

Static Program Analysis

Yue Li and Tian Tan



2020 Spring

Static Program Analysis

Intermediate Representation

Nanjing University

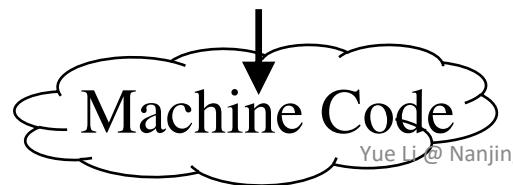
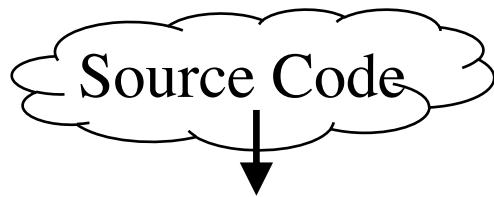
Yue Li

2020

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7. Control Flow Graphs (CFG)

Compiler



Compiler

Source Code

Scanner

Tokens

Lexical Analysis

You ↗ goouojd

Regular
Expression

Machine Code

Compiler

Tokens

AST

Source Code

Scanner

Parser

Lexical Analysis

You ↗ goouojd

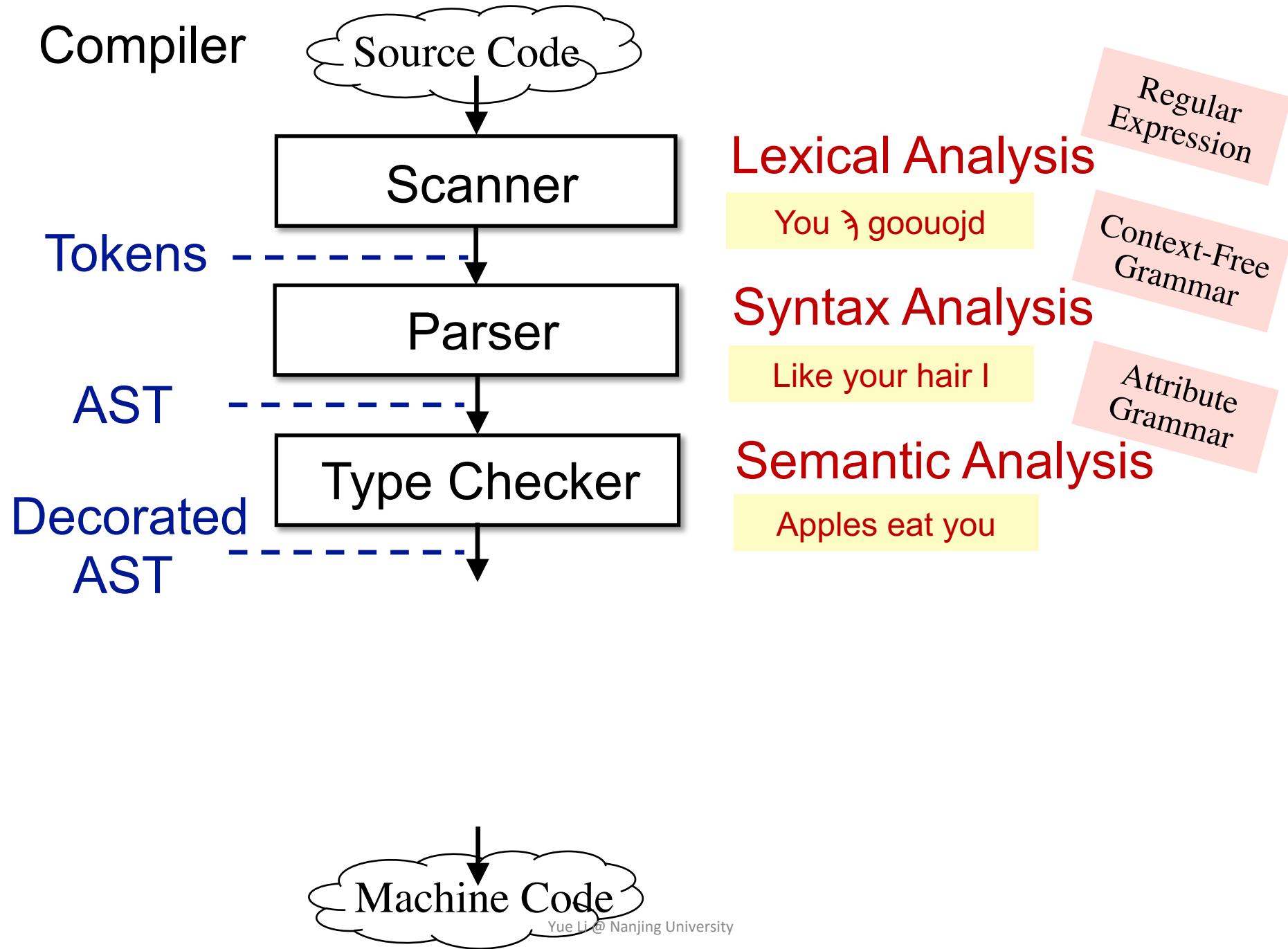
Regular
Expression

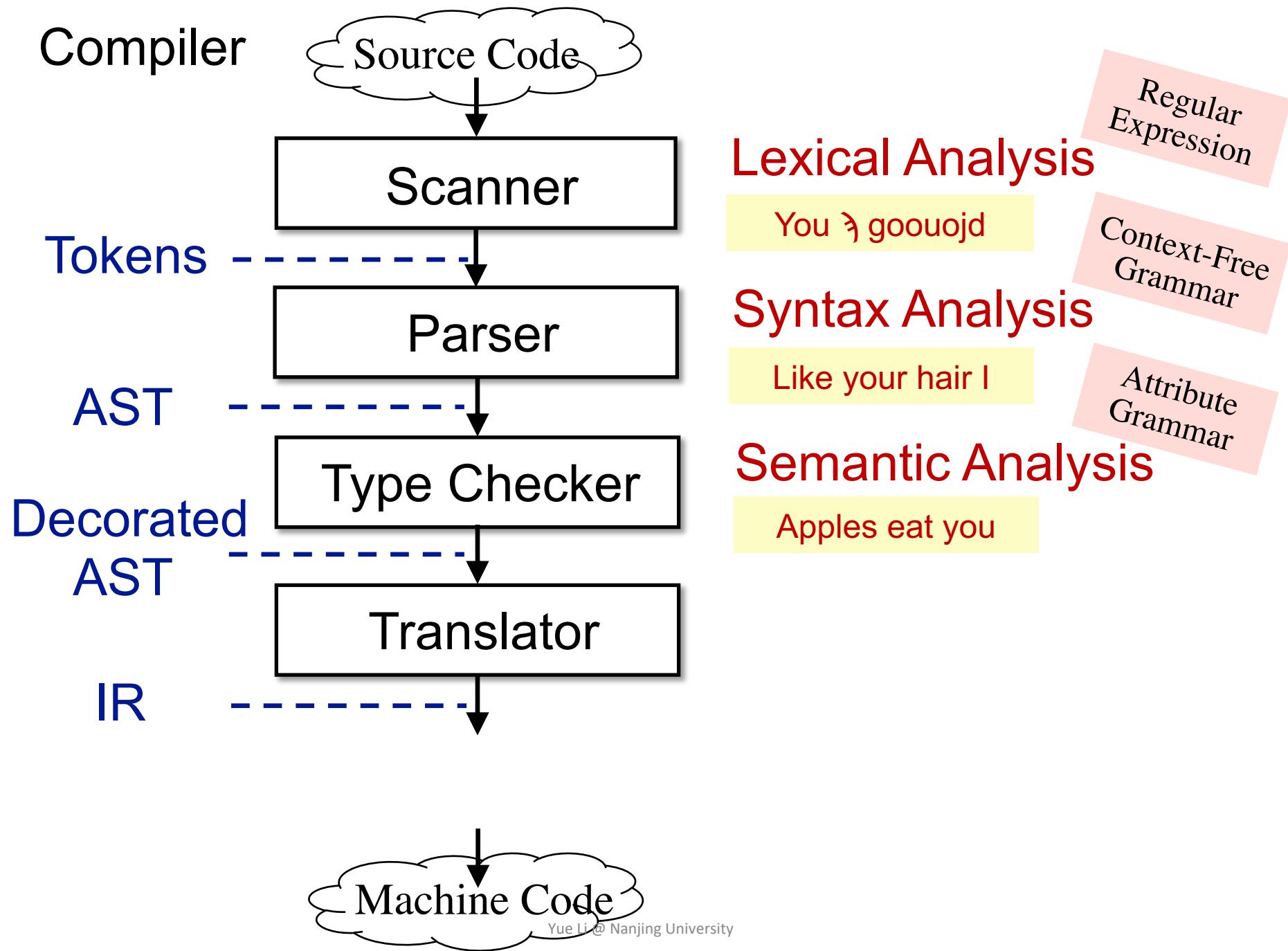
Syntax Analysis

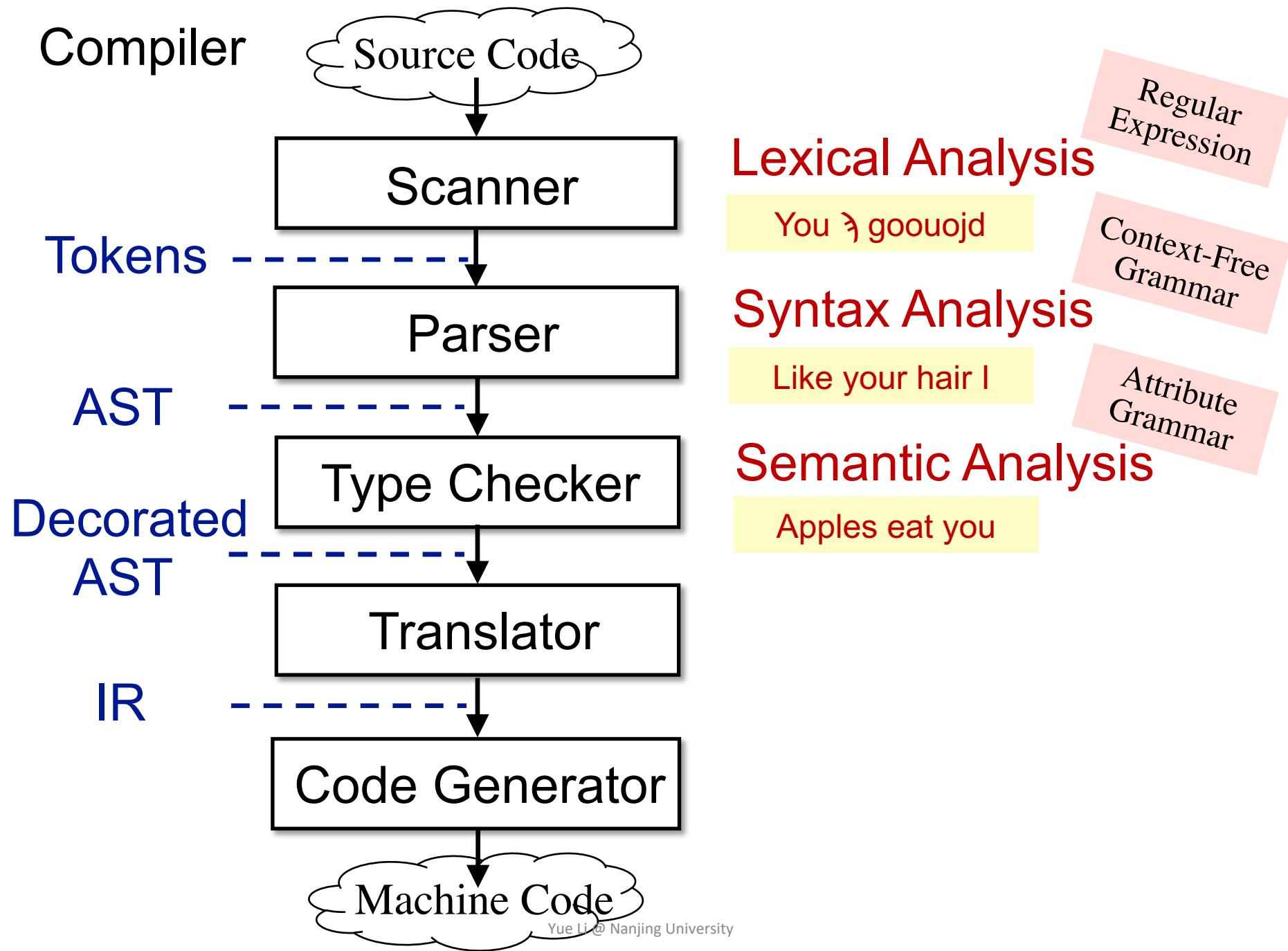
Like your hair !

