

## Neural Networks

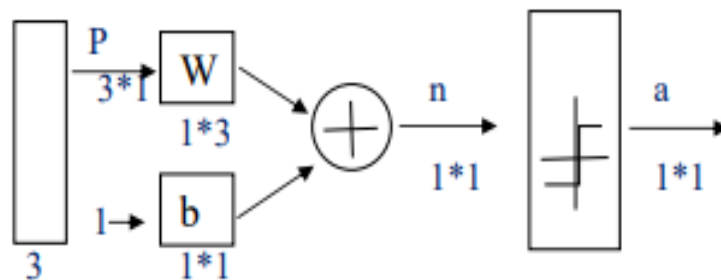
### Sheet -1

1- Q1

Solve 1:

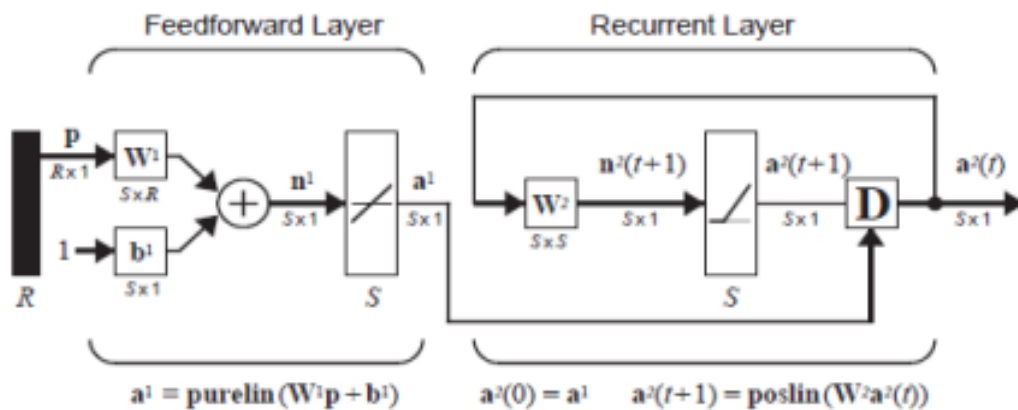
i- The design of perceptron

Input



Let's assume weight matrix  $W = [0 \ -1 \ 1]$  and  $b = 0$   
And the target of banana and pineapple  $t1 = -1$  ,  $t2 = 1$   
And the transfer function is **Symmetric Hard Limit**.

