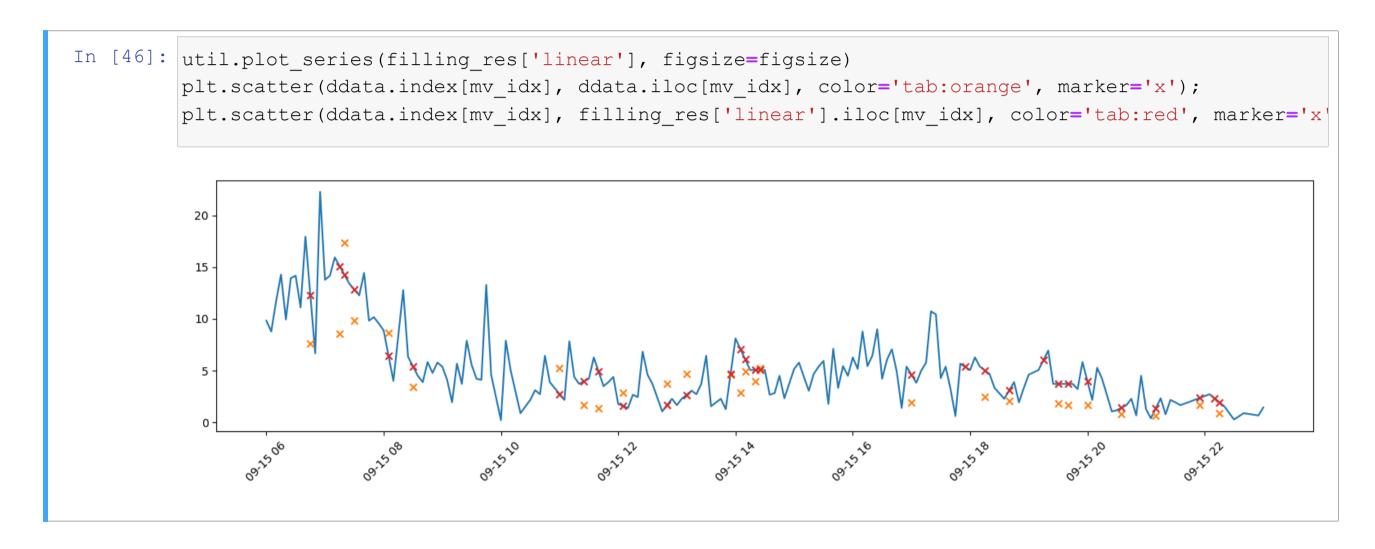
All perform worse than backward filling (at least in this case)!





Linear Filling on the Benchmark

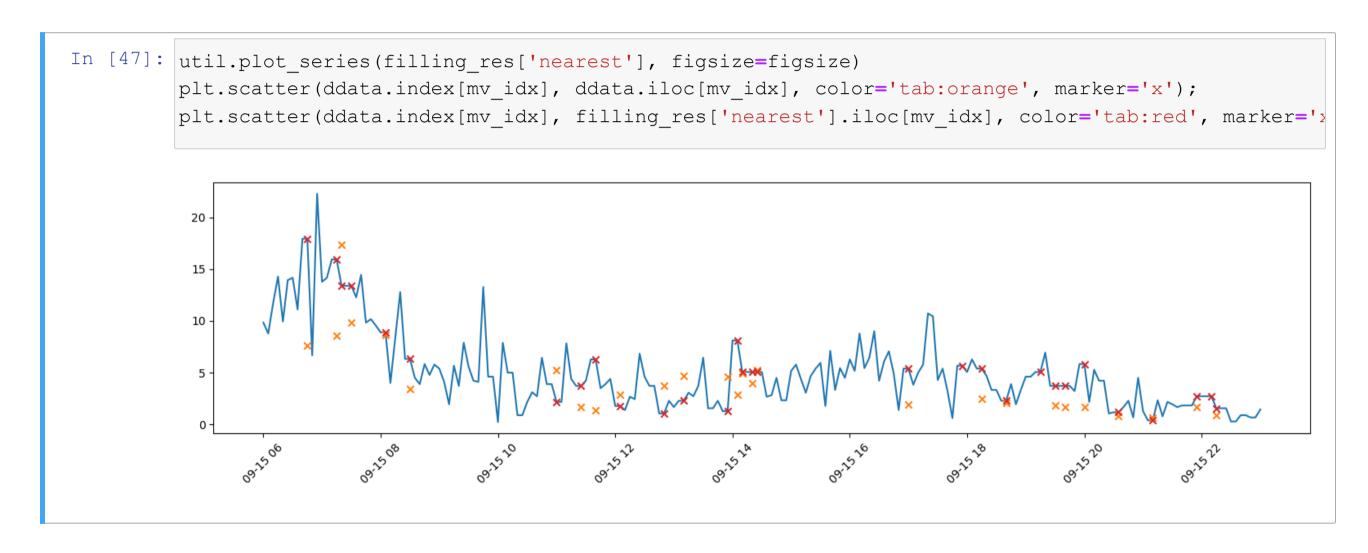
Let's have a close look at the results for linear filling



- Linear filling works well for series with slower dynamics
- ...Rut does not work well for series that faster dynamics