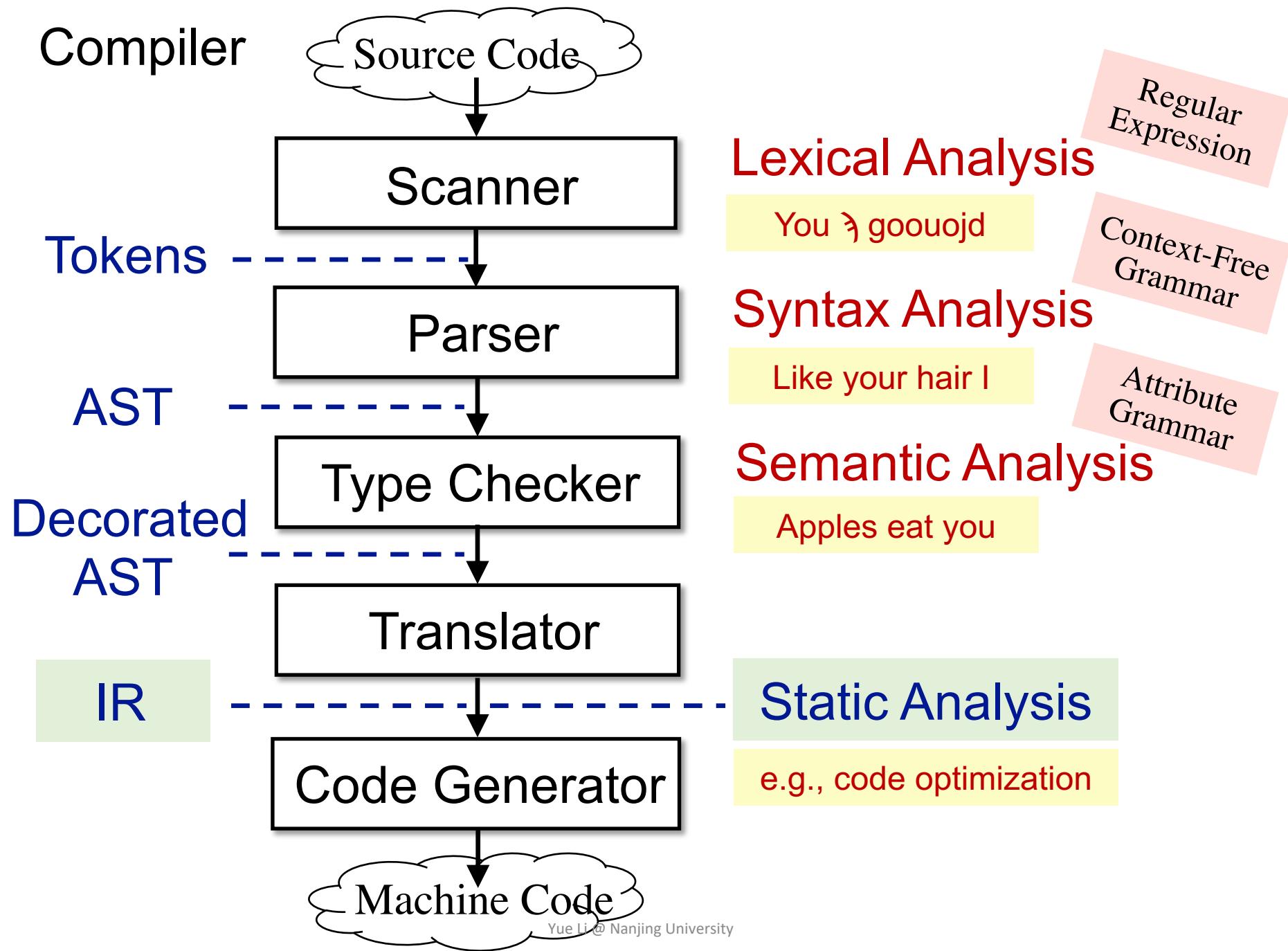
Context-Free
Grammar

Machine Code

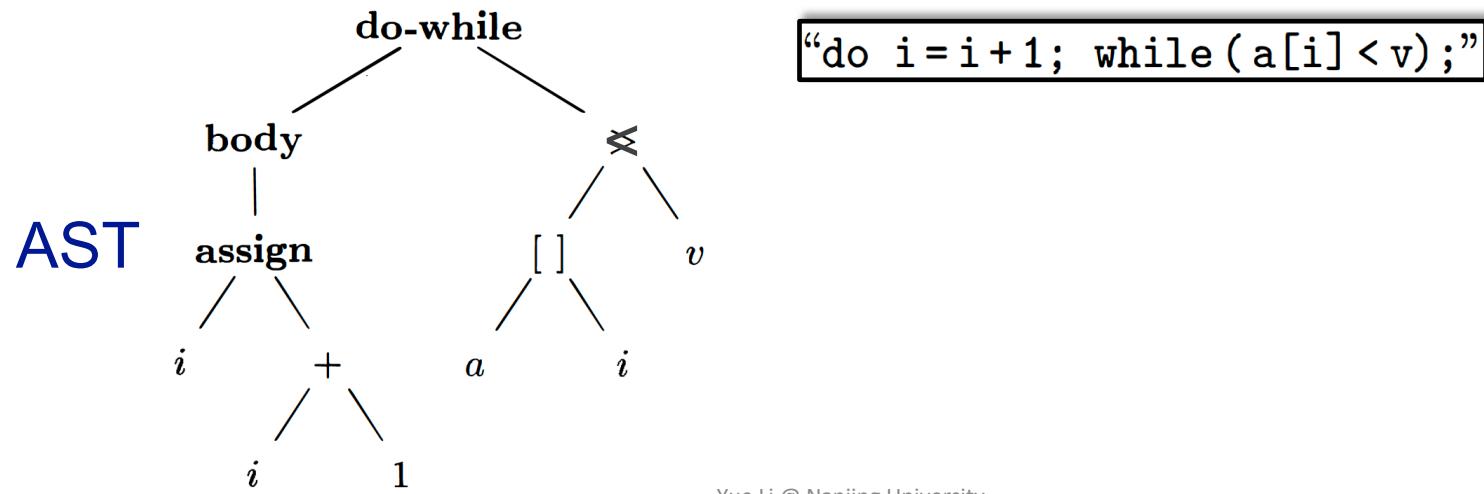






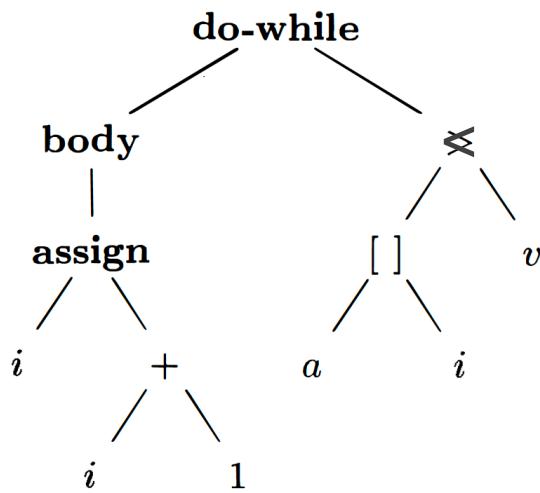


AST vs. IR



AST vs. IR

AST



“do i = i + 1; while (a[i] < v);”

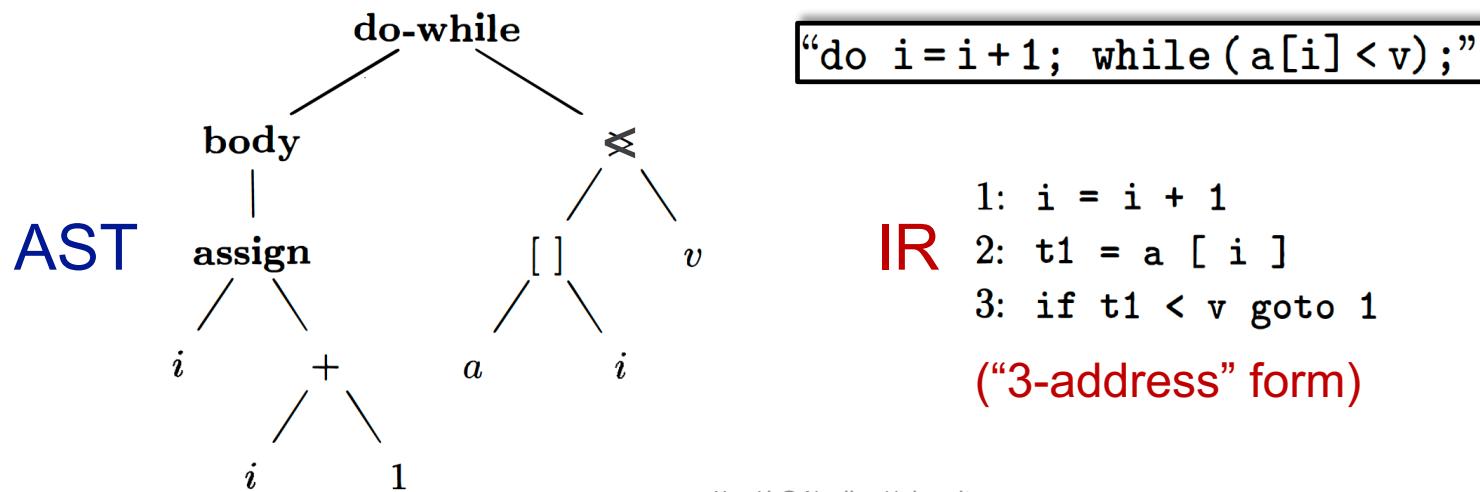
IR

1: `i = i + 1`
2: `t1 = a [i]`
3: `if t1 < v goto 1`
(“3-address” form)

AST vs. IR

- high-level and closed to grammar structure
- usually language dependent
- suitable for fast type checking
- lack of control flow information

- low-level and closed to machine code
- usually language independent
- compact and uniform
- contains control flow information
- usually considered as the basis for static analysis



Intermediate Representation (IR)

- 3-Address Code (3AC)

There is at most one operator on the right side of an instruction.

$$t2 = a + b + 3 \quad \Rightarrow \quad \begin{array}{l} t1 = a + b \\ t2 = t1 + 3 \end{array}$$

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Why called 3-address?

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Why called 3-address?

Address can be one of the following:

- Name: a, b
- Constant: 3
- Compiler-generated temporary: t1, t2

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There is at most one operator on the right side of an instruction.

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Why called 3-address?

Address can be one of the following:

- Name: a, b
- Constant: 3
- Compiler-generated temporary: t1, t2

Each type of instructions has its own 3AC form

Some Common 3AC Forms

- $x = y \ bop\ z$
x, y, z: addresses
bop: binary arithmetic or logical operation
- $x = uop\ y$
uop: unary operation (minus, negation, casting)
- $x = y$
L: a label to represent a program location
- goto *L*
rop: relational operator ($>$, $<$, $==$, \geq , \leq , etc.)
goto L: unconditional jump
- if x goto *L*
if ... goto L: conditional jump
- if x *rop* y goto *L*

Some Common 3AC Forms

- $x = y \ bop\ z$
 - $x = uop\ y$
 - $x = y$
 - goto L
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L: a label to represent a program location
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goto L: unconditional jump
if ... goto L: conditional jump

Let's see some more real-world complicated forms

Soot and Its IR: Jimple

- Soot

Most popular static analysis framework for Java

<https://github.com/Sable/soot>

<https://github.com/Sable/soot/wiki/Tutorials>

Soot's IR is Jimple: typed 3-address code

```
package nju.sa.examples;
public class DoWhileLoop3AC {
    public static void main(String[] args) {
        int[] arr = new int[10];
        int i = 0;
        do {
            i = i + 1;
        } while (arr[i] < 10);
    }
}
```

Java Src

Do-While Loop

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package nju.sa.examples;
public class DoWhileLoop3AC {
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}
```

Java Src

Do-While Loop

```
public static void main(java.lang.String[])
{
    java.lang.String[] r0;
    int[] r1;
    int $i0, i1;

    r0 := @parameter0: java.lang.String[];
    r1 = newarray (int)[10];
    i1 = 0;

    label1:
    i1 = i1 + 1;
    $i0 = r1[i1];
    if $i0 < 10 goto label1;

    return;
}
```

```
package nju.sa.examples;
public class MethodCall3AC {

    String foo(String para1, String para2) {
        return para1 + " " + para2;
    }

    public static void main(String[] args) {
        MethodCall3AC mc = new MethodCall3AC();
        String result = mc.foo("hello", "world");
    }
}
```

Java Src



```

java.lang.String foo(java.lang.String, java.lang.String)
{
    nju.sa.examples.MethodCall3AC r0;
    java.lang.String r1, r2, $r7;
    java.lang.StringBuilder $r3, $r4, $r5, $r6;

    r0 := @this: nju.sa.examples.MethodCall3AC;

    r1 := @parameter0: java.lang.String;

    r2 := @parameter1: java.lang.String;

    $r3 = new java.lang.StringBuilder;

    specialinvoke $r3.<java.lang.StringBuilder: void <init>()>();

    $r4 = virtualinvoke $r3.<java.lang.StringBuilder: java.lang.StringBuilder append(java.lang.String)>(r1);

    $r5 = virtualinvoke $r4.<java.lang.StringBuilder: java.lang.StringBuilder append(java.lang.String)>(" ");

    $r6 = virtualinvoke $r5.<java.lang.StringBuilder: java.lang.StringBuilder append(java.lang.String)>(r2);

    $r7 = virtualinvoke $r6.<java.lang.StringBuilder: java.lang.String toString()>();

    return $r7;
}

```

```

package nju.sa.examples;
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```

Java Src



```
public static void main(java.lang.String[])
{
    java.lang.String[] r0;
    nju.sa.examples.MethodCall3AC $r3;

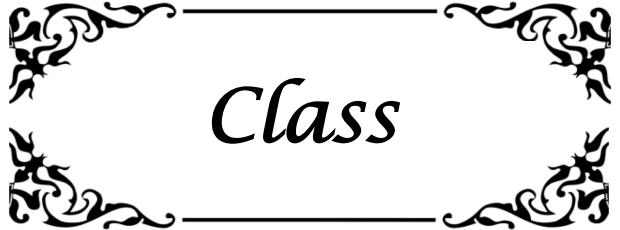
    r0 := @parameter0: java.lang.String[];

    $r3 = new nju.sa.examples.MethodCall3AC;

    specialinvoke $r3.<nju.sa.examples.MethodCall3AC: void <init>()>();

    virtualinvoke $r3.<nju.sa.examples.MethodCall3AC:
        java.lang.String foo(java.lang.String,java.lang.String)>("hello", "world");

    return;
}
```



Class

```
package nju.sa.examples;
public class Class3AC {

    public static final double pi = 3.14;
    public static void main(String[] args) {

    }
}
```

Java Src

```
public class nju.sa.examples.Class3AC extends java.lang.Object
{
    public static final double pi;

    public void <init>()
    {
        nju.sa.examples.Class3AC r0;

        r0 := @this: nju.sa.examples.Class3AC;

        specialinvoke r0.<java.lang.Object: void <init>()>();

        return;
    }

    public static void main(java.lang.String[])
    {
        java.lang.String[] r0;

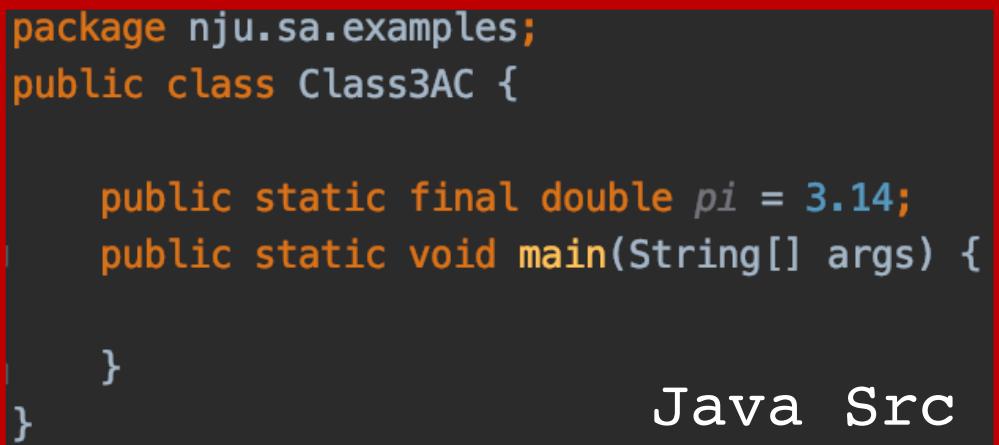
        r0 := @parameter0: java.lang.String[];

        return;
    }

    public static void <clinit>()
    {
        <nju.sa.examples.Class3AC: double pi> = 3.14;

        return;
    }
}
```