ii- The design of hamming

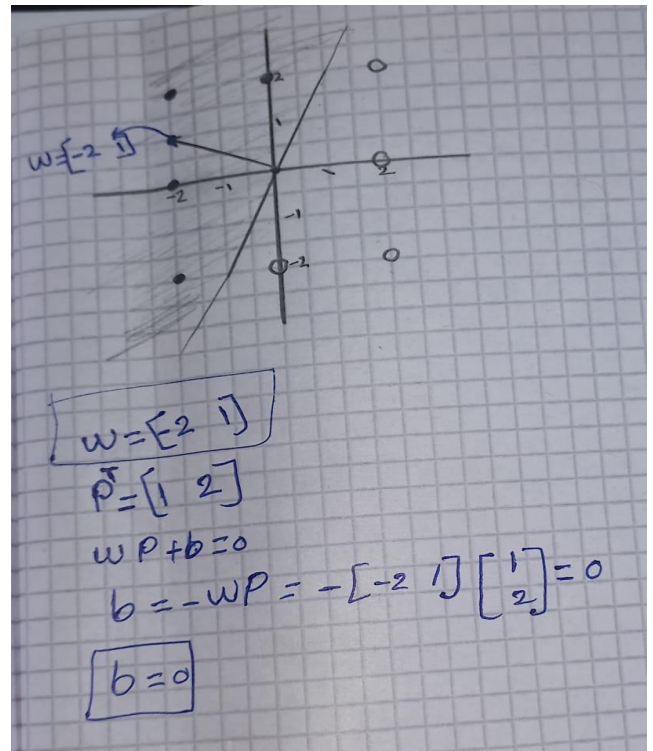
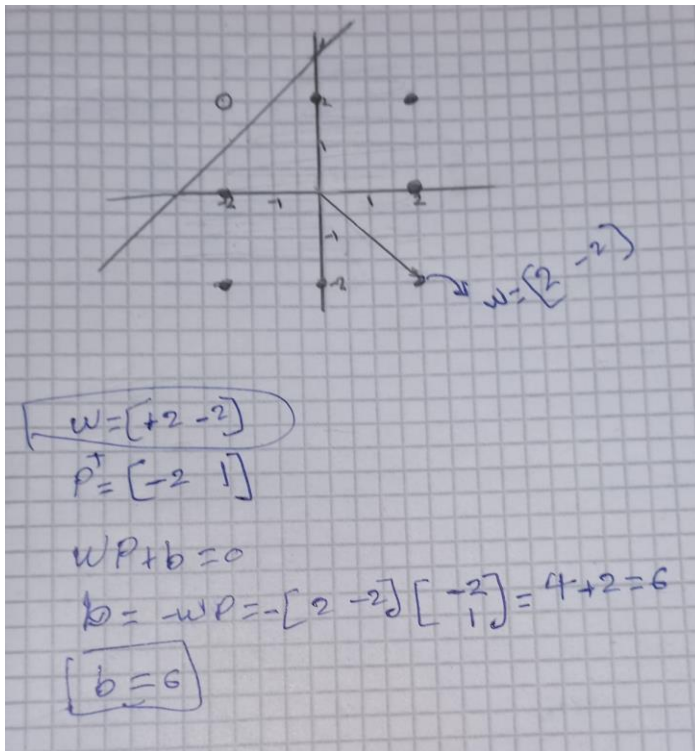


First layer has 2 neurons and 3 input so  $w$  will be  $2 \times 3$  and  $b$   $2 \times 1$   
 $S = 2$  and  $R = 3$  in the diagram.

In first layer:  $W^1 = \begin{bmatrix} -1 & 1 & -1 \\ -1 & -1 & 1 \end{bmatrix}$        $b^T = [R \ R] = [3 \ 3]$

Second layer:  $W^2 = \begin{bmatrix} 1 & -\epsilon \\ -\epsilon & 1 \end{bmatrix} = \begin{bmatrix} 1 & -0.5 \\ -0.5 & 1 \end{bmatrix}$

2- Q2



3- Q3 Mention different transfer function that can be used in Neural Network

- 1- Hard limit
- 2- symmetrical hard limit
- 3- linear
- 4- saturating linear
- 5- symmetrical saturating linear
- 6- log-sigmoid
- 7- hyperbolic tangent sigmoid
- 8- positive linear
- 9- competitive

4- Q4

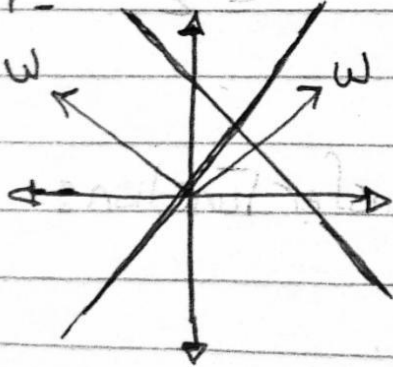
i-  $w = \begin{bmatrix} 1 \\ -1 \end{bmatrix}$  ,  $b = \begin{bmatrix} -2 \end{bmatrix}$

$\therefore R=2, S=2$   
 $\therefore \text{num of classes} = 2^2 = 4 \text{ classes}$

ii-  $WP+b$  , Suppose  $P = \begin{bmatrix} 1 \\ -1 \end{bmatrix}$   
 $\begin{bmatrix} 0 \\ -2 \end{bmatrix} + \begin{bmatrix} -2 \\ 0 \end{bmatrix} = \begin{bmatrix} -2 \\ -2 \end{bmatrix}$