Nearest Filling on the Benchmark

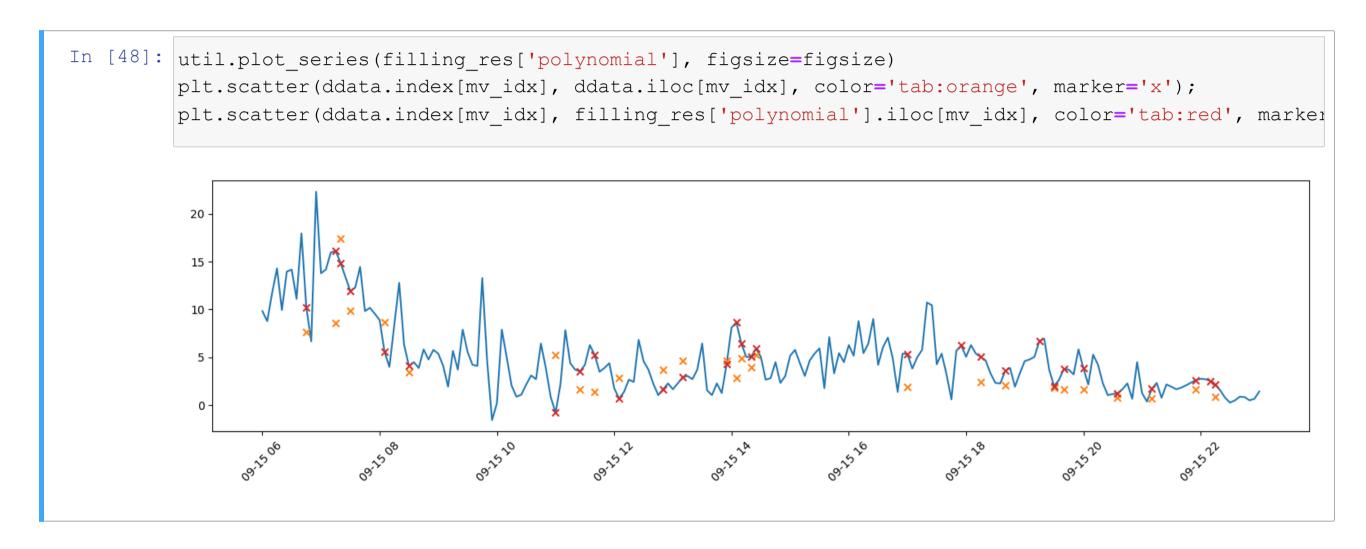
Let's have a close look at the results for nearest filling



- Nearest filling is a compromise between forward and backward filling
- ...And in our case its performance is the average of the two

Polynomial Filling on the Benchmark

Let's have a close look at the results for polynomial filling

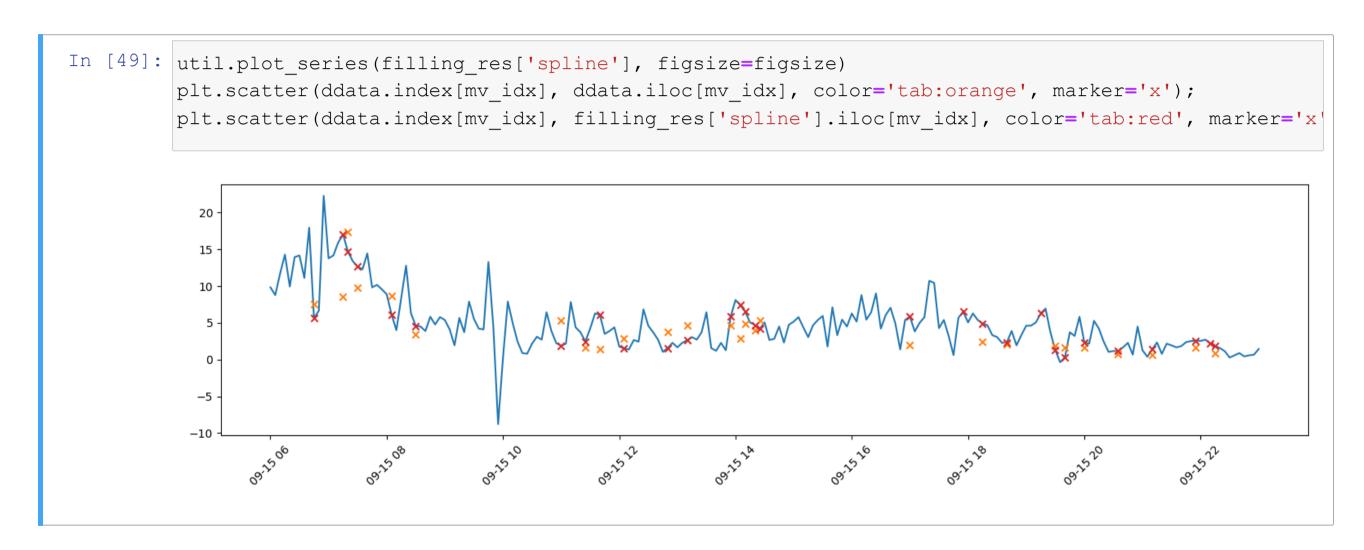


Polynomial interpolation relies in nearby value to fit a polynomial



Spline Filling on the Benchmark

Let's have a close look at the results for spline filling



- Spline interpolation relies on <u>piecewise polynomial curves</u>
- ...And it's often more robust than polynomial interpolation

How do we choose which method is best? Is the (R)MSE enough?



