Credit Risk: Coursework Dependence

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Coursework: Introduction

- The aim of the coursework is to get familiar with dependence modeling. It is recommended that you read the slides of Lectures 2 and 3 before you do the coursework.
- The results can be obtained using Python, matlab, R or other software packages.
- The results should be uploaded on the blackboard no later than 14 July 2020.
- Please make sure the answers are to-the-point and concise. The results should be summarised on no more than 2 pages.



Simulation Study of Gaussian and t-copula

Exercise: Populate the table below with default probabilities (in percent, 2 decimals).

	Gaussian copula $(ho=)$			Student t-copula $(ho=)$		
	0%	20%	40%	0%	20%	40%
$P(D \ge 9, \tau \le 1y)$						
$P(D \ge 11, \tau \le 1y)$						
$P(D \ge 14, \tau \le 1y)$						
$P(D=0, \tau > 1.5y)$						
$P(D=0, \tau > 2.5y)$						
$P(D=0, \tau > 3.5y)$						

Discuss the results in the table.

0 default in first 3.5y



Simulation Study of Gaussian and t-copula

- The number of assets in the portfolio equals 30,
- $P(D \ge 9, \tau \le 1y)$: the probability of 9 or more defaults within the first year,
- $P(D=0, \tau > 2.5y)$: the probability of zero defaults within the first 2.5 years,
- Number of simulations = 250,000,
- Columns 2, 3 and 4 (5, 6 and 7) should have the results using a Gaussian copula framework (Student t-copula framework).



Gaussian Copula Framework

- Generate $X_1, X_2,...$ and X_{30} which are jointly normal distributed variables with means zero, standard deviations one and correlation 0%, 20% and 40%, respectively.
- Use Cholesky decomposition: $\Gamma\Gamma' = \sum$

$$X \sim N(0, I)$$
 and $\Gamma X \sim N(0, \Gamma \Gamma')$

- Let $U_i = \Phi(X_i)$ where Φ is the univariate cumulative normal distribution function.
- Calculate the default times (τ) using the following assumptions for the $\lambda = 10\%$.



Student-t Copula Framework

- Generate X_1 , X_2 ,... and X_{30} which are jointly Student t distributed variables with correlation 0%, 20% and 40%, respectively, and degrees of freedom $\nu = 4$.
- Let $U_i = t_{\nu}(X_i)$ where t_{ν} is the univariate cumulative Student t distribution function.
- Calculate the default times (τ) using the following assumptions for the $\lambda=10\%$.
- Compare your results to those of the Gaussian Copula framework.
- How do you use the above techniques to value CDO tranches?
- How do you use the above techniques to value an n-to-default?