3AC(jimple)

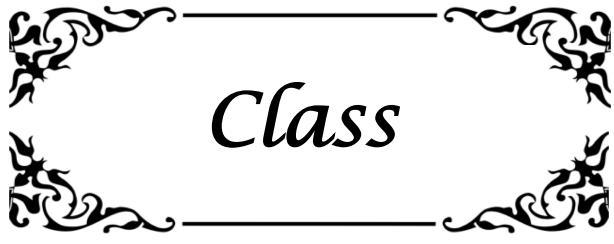


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package nju.sa.examples;
public class Class3AC {

    public static final double pi = 3.14;
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    }
}
```

Java Src



Class

Static Single Assignment (SSA)

Optional material

- All assignments in SSA are to variables with distinct names
 - Give each definition a fresh name
 - Propagate fresh name to subsequent uses
 - Every variable has exactly one definition

$$p = a + b$$

$$q = p - c$$

$$p = q * d$$

$$p = e - p$$

$$q = p + q$$

$$p_1 = a + b$$

$$q_1 = p_1 - c$$

$$p_2 = q_1 * d$$

$$p_3 = e - p_2$$

$$q_2 = p_3 + q_1$$

3AC

SSA

Static Single Assignment (SSA)

- All assignments in SSA are to variables with distinct names
 - Give each definition a fresh name
 - Propagate fresh name to subsequent uses
 - Every variable has exactly one definition

$$\begin{array}{l} p = a + b \\ q = p - c \\ p = q * d \\ p = e - p \\ q = p + q \end{array}$$

3AC

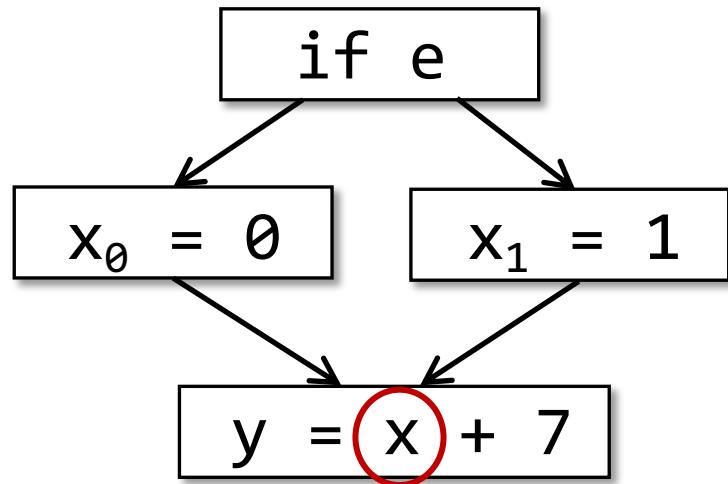
$$\begin{array}{l} p_1 = a + b \\ q_1 = p_1 - c \\ p_2 = q_1 * d \\ p_3 = e - p_2 \\ q_2 = p_3 + q_1 \end{array}$$

SSA



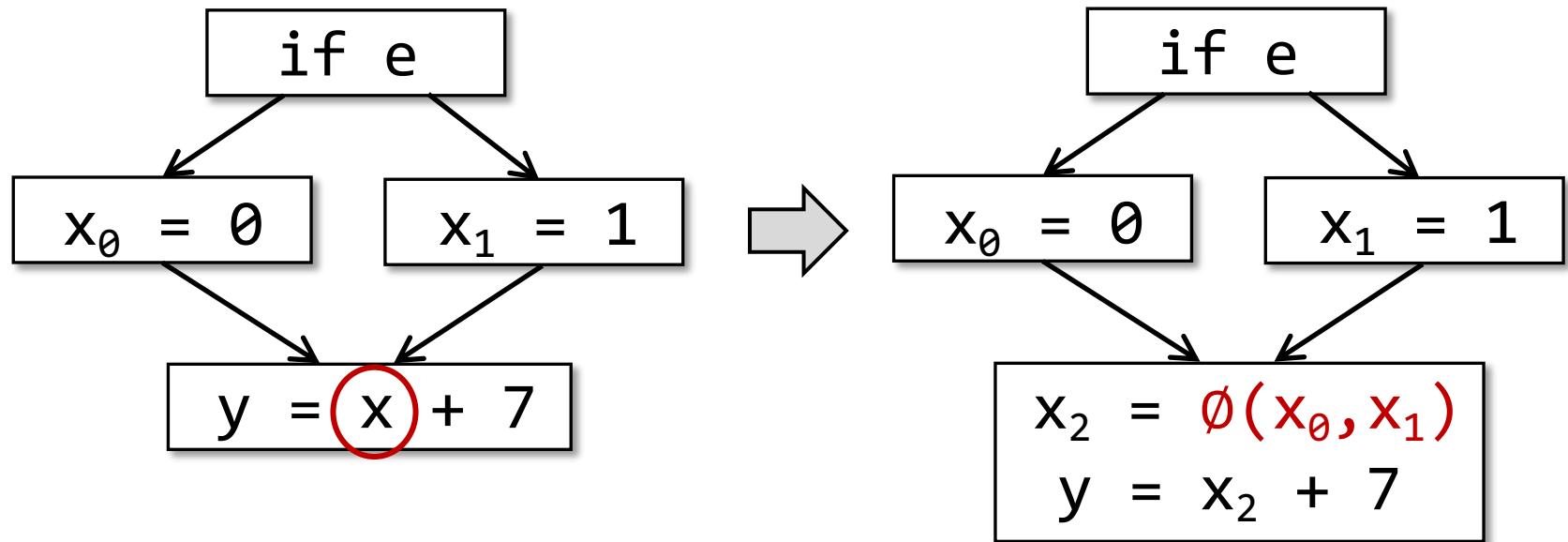
Static Single Assignment (SSA)

- What if a variable use is at control flow merges?



Static Single Assignment (SSA)

- What if a variable use is at control flow merges?



- A special merge operator, \emptyset (called phi-function), is introduced to select the values at merge nodes
- $\emptyset(x_0, x_1)$ has the value x_0 if the control flow passes through the true part of the conditional and the value x_1 otherwise

Why SSA?

Why not SSA?

Why SSA?

- Flow information is indirectly incorporated into the unique variable names

May help deliver some simpler analyses, e.g., flow-insensitive analysis gains partial precision of flow-sensitive analysis via SSA
- Define-and-Use pairs are explicit

Enable more effective data facts storage and propagation in some on-demand tasks
- Some optimization tasks perform better on SSA (e.g., conditional constant propagation, global value numbering)

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Why not SSA?

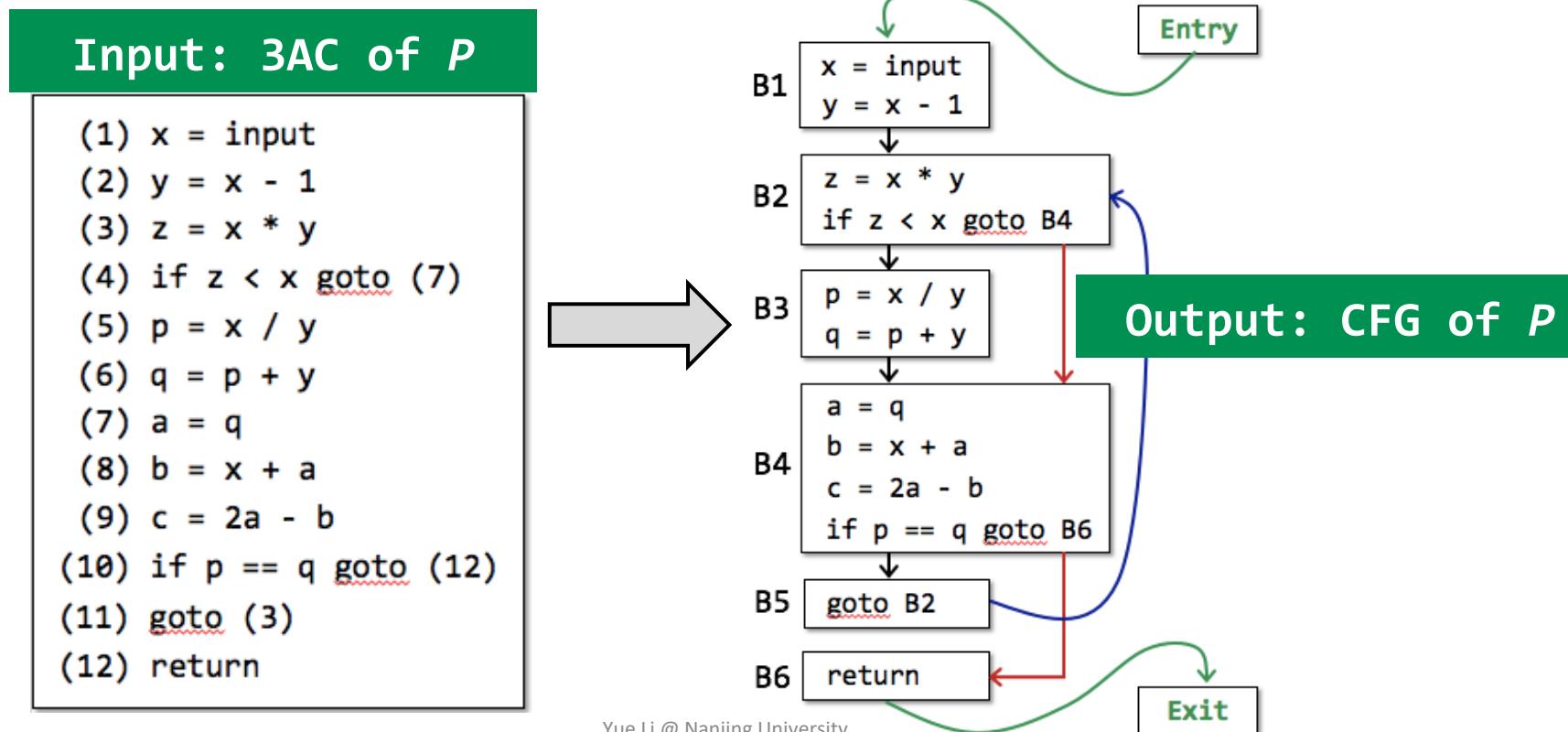
- SSA may introduce too many variables and phi-functions
- May introduce inefficiency problem when translating to machine code (due to copy operations)

Control Flow Analysis

- Usually refer to building Control Flow Graph (CFG)

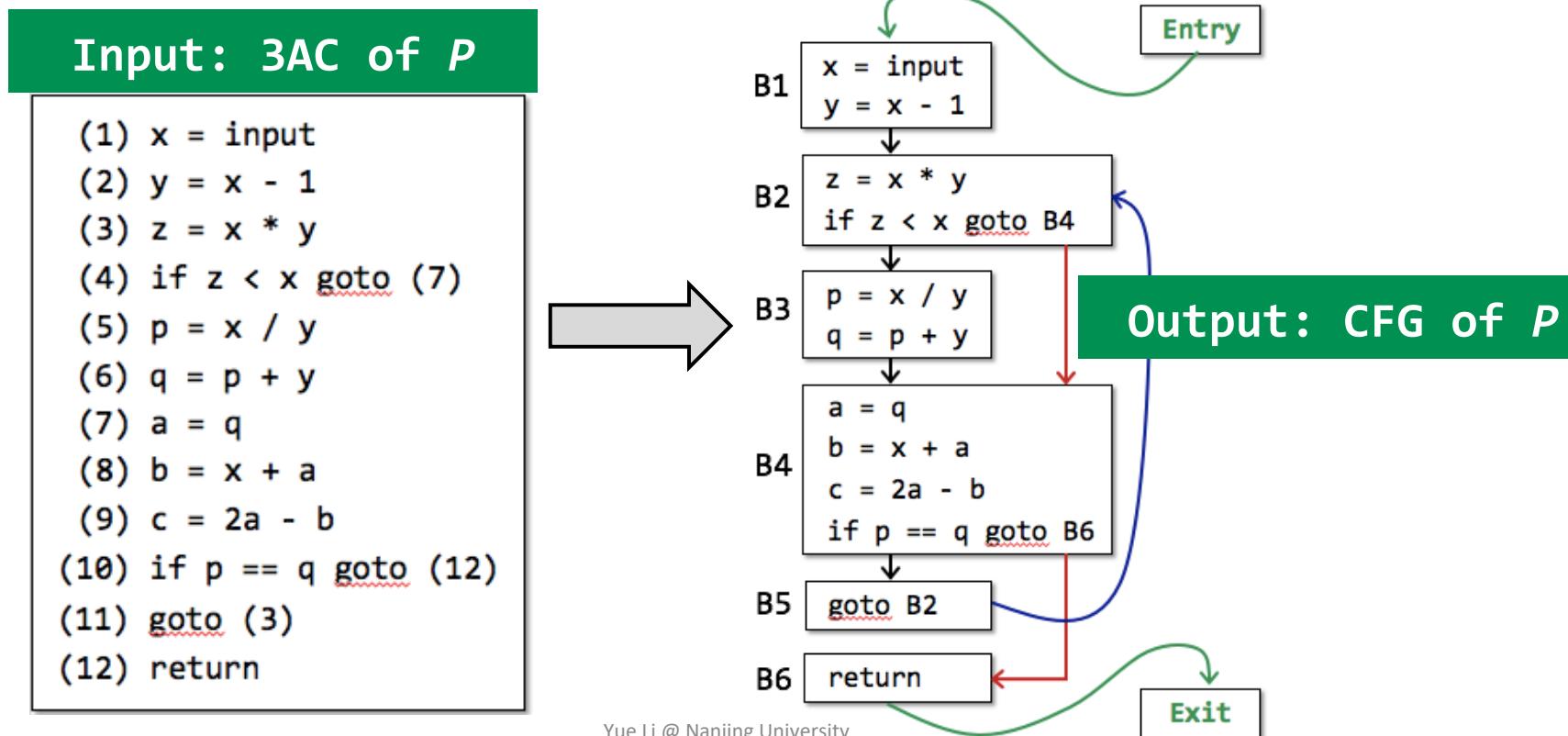
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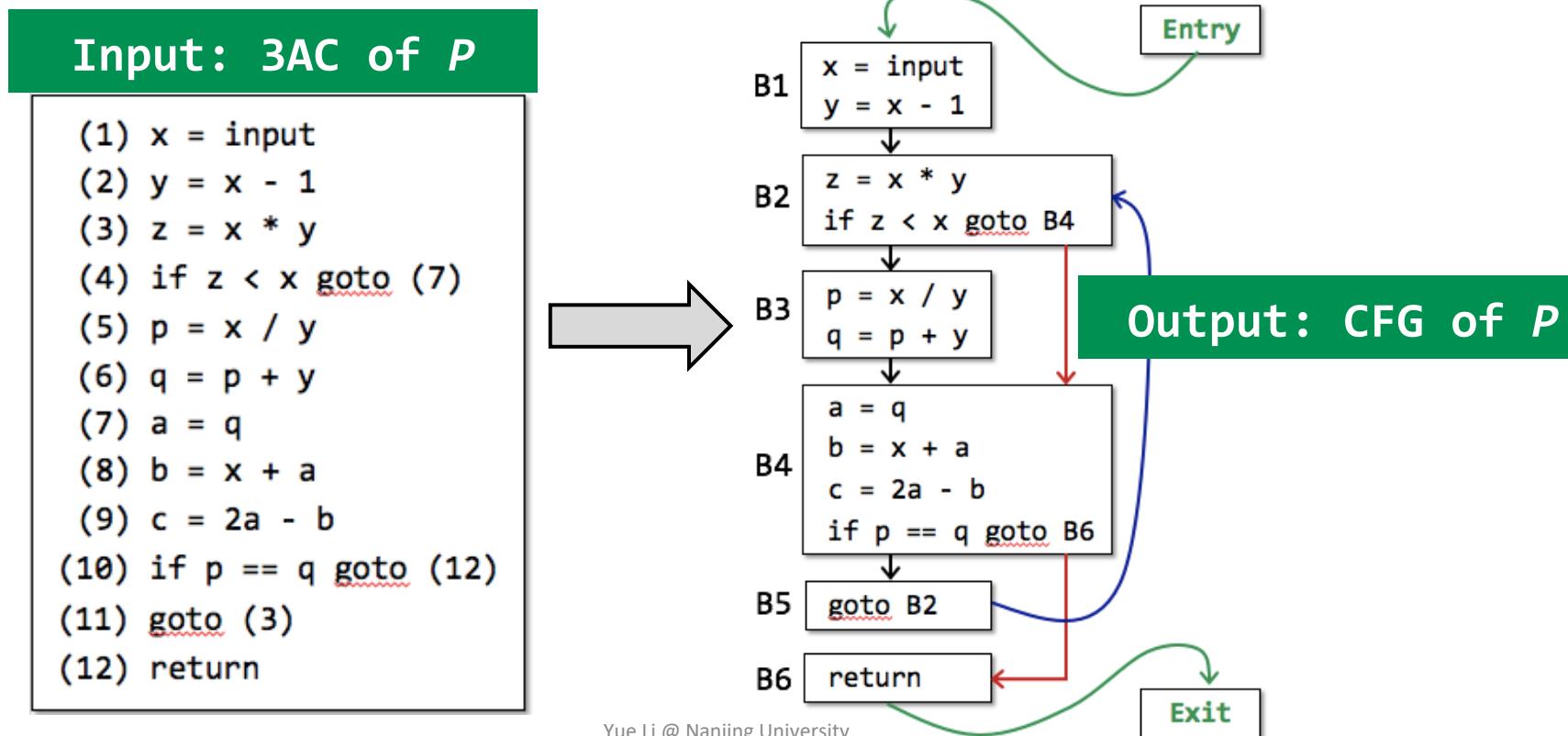
Control Flow Analysis

- Usually refer to building Control Flow Graph (CFG)
- CFG serves as the basic structure for static analysis



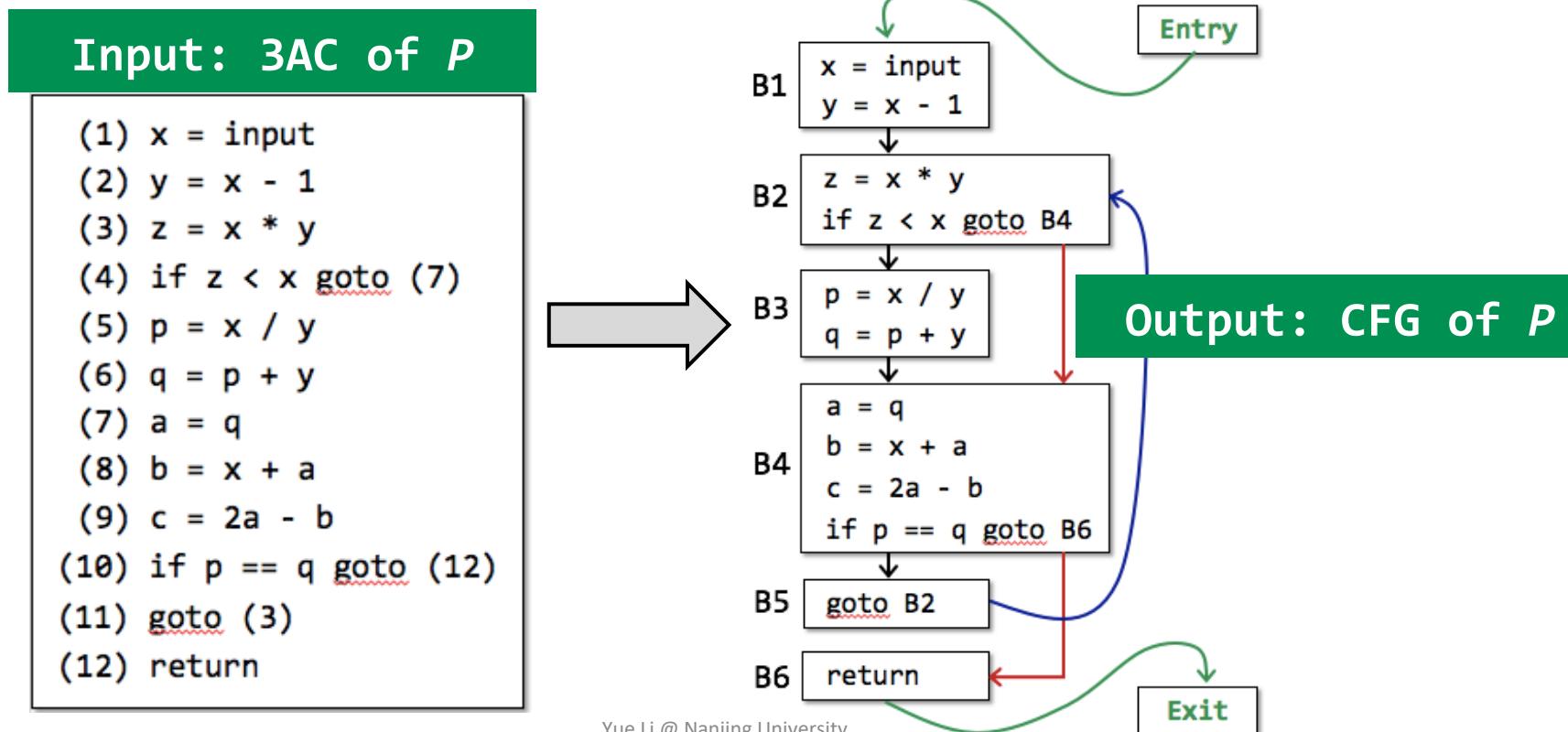
Control Flow Analysis

- Usually refer to building Control Flow Graph (CFG)
- CFG serves as the basic structure for static analysis
- The node in CFG can be an individual 3-address instruction, or (usually) a Basic Block (BB)



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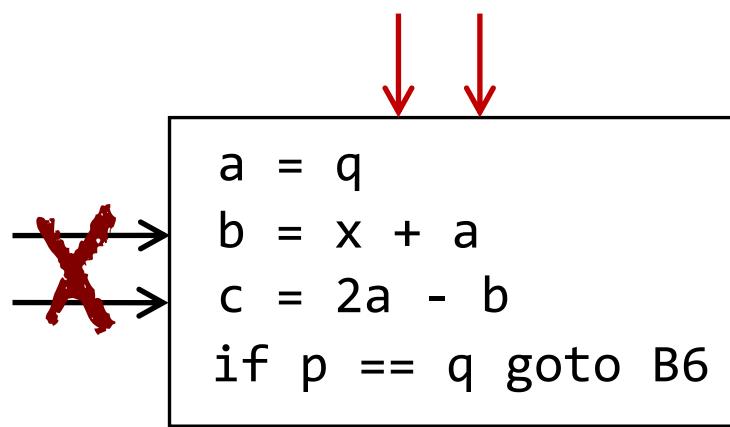
Basic Blocks (BB)

- Basic blocks (BB) are maximal sequences of consecutive three-address instructions with the properties that