Use Symmetric Transfer Function  $f(x) = \frac{1}{2} (1 + \tanh(x))$   
 $a < 0 \rightarrow -1$  ,  $a > 0 \rightarrow 1$   
 $\therefore a = \begin{bmatrix} -1 \\ -1 \end{bmatrix}$

iii-



5- Q5

5-

$$P_1 = \begin{bmatrix} 2 \\ 2 \end{bmatrix}, t_1 = 0$$

$$P_2 = \begin{bmatrix} 1 \\ -2 \end{bmatrix}, t_2 = 1$$

$$P_3 = \begin{bmatrix} -2 \\ 2 \end{bmatrix}, t_3 = 0$$

$$P_4 = \begin{bmatrix} -1 \\ 1 \end{bmatrix}, t_4 = 1$$

- use  $W(0) = \begin{bmatrix} 0 & 0 \end{bmatrix}, b(0) = 0$
- use transfer function is HardLimit
  - $n \geq 0 \rightarrow a = 1$
  - $n < 0 \rightarrow a = 0$

$$W(\text{new}) = W(\text{old}) + eP^T$$

$$b(\text{new}) = b(\text{old}) + e$$

$$e = t - a$$

$$a_1 = \text{hardlim}(W(0)P_1 + b) = \text{hardlim}\left(\begin{bmatrix} 0 & 0 \end{bmatrix} \begin{bmatrix} 2 \\ 2 \end{bmatrix} + 0\right)$$

$$a_1 = \text{hardlim}(0) = 1 \neq t_1$$

$$W(1) = W(0) + (t - a)P_1^T$$

$$W(1) = \begin{bmatrix} 0 & 0 \end{bmatrix} + (-1) \begin{bmatrix} 2 & 2 \end{bmatrix} = \begin{bmatrix} -2 & -2 \end{bmatrix}$$

$$b(1) = b(0) + (t - a) = 0 + (-1) = -1$$

$$a_2 = \text{hardlim}(W(1)P_2 + b(1)) = \text{hardlim}\left(\begin{bmatrix} -2 & -2 \end{bmatrix} \begin{bmatrix} 1 \\ -2 \end{bmatrix} - 1\right) = \text{hardlim}(1) = 1 = t_2$$

$$a_3 = \text{hardlim}(W(1)P_3 + b(1)) = \text{hardlim}\left(\begin{bmatrix} -2 & -2 \end{bmatrix} \begin{bmatrix} -2 \\ 2 \end{bmatrix} - 1\right) = \text{hardlim}(-1) = 0 = t_3$$

$$a_4 = \text{hardlim}(W(1)P_4 + b(1)) = \text{hardlim}\left(\begin{bmatrix} -2 & -2 \end{bmatrix} \begin{bmatrix} -1 \\ 1 \end{bmatrix} - 1\right) = \text{hardlim}(-1) = 0 \neq t_4$$

$$W(2) = W(1) + (t - a)P_4^T$$

$$W(2) = \begin{bmatrix} -2 & -2 \end{bmatrix} + (1) \begin{bmatrix} -1 & 1 \end{bmatrix} = \begin{bmatrix} -3 & -1 \end{bmatrix}$$

$$b(2) = b(1) + (t - a) = -1 + 1 = 0$$

$$a_1 = \text{hardlim}(W(2)P_1 + b(2)) = \text{hardlim}\left(\begin{bmatrix} -3 & -1 \end{bmatrix} \begin{bmatrix} 2 \\ 2 \end{bmatrix} + 0\right) = \text{hardlim}(-8) = 0 = t_1$$

$$a_2 = \text{hardlim}(W(2)P_2 + b(2)) = \text{hardlim}\left(\begin{bmatrix} -3 & -1 \end{bmatrix} \begin{bmatrix} 1 \\ -2 \end{bmatrix} + 0\right) = \text{hardlim}(-1) = 0 \neq t_2$$

$$W(3) = W(2) + (t - a)P_2^T$$

$$W(3) = \begin{bmatrix} -3 & -1 \end{bmatrix} + (1) \begin{bmatrix} 1 & -2 \end{bmatrix} = \begin{bmatrix} -2 & -3 \end{bmatrix}$$

