## Notes on Audio Processing

As of March 19, 2019

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\begin{array}{l} \operatorname{signal} \ \ldots \ldots \ldots \mathbb{R} \to \mathbb{C} \\ i^2 = -1 \\ \\ \operatorname{correlate} \left( a, \ b \right)_t = a_t \cdot \overline{b_t} \\ \\ \operatorname{fourier} \left( \operatorname{out} \ (\operatorname{signal}), \ \operatorname{in} \ (\operatorname{signal}), \ \operatorname{frequency} \in \mathbb{R}, \ \operatorname{bandwidth} \in \mathbb{R} \right) \ \{ \\ \operatorname{Let} \ a = \operatorname{in} \\ \operatorname{Let} \ b_t = e^{i \cdot \omega \cdot t} \quad \text{with} \ \omega = 2\pi \cdot \operatorname{frequency} \quad \forall \ t \in \operatorname{range} \\ \operatorname{out} \leftarrow \operatorname{correlate}(a, b) \\ \operatorname{out} \leftarrow \operatorname{lowPass}(\operatorname{out}, \operatorname{bandwidth}) \\ \operatorname{out} \leftarrow \operatorname{lowPass}'(\operatorname{out}, \operatorname{bandwidth}) \\ \} \end{array}
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The beauty of that definition lies within its simplicity:

It only consists of building blocks that are simple to implement and cheap in run-time cost.

The 'lowPass' and 'correlate' procedures need only make a single pass over the signal data, thus run in  $\mathcal{O}(n)$  time.

 $e^{i\cdot\omega\cdot t}$  too can be implemented to run very quickly.