```
a = q  
b = x + a  
c = 2a - b  
if p == q goto B6
```

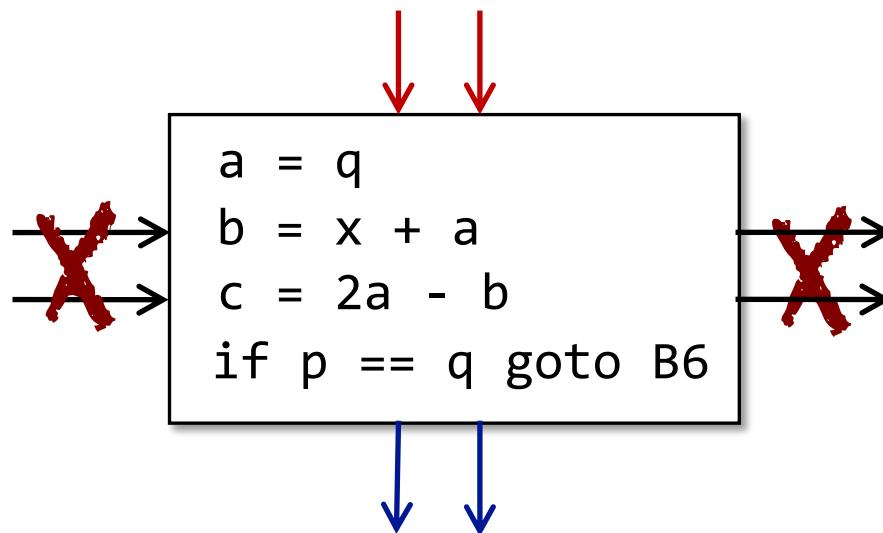
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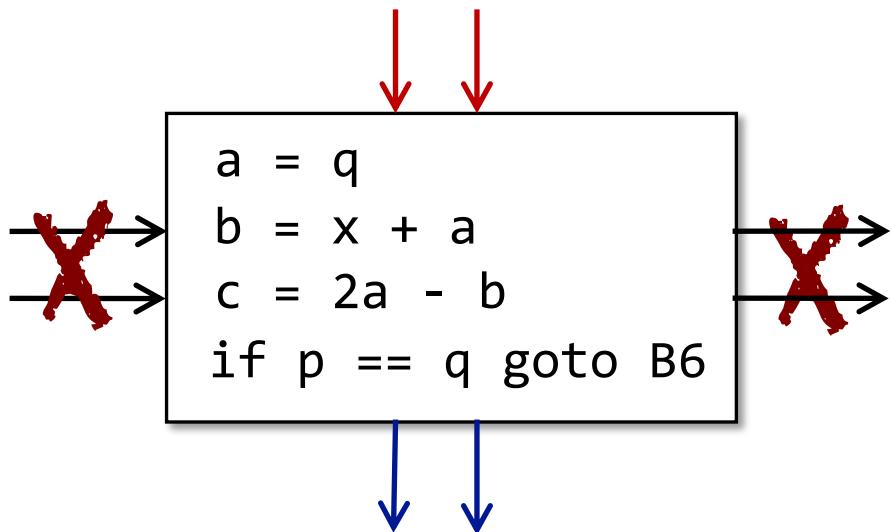
Basic Blocks (BB)

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 - It can be entered only at the beginning, i.e., *the first instruction in the block*
 - It can be exited only at the end, i.e., *the last instruction in the block*



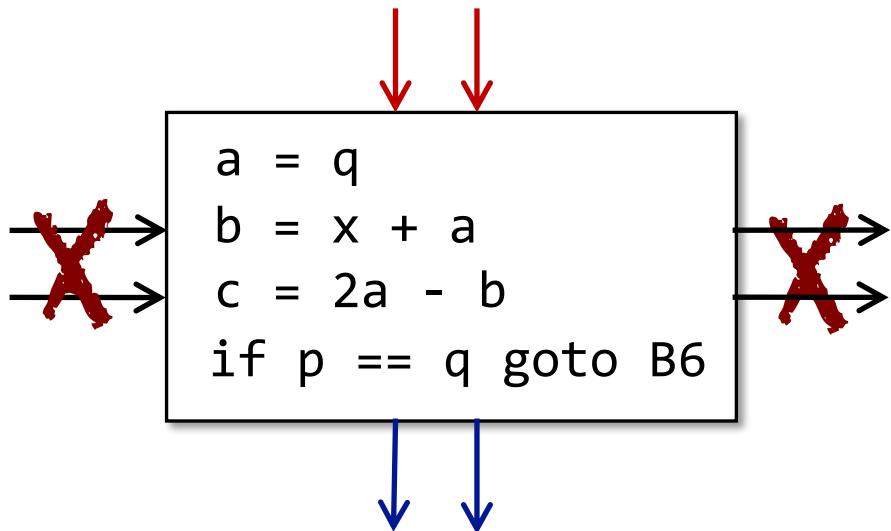
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(1) x = input  
(2) y = x - 1  
(3) z = x * y  
(4) if z < x goto (7)  
(5) p = x / y  
(6) q = p + y  
(7) a = q  
(8) b = x + a  
(9) c = 2a - b  
(10) if p == q goto (12)  
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(12) return
```

Now try to design the algorithm to build BBs by yourself!



