

7. Give an efficient method for generating nine uniform points on $(0, 1)$ conditional on the event that no two of them are within 0.1 of each other.

Use Gibbs sampler.

Step1 : Generate 9 points from $\text{uniform}(0, 1)$

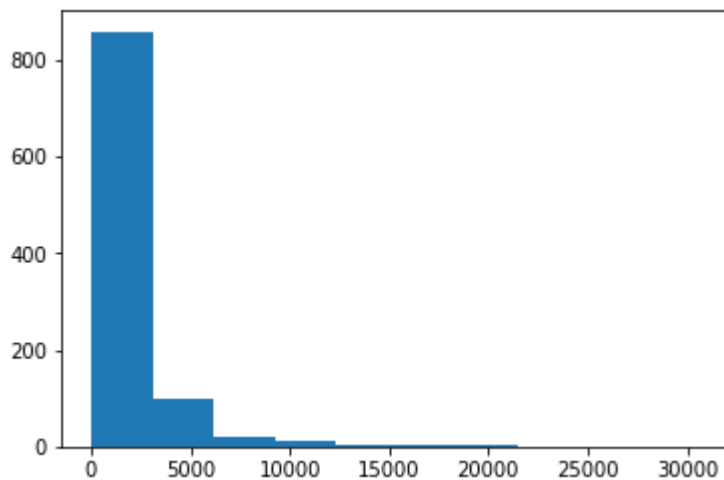
Step2 : Generate U_1, U_2 from $U(0, 1)$, $I = \text{int}(nU_1)+1$

Step3 : $D_i = U_1 - X[j]$, for $j \neq I, i=1, \dots, 8$

Step4 : If $D_i > 0.1$ for all $i = 1, \dots, 8$, $X[I] = U_2$; else go to step2

Step5 : Repeat until all point distance not within 0.1

Via simulation 1000 times



Most are 0~2500 succeed