

## Challenge 7 – Context Free Languages (CFLs) and Context Free Grammars (CFGs)

Consider the language defined by  $L_1 = \{a^i b^j \mid i \neq j\}$  and the following CFG grammar  $G$ :

$S \rightarrow CA \mid AE$

$A \rightarrow aAb \mid \varepsilon$

$C \rightarrow aD$

$D \rightarrow aD \mid \varepsilon$

$E \rightarrow bF$

$F \rightarrow bF \mid \varepsilon$

- (a) Is  $L(G) = L_1$ ? If so, prove by induction the following statement: if  $w \in L(G)$  then  $w \in L_1$
- (b) Is the prove of the previous statement enough to prove  $L(G) = L_1$ ? Justify your answer.