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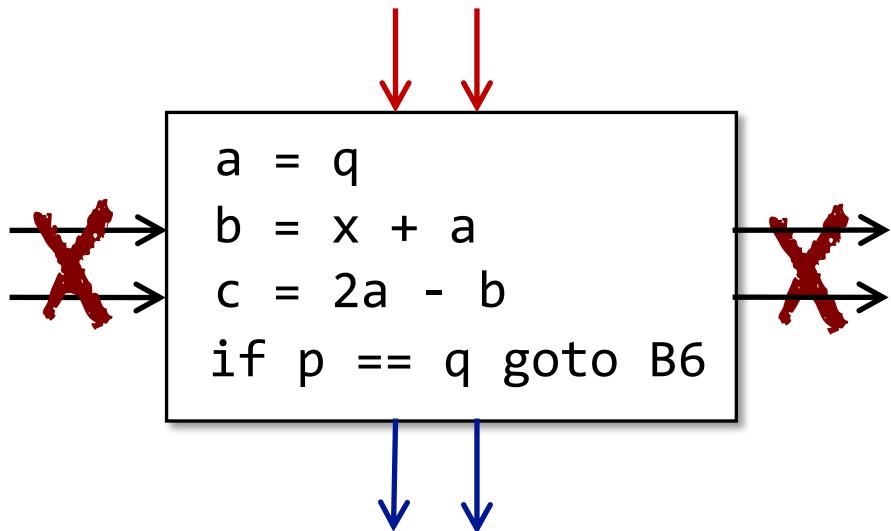


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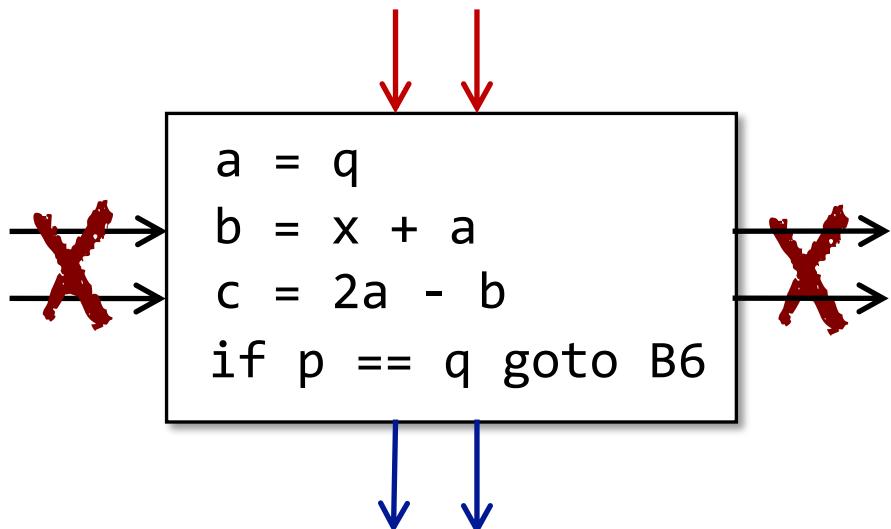
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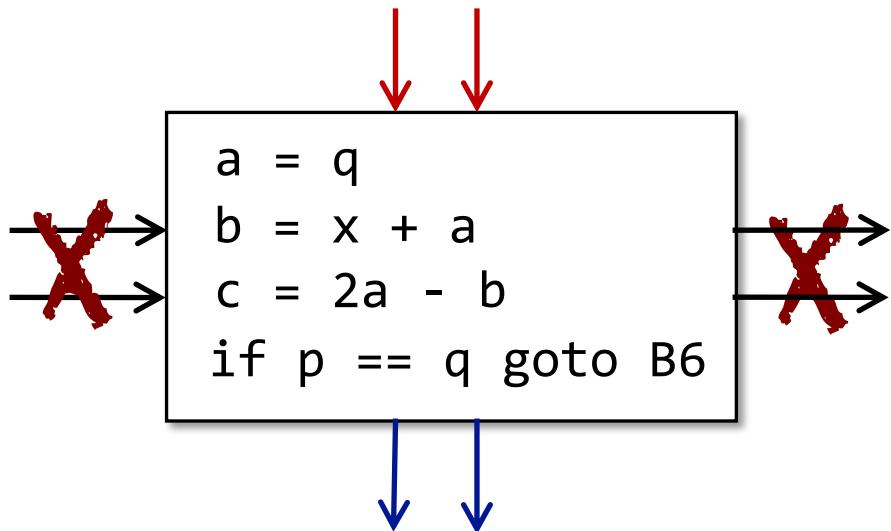


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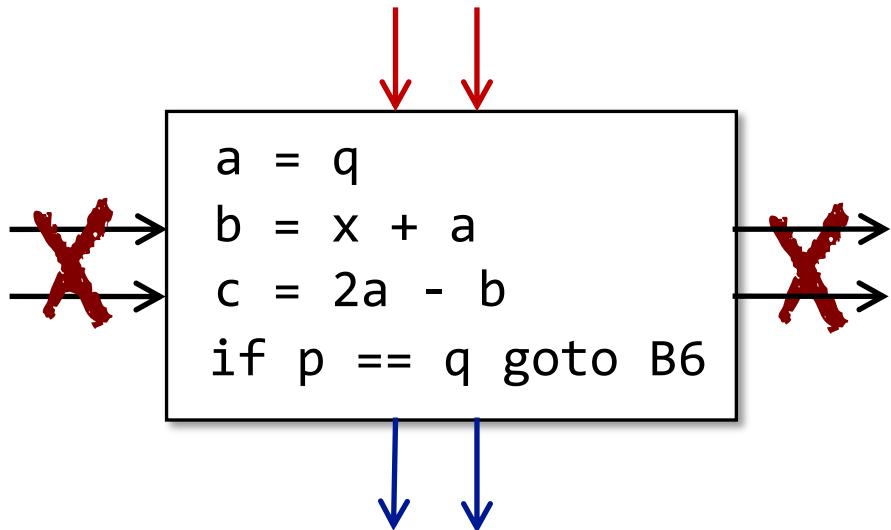


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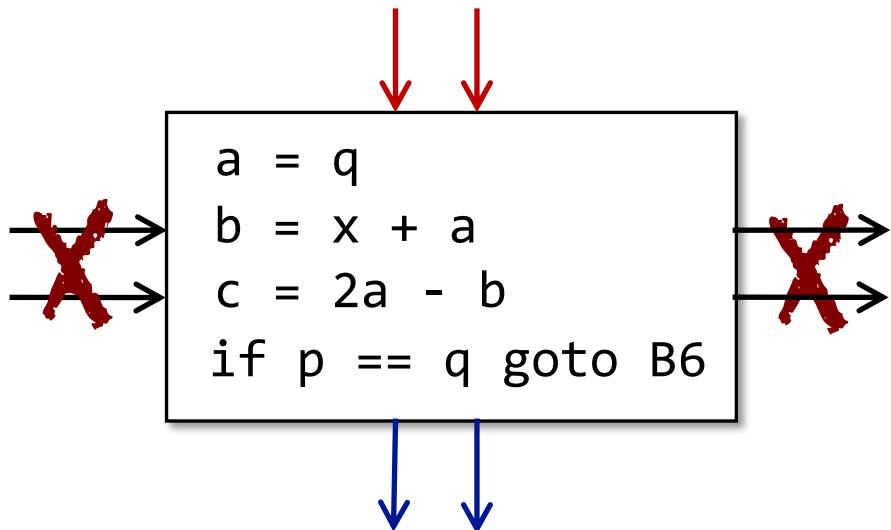


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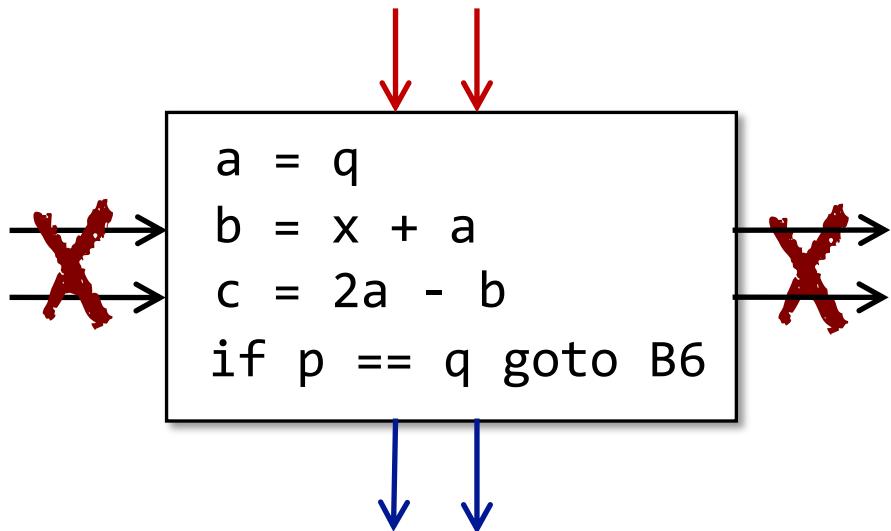


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Now try to design the algorithm to build BBs by yourself!



How to build Basic Blocks?

INPUT: A sequence of three-address instructions of P

OUTPUT: A list of basic blocks of P

METHOD: (1) Determine the leaders in P

- The first instruction in P is a leader
- Any target instruction of a conditional or unconditional jump is a leader
- Any instruction that immediately follows a conditional or unconditional jump is a leader

(2) Build BBs for P

- A BB consists of a leader and all its subsequent instructions until the next leader

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(4) if z < x goto (7)  
(5) p = x / y  
(6) q = p + y  
(7) a = q  
(8) b = x + a  
(9) c = 2a - b  
(10) if p == q goto (12)  
(11) goto (3)  
(12) return
```

Output: BBs of P

(1) Determine the leaders in P

- The first instruction in P is a leader

Input: 3AC of P

```
(1) x = input  
(2) y = x - 1  
(3) z = x * y  
(4) if z < x goto (7)  
(5) p = x / y  
(6) q = p + y  
(7) a = q  
(8) b = x + a  
(9) c = 2a - b  
(10) if p == q goto (12)  
(11) goto (3)  
(12) return
```

Output: BBs of P

(1) Determine the leaders in P

- (1)

Input: 3AC of P

```
(1) x = input  
(2) y = x - 1  
(3) z = x * y  
(4) if z < x goto (7)  
(5) p = x / y  
(6) q = p + y  
(7) a = q  
(8) b = x + a  
(9) c = 2a - b  
(10) if p == q goto (12)  
(11) goto (3)  
(12) return
```

Output: BBs of P

(1) Determine the leaders in P

- (1)
- Any target instruction of a conditional or unconditional jump is a leader

Input: 3AC of P

```
(1) x = input  
(2) y = x - 1  
(3) z = x * y  
(4) if z < x goto (7)  
(5) p = x / y  
(6) q = p + y  
(7) a = q  
(8) b = x + a  
(9) c = 2a - b  
(10) if p == q goto (12)  
(11) goto (3)  
(12) return
```

Output: BBs of P

(1) Determine the leaders in P

- (1)
- Any target instruction of a conditional or unconditional jump is a leader

Input: 3AC of P

```
(1) x = input  
(2) y = x - 1  
(3) z = x * y  
(4) if z < x goto (7)  
(5) p = x / y  
(6) q = p + y  
(7) a = q  
(8) b = x + a  
(9) c = 2a - b  
(10) if p == q goto (12)  
(11) goto (3)  
(12) return
```

Output: BBs of P

(1) Determine the leaders in P

- (1)
- (3), (7), (12)

Input: 3AC of P

```
(1) x = input  
(2) y = x - 1  
(3) z = x * y  
(4) if z < x goto (7)  
(5) p = x / y  
(6) q = p + y  
(7) a = q  
(8) b = x + a  
(9) c = 2a - b  
(10) if p == q goto (12)  
(11) goto (3)  
(12) return
```

Output: BBs of P

(1) Determine the leaders in P

- (1)
- (3), (7), (12)
- Any instruction that immediately follows a conditional or unconditional jump is a leader

Input: 3AC of P

```
(1) x = input  
(2) y = x - 1  
(3) z = x * y  
(4) if z < x goto (7)  
(5) p = x / y  
(6) q = p + y  
(7) a = q  
(8) b = x + a  
(9) c = 2a - b  
(10) if p == q goto (12)  
(11) goto (3)  
(12) return
```

Output: BBs of P

(1) Determine the leaders in P

- (1)
- (3), (7), (12)
- Any instruction that immediately follows a conditional or unconditional jump is a leader

Input: 3AC of P

```
(1) x = input  
(2) y = x - 1  
(3) z = x * y  
(4) if z < x goto (7)  
(5) p = x / y  
(6) q = p + y  
(7) a = q  
(8) b = x + a  
(9) c = 2a - b  
(10) if p == q goto (12)  
(11) goto (3)  
(12) return
```

Output: BBs of P

(1) Determine the leaders in P

- (1)
- (3),(7),(12)
- (5),(11),(12)

Input: 3AC of P

```
(1) x = input  
(2) y = x - 1  
(3) z = x * y  
(4) if z < x goto (7)  
(5) p = x / y  
(6) q = p + y  
(7) a = q  
(8) b = x + a  
(9) c = 2a - b  
(10) if p == q goto (12)  
(11) goto (3)  
(12) return
```

Output: BBs of P

(1) Determine the leaders in P

- (1) Leaders: (1), (3),
- (3), (7), (12) (5), (7), (11), (12)
- (5), (11), (12)

Input: 3AC of P

```
(1) x = input  
(2) y = x - 1  
(3) z = x * y  
(4) if z < x goto (7)  
(5) p = x / y  
(6) q = p + y  
(7) a = q  
(8) b = x + a  
(9) c = 2a - b  
(10) if p == q goto (12)  
(11) goto (3)  
(12) return
```

Output: BBs of P

(1) Determine the leaders in P

- (1) Leaders: (1), (3),
- (3), (7), (12) (5), (7), (11), (12)
- (5), (11), (12)

(2) Build BBs for P

- A BB consists of a leader and all its subsequent instructions until the next leader

Input: 3AC of P

```
(1) x = input  
(2) y = x - 1  
(3) z = x * y  
(4) if z < x goto (7)  
(5) p = x / y  
(6) q = p + y  
(7) a = q  
(8) b = x + a  
(9) c = 2a - b  
(10) if p == q goto (12)  
(11) goto (3)  
(12) return
```

Output: BBs of P

(1) Determine the leaders in P

- (1) Leaders: (1), (3),
- (3), (7), (12) (5), (7), (11), (12)
- (5), (11), (12)

(2) Build BBs for P

- A BB consists of a leader and all its subsequent instructions until the next leader
- B1 {(1)}
- B2 {(3)}
- B3 {(5)}
- B4 {(7)}
- B5 {(11)}
- B6 {(12)}

Input: 3AC of P

```
(1) x = input  
(2) y = x - 1  
(3) z = x * y  
(4) if z < x goto (7)  
(5) p = x / y  
(6) q = p + y  
(7) a = q  
(8) b = x + a  
(9) c = 2a - b  
(10) if p == q goto (12)  
(11) goto (3)  
(12) return
```

Output: BBs of P

(1) Determine the leaders in P

- (1) Leaders: (1), (3), (5), (7), (11), (12)
- (3), (7), (12)
- (5), (11), (12)

(2) Build BBs for P

- A BB consists of a leader and all its subsequent instructions until the next leader
- B1 {(1), (2)}
- B2 {(3), (4)}
- B3 {(5), (6)}
- B4 {(7), (8), (9), (10)}
- B5 {(11)}
- B6 {(12)}

Input: 3AC of P