$$b(3) = b(2) + (t - a) = 0 + 1 = 1$$

$$a_3 = \text{hardlim}(W(3)P_3 + b(3)) = \text{hardlim}\left(\begin{bmatrix} -2 & -3 \end{bmatrix} \begin{bmatrix} -2 \\ 2 \end{bmatrix} + 1\right) = \text{hardlim}(-1) = 0 = t_3$$

$$a_4 = \text{hardlim}(W(3)P_4 + b(3)) = \text{hardlim}\left(\begin{bmatrix} -2 & -3 \end{bmatrix} \begin{bmatrix} -1 \\ 1 \end{bmatrix} + 1\right) = \text{hardlim}(0) = 1 = t_4$$

$$a_1 = \text{hardlim}(W(3)P_1 + b(3)) = \text{hardlim}\left(\begin{bmatrix} -2 & -3 \end{bmatrix} \begin{bmatrix} 2 \\ 2 \end{bmatrix} + 1\right) = \text{hardlim}(9) = 1 = t_1$$

$$a_2 = \text{hardlim}(W(3)P_2 + b(3)) = \text{hardlim}\left(\begin{bmatrix} -2 & -3 \end{bmatrix} \begin{bmatrix} 1 \\ -2 \end{bmatrix} + 1\right) = \text{hardlim}(5) = 1 = t_2$$

then  $W = \begin{bmatrix} -2 & -3 \end{bmatrix}$  &  $b = 1$

# مع تحياتي بالتوفيق



6- Q6

6-  $W = (3 \ 2)$   $P = [-5 \ 7]^T$   
 $n = 0.5$   
 $WP + b = 0.5$   
 $(3 \ 2) \begin{bmatrix} -5 \\ 7 \end{bmatrix} + b = 0.5$   
 $-15 + 14 + b = 0.5$   
 $b = 1.5$   
 i- No  
 ii- yes &  $b = 1.5$   
 iii- yes &  $\frac{1}{1+e^{-n}} = 0.5 \Rightarrow n = 0 \Rightarrow WP + b = 0$   
 $-1 + b = 0$   
 $b = 1$   
 iv- No

7- Q7

⑦  $R = 4$   $S = 6$   
 i- 6  
 ii-  $S \times R = 6 \times 4 \rightarrow W^1$  Layer 1  
 $S \times S = 6 \times 6 \rightarrow W^2$  Layer 2  
 iii- there isn't enough information for that question

**Answer the following MCQs questions**

- 8- What are **dendrites**?
- a) **fibers of nerves**
  - b) nuclear projections
  - c) other name for nucleus
  - d) none of the mentioned
- 9- What is **shape** of **dendrites** like
- a) oval
  - b) round
  - c) **tree**
  - d) rectangular
- 10- What is purpose of **Axon**?
- a) receptors
  - b) **transmitter**
  - c) **transmission**
  - d) none of the mentioned
- 11- The **cell body of neuron** can be analogous to what **mathematical operation**?
- a) **summing**
  - b) differentiator
  - c) integrator
  - d) none of the mentioned
- 12- In a **three layer** network, number of classes is determined by?
- a) number of units in second layer
  - b) **number of units in third layer**
  - c) number of units in second and third layer
  - d) none of the mentioned
- 13- Which is the most direct **application** of **neural networks**?
- a) vector quantization
  - b) pattern mapping
  - c) **pattern classification**
  - d) control applications
- 14- In a three layer network, number of classes is determined by?
- a) number of units in second layer
  - b) **number of units in third layer**
  - c) number of units in second and third layer
  - d) none of the mentioned

15- For what purpose, **hamming** network is suitable?

- a) **classification**
- b) association
- c) pattern storage
- d) none of the mentioned

16- **Prototype** is consisting of

- |                       |                       |                       |
|-----------------------|-----------------------|-----------------------|
|                       | <i>shape</i>          |                       |
| a) [ <i>texture</i> ] | b) [ <i>texture</i> ] | c) [ <i>texture</i> ] |
| <i>size</i>           | <i>weight</i>         | <i>color</i>          |