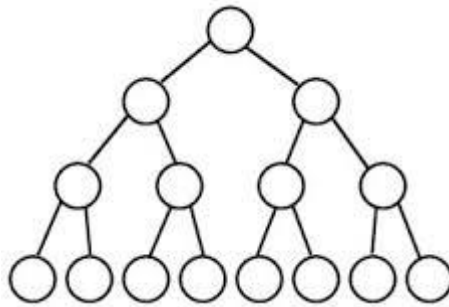


## Challenge 1 – Proof by Induction

Prove by induction that the number of levels of a perfect binary tree<sup>1</sup> is  $\log_2(n+1)$ , where  $n$  is the number of nodes of the tree.



*Figure 1. Example of a perfect binary tree (this one with 15 nodes and with 4 levels).*

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<sup>1</sup> Assume that in a perfect binary tree all the internal nodes (i.e., all the nodes except the leaves) of the tree have two children (all the leaves are at the same level).