```
(1) x = input  
(2) y = x - 1  
(3) z = x * y  
(4) if z < x goto (7)  
(5) p = x / y  
(6) q = p + y  
(7) a = q  
(8) b = x + a  
(9) c = 2a - b  
(10) if p == q goto (12)  
(11) goto (3)  
(12) return
```

Output: BBs of P

- B1 {(1),(2)}
- B2 {(3),(4)}
- B3 {(5),(6)}
- B4 {(7),(8),(9),(10)}
- B5 {(11)}
- B6 {(12)}

Input: 3AC of P

```
(1) x = input  
(2) y = x - 1  
(3) z = x * y  
(4) if z < x goto (7)  
(5) p = x / y  
(6) q = p + y  
(7) a = q  
(8) b = x + a  
(9) c = 2a - b  
(10) if p == q goto (12)  
(11) goto (3)  
(12) return
```

Output: BBs of P

B1

```
(1) x = input  
(2) y = x - 1
```

B2

```
(3) z = x * y  
(4) if z < x goto (7)
```

B3

```
(5) p = x / y  
(6) q = p + y
```

B4

```
(7) a = q  
(8) b = x + a  
(9) c = 2a - b  
(10) if p == q goto (12)
```

B5

```
(11) goto (3)
```

B6

```
(12) return
```

Input: 3AC of P

```
(1) x = input  
(2) y = x - 1  
(3) z = x * y  
(4) if z < x goto (7)  
(5) p = x / y  
(6) q = p + y  
(7) a = q  
(8) b = x + a  
(9) c = 2a - b  
(10) if p == q goto (12)  
(11) goto (3)  
(12) return
```

How to build CFG
on top of BBs?

Output: BBs of P

B1

```
(1) x = input  
(2) y = x - 1
```

B2

```
(3) z = x * y  
(4) if z < x goto (7)
```

B3

```
(5) p = x / y  
(6) q = p + y
```

B4

```
(7) a = q  
(8) b = x + a  
(9) c = 2a - b  
(10) if p == q goto (12)
```

B5

```
(11) goto (3)
```

B6

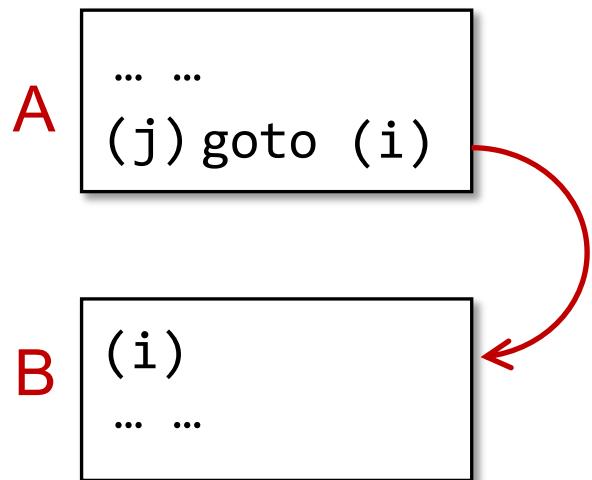
```
(12) return
```

Control Flow Graph (CFG)

- The nodes of CFG are basic blocks
- There is an edge from block A to block B if and only if

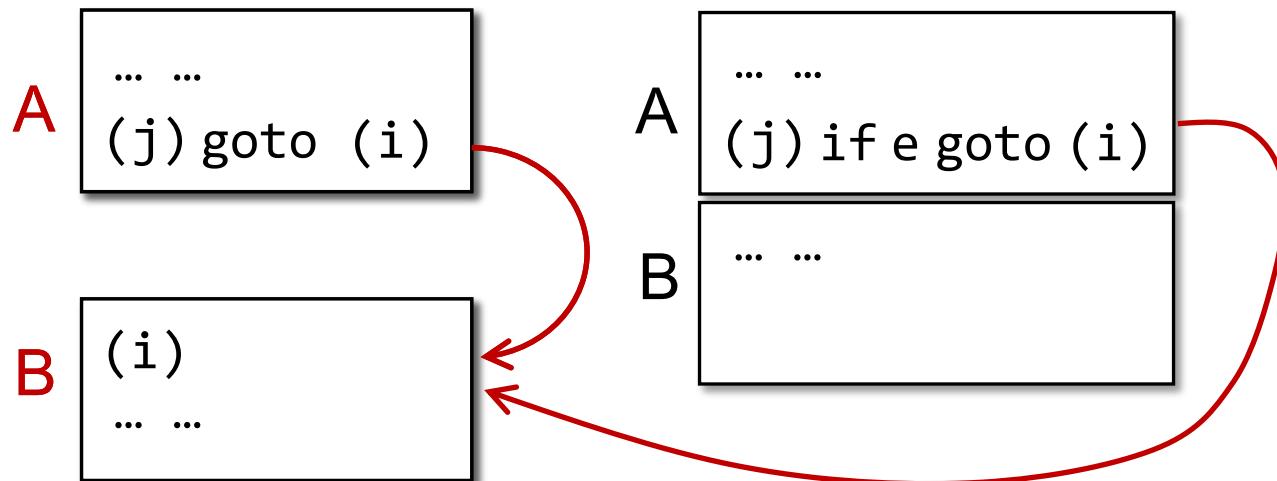
Control Flow Graph (CFG)

- The nodes of CFG are basic blocks
- There is an edge from block A to block B if and only if



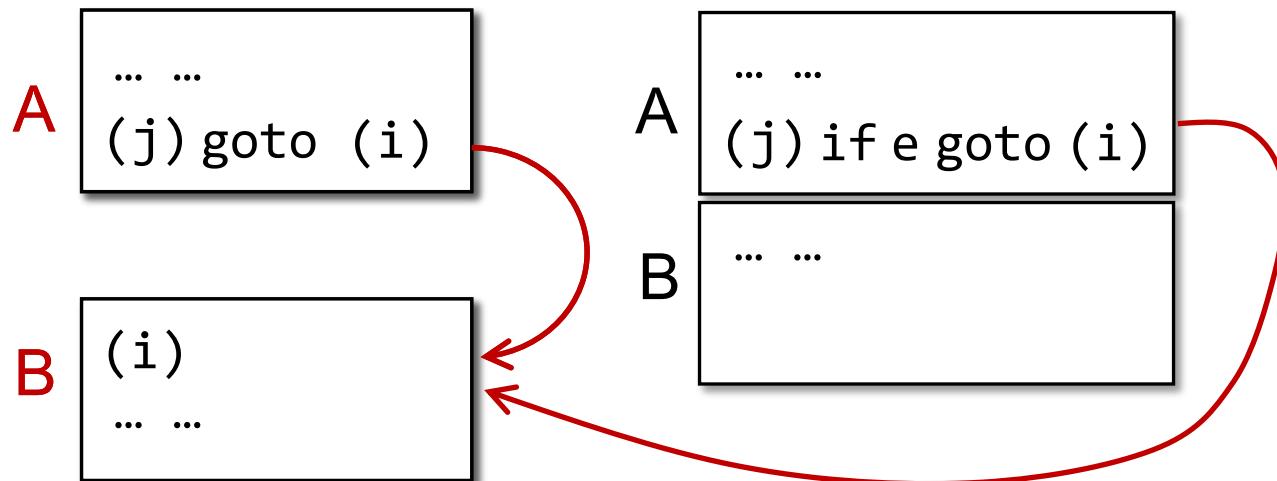
Control Flow Graph (CFG)

- The nodes of CFG are basic blocks
- There is an edge from block A to block B if and only if



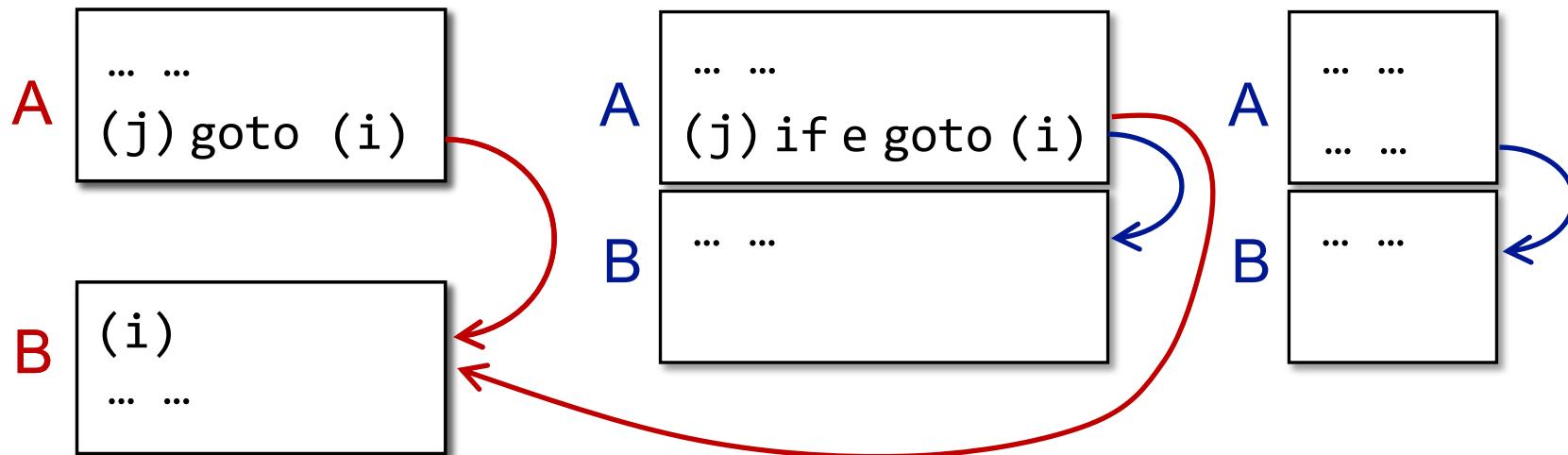
Control Flow Graph (CFG)

- The nodes of CFG are basic blocks
- There is an edge from block A to block B if and only if
 - There is a conditional or unconditional jump from the end of A to the beginning of B



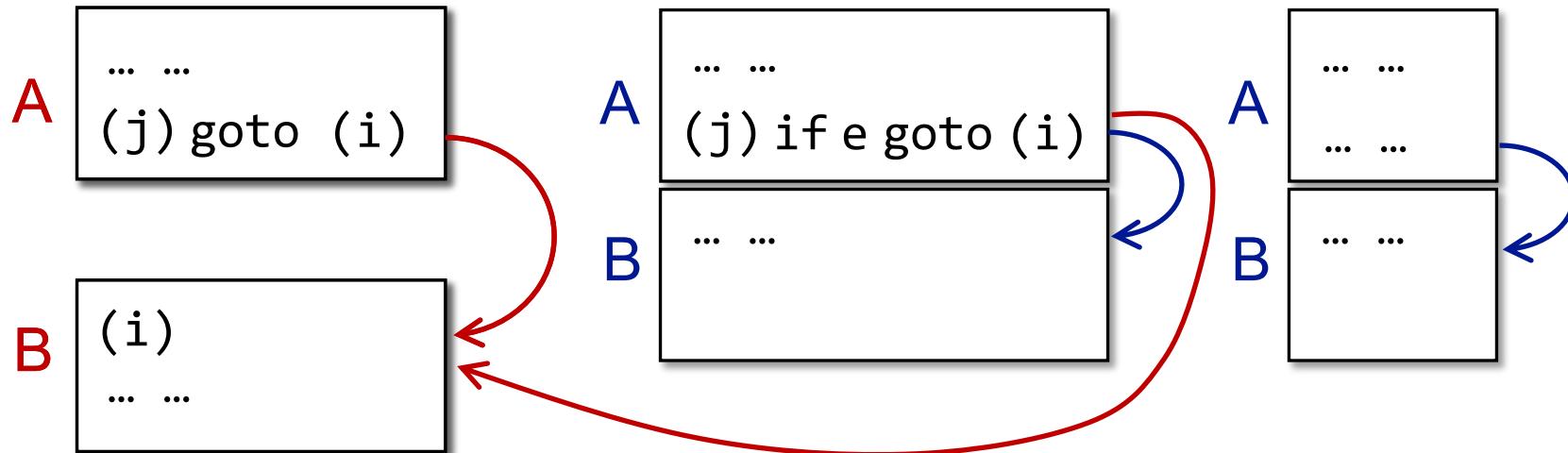
Control Flow Graph (CFG)

- The nodes of CFG are basic blocks
- There is an edge from block A to block B if and only if
 - There is a conditional or unconditional jump from the end of A to the beginning of B



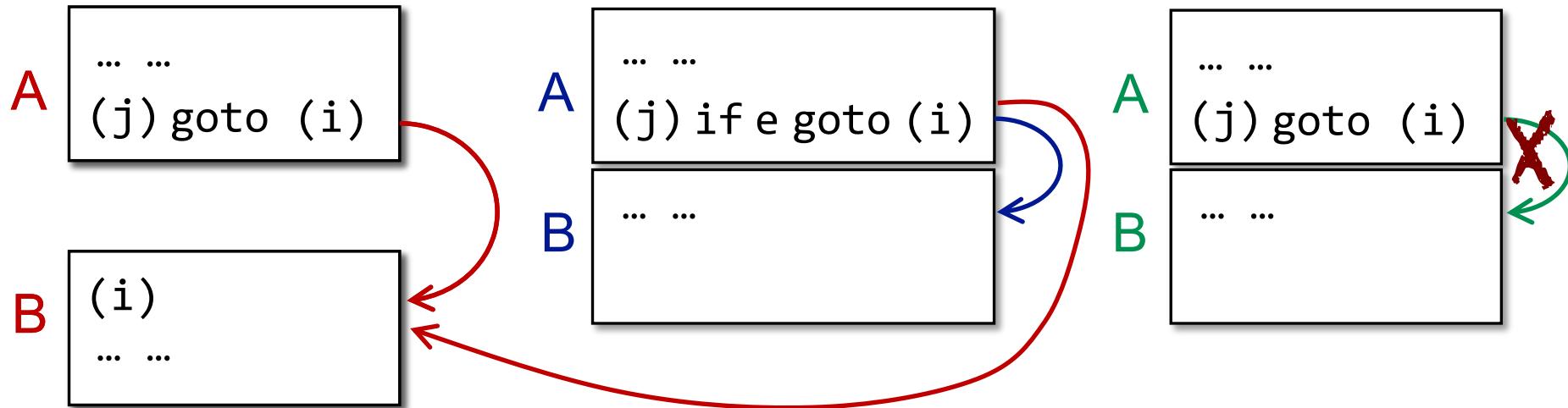
Control Flow Graph (CFG)

- The nodes of CFG are basic blocks
- There is an edge from block A to block B if and only if
 - There is a conditional or unconditional jump from the end of A to the beginning of B
 - B immediately follows A in the original order of instructions



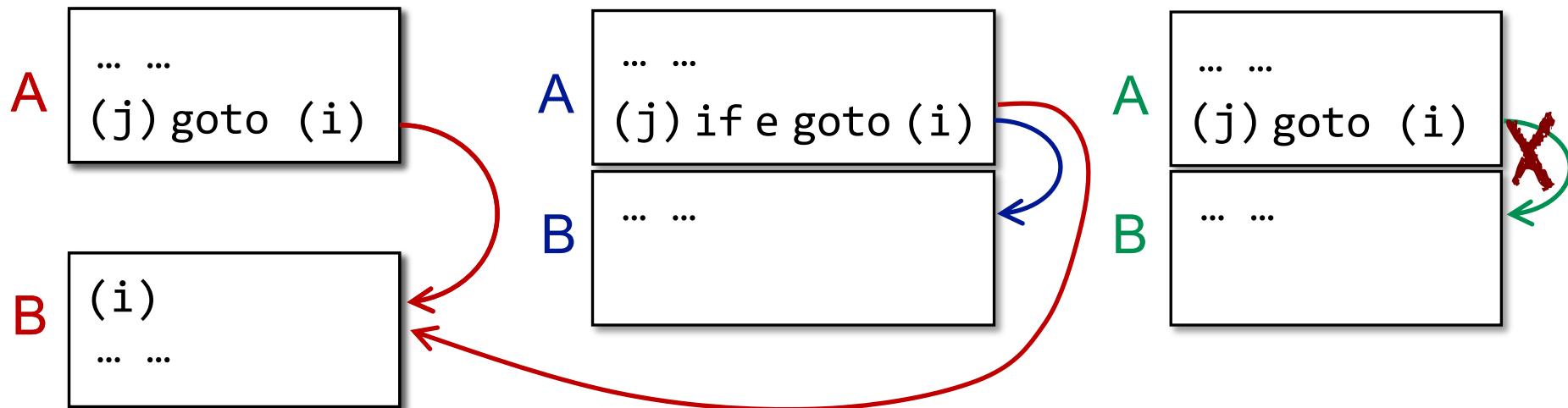
Control Flow Graph (CFG)

- The nodes of CFG are basic blocks
- There is an edge from block A to block B if and only if
 - There is a conditional or unconditional jump from the end of A to the beginning of B
 - B immediately follows A in the original order of instructions



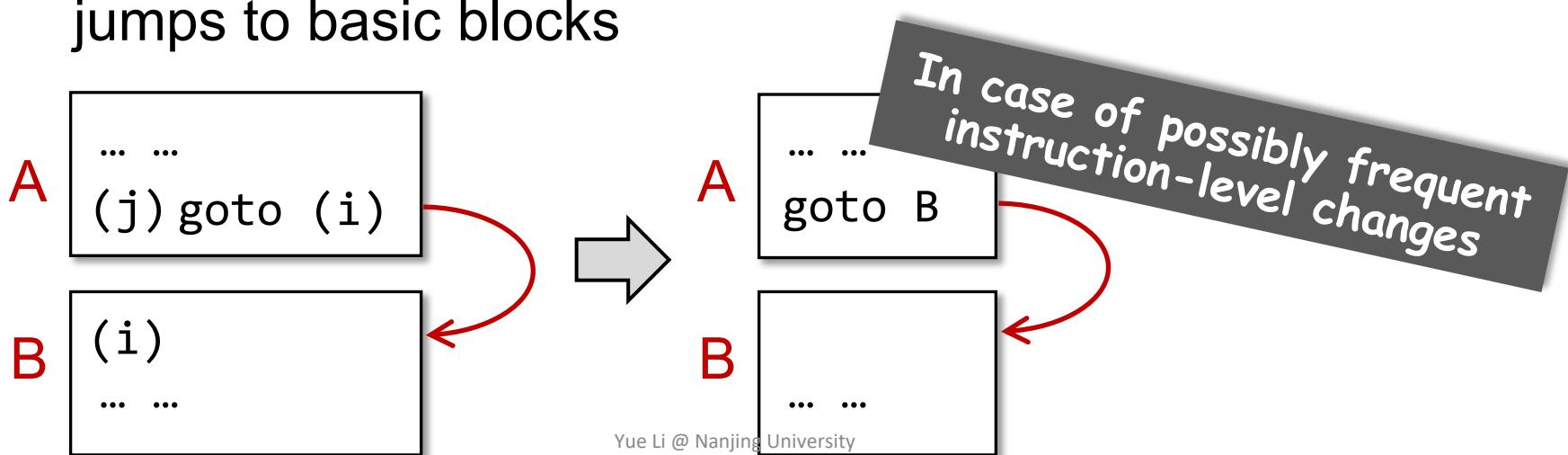
Control Flow Graph (CFG)

- The nodes of CFG are basic blocks
- There is an edge from block A to block B if and only if
 - There is a conditional or unconditional jump from the end of A to the beginning of B
 - B immediately follows A in the original order of instructions and A does not end in an unconditional jump



Control Flow Graph (CFG)

- The nodes of CFG are basic blocks
- There is an edge from block A to block B if and only if
 - There is a conditional or unconditional jump from the end of A to the beginning of B
 - B immediately follows A in the original order of instructions and A does not end in an unconditional jump
- It is normal to replace the jumps to instruction labels by jumps to basic blocks



B1

