

Problem 1:

a)

1. Insert 3:

3

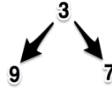
Array: 3

2. Insert 9:



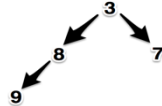
Array: 3 9

3. Insert 7:



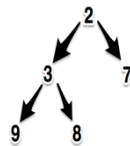
Array: 3 9 7

4. Insert 8:



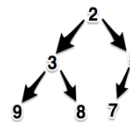
Array: 3 8 7 9

5. Insert 2:



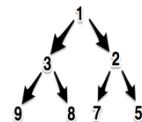
Array: 2 3 7 9 8

6. Insert 5:



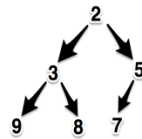
Array: 2 3 5 9 8 7

7. Insert 1:



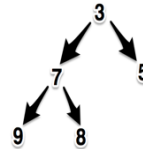
Array: 1 3 2 9 8 7 5

Delete Min (First time):



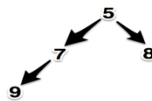
Array: 2 3 5 9 8 7

Delete Min (Second time):



Array: 3 7 5 9 8

Delete Min (Third time):



Array: 5 7 8 9

b)

Max heap: Array [null 9 8 7 3 2 5 1]

Delete Max: Array [null 8 3 7 1 2 5 9]

Delete Max: Array [null 7 3 5 1 2 8 9]

Delete Max: Array [null 5 3 2 1 7 8 9]

Delete Max: Array [null 3 1 2 5 7 8 9]

Delete Max: Array [null 2 1 3 5 7 8 9]

Delete Max: Array [null 1 2 3 5 7 8 9]

Delete Max: Array [null 1 2 3 5 7 8 9]

Problem 2:

a. $N + (N + 1) + (((N + (N + 1))) + 1) = 4N + 3 = N$

b. $2^{2\log N+1} = 2^{2\log N+\log 2} = 2^{\log 2N^2} = 2N^2 = N^2$

c. $2^{4.1\log N+1} = 2^{4.1\log N+\log 2} = 2^{\log 2N^{4.1}} = 2N^{4.1} = N^{4.1}$

d. $2^N - 1 = 2^N$