```
(1) x = input  
(2) y = x - 1
```

B2

```
(3) z = x * y  
(4) if z < x goto (7)
```

B3

```
(5) p = x / y  
(6) q = p + y
```

B4

```
(7) a = q  
(8) b = x + a  
(9) c = 2a - b  
(10) if p == q goto (12)
```

B5

```
(11) goto (3)
```

B6

```
(12) return
```

B1

```
x = input  
y = x - 1
```

B2

```
z = x * y  
if z < x goto B4
```

B3

```
p = x / y  
q = p + y
```

B4

```
a = q  
b = x + a  
c = 2a - b  
if p == q goto B6
```

B5

```
goto B2
```

B6

```
return
```

Add edges in CFG

B1

```
x = input  
y = x - 1
```

B2

```
z = x * y  
if z < x goto B4
```

B3

```
p = x / y  
q = p + y
```

B4

```
a = q  
b = x + a  
c = 2a - b  
if p == q goto B6
```

B5

```
goto B2
```

B6

```
return
```

Add edges in CFG

B1

```
x = input  
y = x - 1
```

B2

```
z = x * y  
if z < x goto B4
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B3

```
p = x / y  
q = p + y
```

B4

```
a = q  
b = x + a  
c = 2a - b  
if p == q goto B6
```

B5

```
goto B2
```

B6

```
return
```

There is a **conditional** or **unconditional** jump from the end of **A** to the beginning of **B**

Add edges in CFG

B1

```
x = input  
y = x - 1
```

B2

```
z = x * y  
if z < x goto B4
```

B3

```
p = x / y  
q = p + y
```

B4

```
a = q  
b = x + a  
c = 2a - b  
if p == q goto B6
```

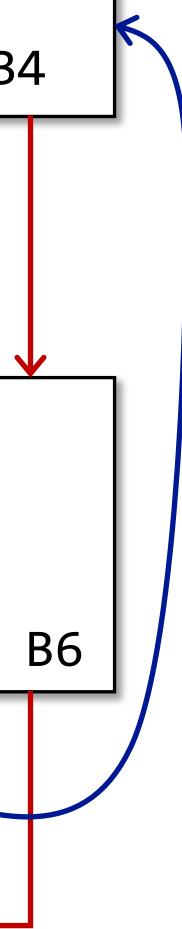
B5

```
goto B2
```

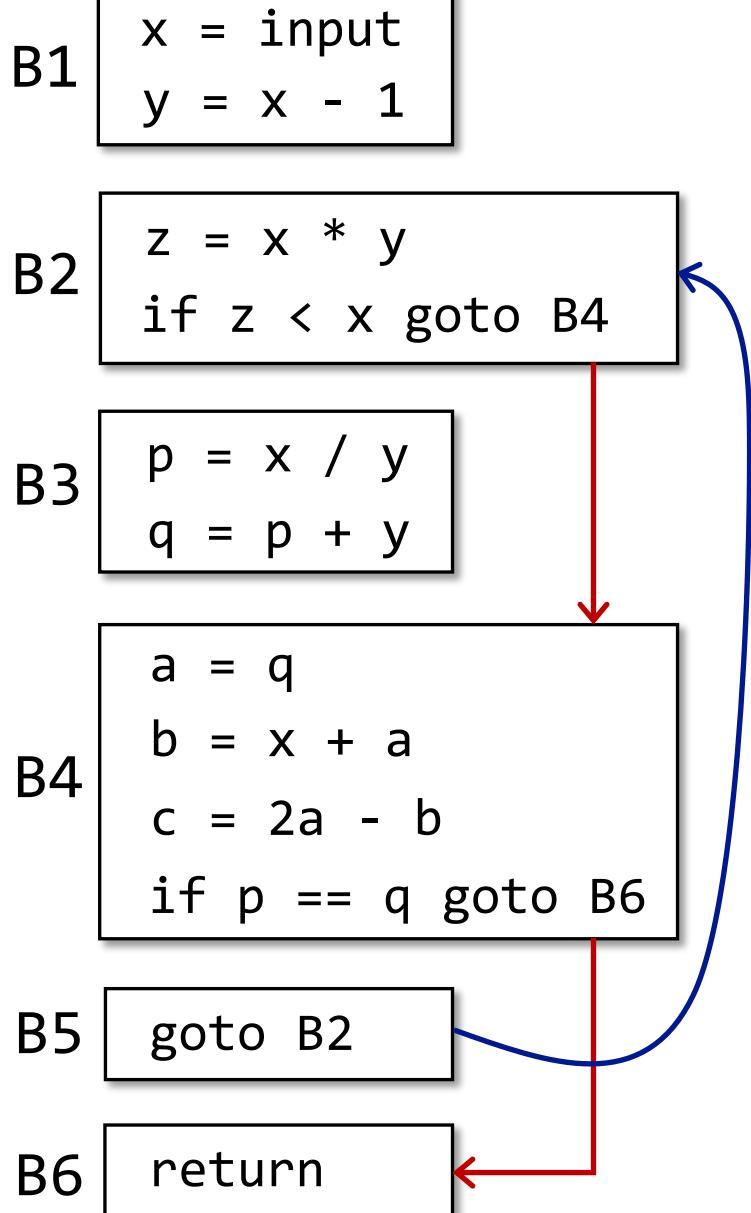
B6

```
return
```

There is a **conditional** or **unconditional** jump from the end of A to the beginning of B



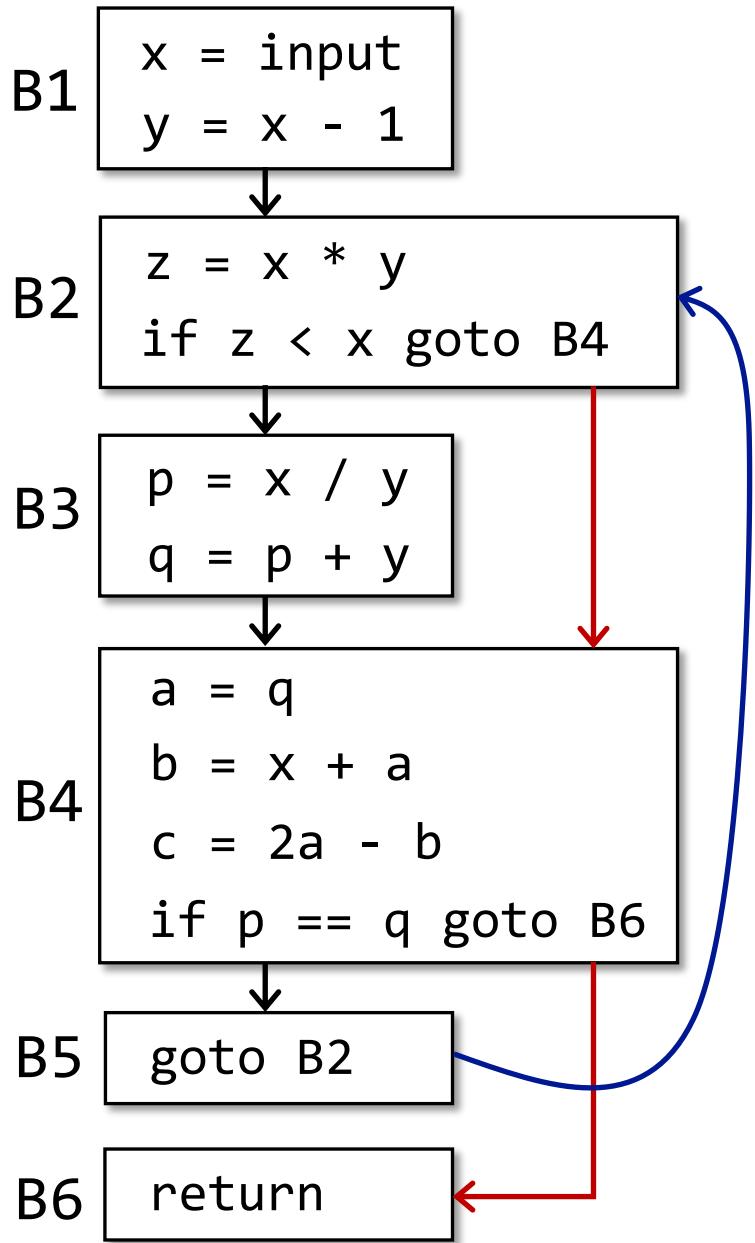
Add edges in CFG



There is a **conditional** or **unconditional** jump from the end of **A** to the beginning of **B**

B immediately follows **A** in the original order of instructions and **A** does not end in an unconditional jump

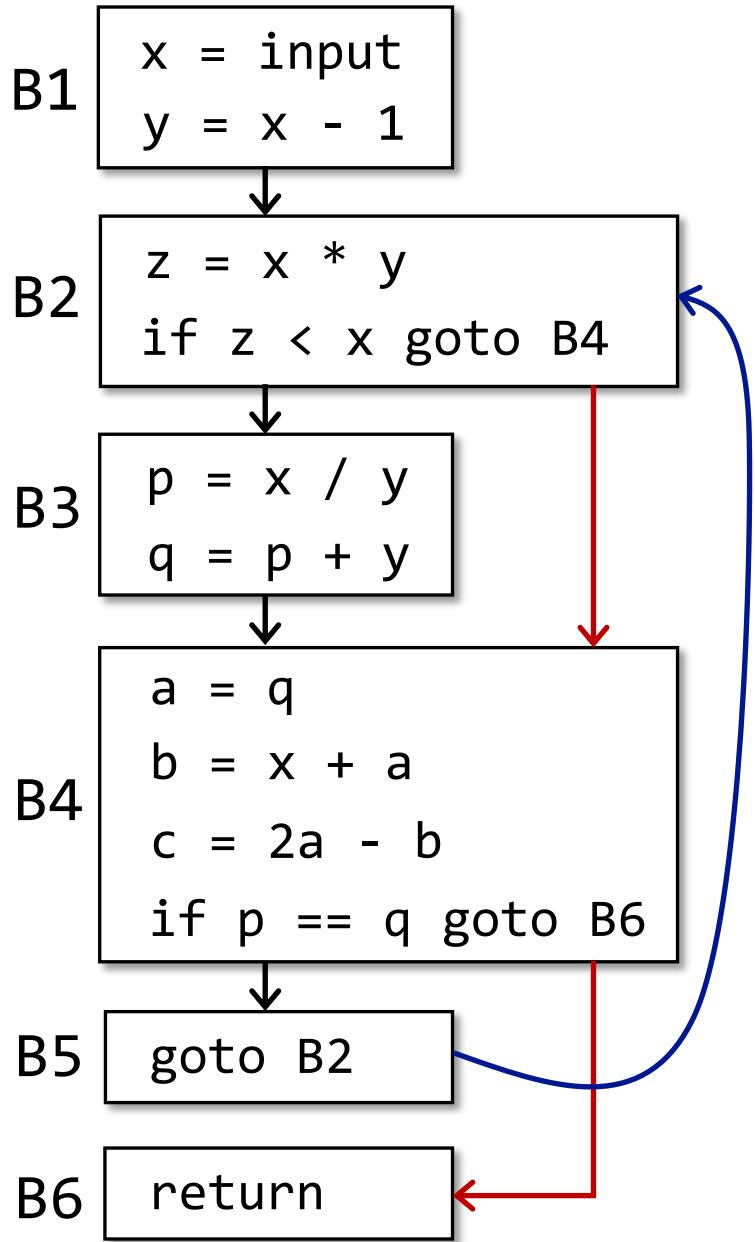
Add edges in CFG



There is a **conditional** or **unconditional** jump from the end of **A** to the beginning of **B**

B immediately follows **A** in the original order of instructions and **A** does not end in an unconditional jump

Add edges in CFG

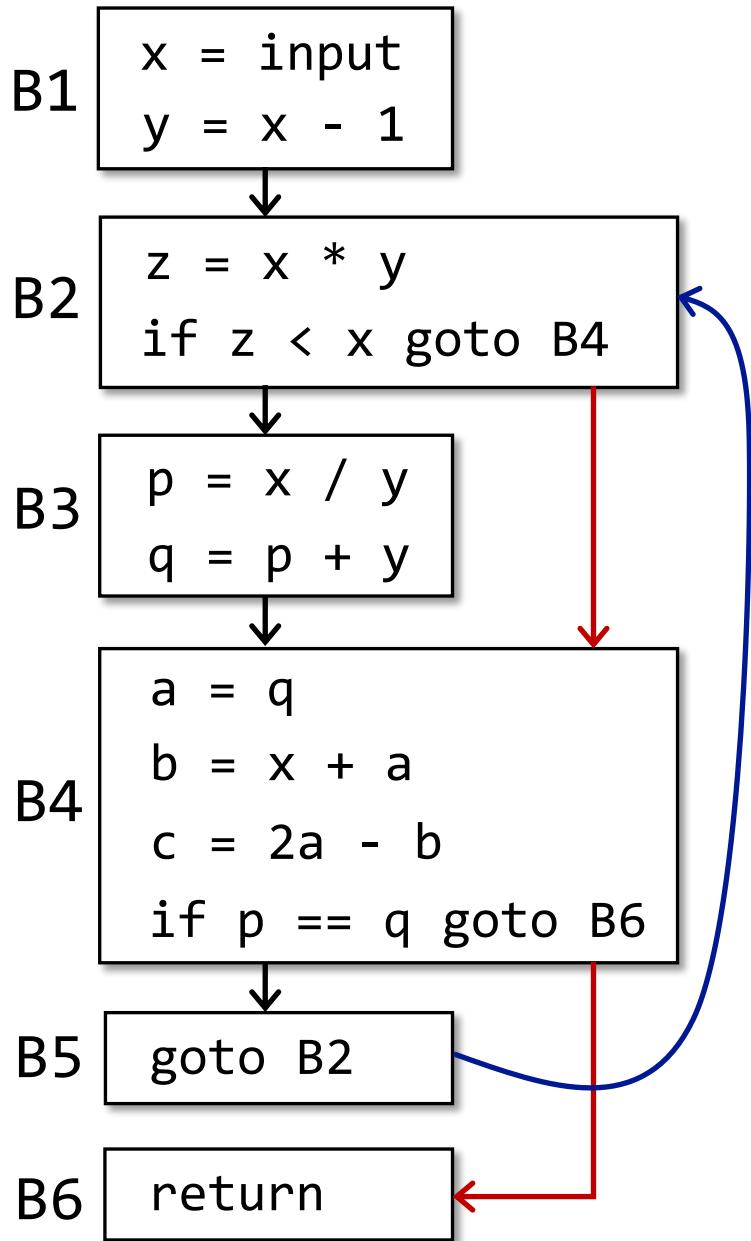


There is a **conditional** or **unconditional** jump from the end of **A** to the beginning of **B**

B immediately follows **A** in the original order of instructions and **A** does not end in an unconditional jump

We say that **A** is a **predecessor** of **B**, and **B** is a **successor** of **A**

Add edges in CFG



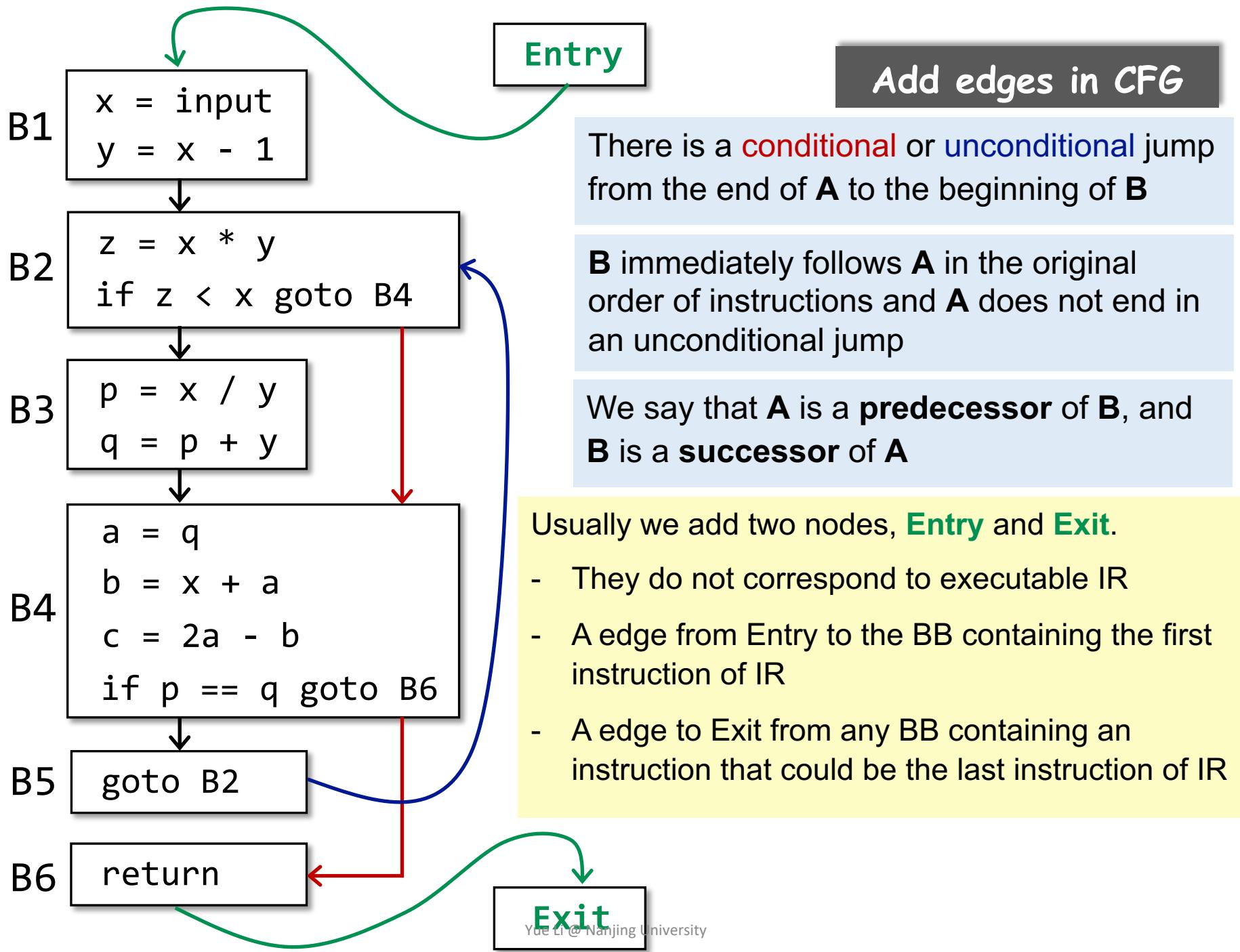
There is a **conditional** or **unconditional jump** from the end of **A** to the beginning of **B**

B immediately follows **A** in the original order of instructions and **A** does not end in an unconditional jump

We say that **A** is a **predecessor** of **B**, and **B** is a **successor** of **A**

Usually we add two nodes, **Entry** and **Exit**.

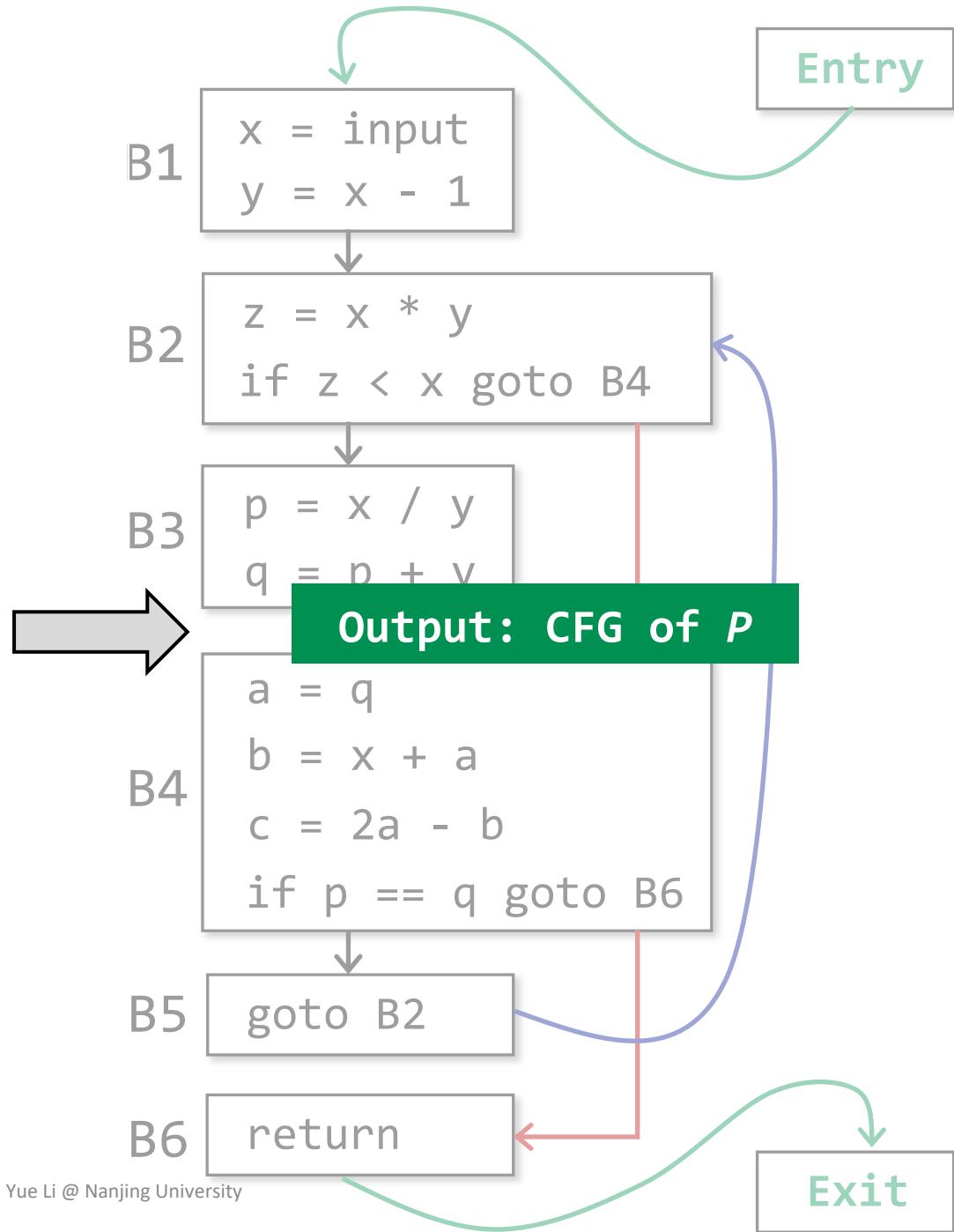
- They do not correspond to executable IR
- A edge from Entry to the BB containing the first instruction of IR
- A edge to Exit from any BB containing an instruction that could be the last instruction of IR



```

(1) x = input
(2) y = x - 1
(3) z = x * y
(4) if z < x goto (7)
(5) p = x / y
(6) a = p + q
Input: 3AC of P
(7) a = q
(8) b = x + a
(9) c = 2a - b
(10) if p == q goto (12)
(11) goto (3)
(12) return

```



Summary

1. Compilers and Static Analyzers
2. AST vs. IR
3. IR: Three-Address Code (3AC)
4. 3AC in Real Static Analyzer: Soot
5. Static Single Assignment (SSA)
6. Basic Blocks (BB)
7. Control Flow Graphs (CFG)

The ~~X~~ You Need To Understand in This Lecture

- The relation between compilers and static analyzers
- Understand 3AC and its common forms (in IR jimple)
- How to build basic blocks on top of IR
- How to construct control flow graphs on top of BBs?

注意注意！
划重点了！



软件分析

南京大学

计算机科学与技术系

程序设计语言与
静态分析研究组

李樾 谭添